Theory and demonstration of plasma measurement using Langmuir probe 電漿量測之蘭摩爾探針原理與實作

Po-Yu Chang 張博宇

Institute of Space and Plasma Sciences

National Cheng Kung University

pchang@mail.ncku.edu.tw

2021 winter break 1/18(Mon.) – 1/22(Fri.) 14:00-17:40

http://capst.ncku.edu.tw/PGS/index.php/teaching/

Lecture 2

2021/1/19 updated 1

Course Outline



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1. Introduction to plasma

a. What is Plasma?

- b. How to generate plasma
- c. Applications of plasma
- 2. Theory of Langmuir probe
 - a. Sheath
 - b. Single Langmuir probe
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Charged particles gyro around magnetic field lines



http://www.ipp.cas.cz/vedecka_struktura_ufp/tokamak/tokamak_compass/diagnostics/ mikrovInne-diagnostiky/ece-ebw-radiometr.html http://www-ssg.sr.unh.edu/tof/Smart/Students/lees/periods.html https://www.euro-fusion.org/2011/09/tokamak-principle-2/ A plasma is a gas in which an important fraction of the atoms is ionized so that the electrons and ions are separated freely



http://ocw.mit.edu/courses/nuclear-engineering/22-611j-introduction-to-plasma-physics-i-fall-2003/lecture-notes/

A plasma can be created when the ionization rate is higher than the recombination rate



J. D. Huba \NRL Plasma Formulary", Naval Research Laboratory, 2013:

There are several Important plasma parameters that need to be considered



$$\lambda_D \equiv \left(\frac{KT_e}{4\pi n e^2}\right)^{1/2}$$

Plasma parameter

$$\Lambda \equiv n \frac{4\pi}{3} \lambda_D^3$$

1 -

Plasma frequency

$$\omega_{\rm pe} \equiv \left(rac{4\pi n_e e^2}{m_e}
ight)^{1/2}$$

• Collision time
$$au_e \equiv \frac{3\sqrt{m_e(RT_e)^{3/2}}}{4\sqrt{2\pi}n\ln\Lambda}$$

• Hall parameter $\chi \equiv \omega_{ce} \tau_e$, where $\omega_{ce} \equiv \frac{eB}{m_e c}$ is the electron gyrofrequency

 $2 \sqrt{2}$

• Plasma beta $\beta \equiv \frac{P}{P_B}$, where $P_B \equiv \frac{B^2}{8\pi}$ is the magnetic pressure

A test ion in the plasma gathers a shielding cloud that tends to cancel its own charge



Francis F. Chen, \Introduction to plasma physics and controlled fusion"8

Debye shielding is a phenomenon such that the potential due to a test charge in a plasma falls off much faster than in vacuum



• Vacuum potential:

 $\phi = \frac{\phi_0}{\phi_0}$



$$\phi = rac{\phi_0}{r} \exp\left(-rac{r}{\lambda_D}
ight) \quad \lambda_D \approx \left(rac{KT_e}{4\pi n e^2}
ight)^{1/2}$$

Electron plasma frequency is the characteristic frequency such that electrons oscillate around their equilibrium positions



Mechanism of plasma oscillations.

• Plasma frequency:

$$\omega_{\rm pe} \equiv \omega = \left(\frac{4\pi n_e e^2}{m_e}\right)^{1/2}$$

• Wave number k becomes imaginary when $\omega < \omega_e$.

$$E = E_0 e^{i(\mathbf{k}\mathbf{x}-\boldsymbol{\omega}\mathbf{t})} = E_0 e^{-k_I t} e^{i(k_R x-\boldsymbol{\omega}\mathbf{t})}$$

The cutoff of the electromagnetic wave is important in laser fusion and in the interaction of radio waves with the ionosphere



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Methods of plasma production



- DC electrical discharges
 - Dark electrical discharges in gases
 - DC electrical glow discharges in gases
 - DC electrical arc discharges in gases
- AC electrical discharges
 - RF electrical discharges in gases
 - Microwave electrical discharges in gases
 - Dielectric-barrier discharges (DBDs)
- Other mechanism
 - Laser produced plasma
 - Pulsed-power generated plasma

Methods of plasma production



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The region where the current exponentially increases is called the Townsend discharge



- Primary electrons: electrons from the cathode due to photoemission, background radiation, static chages, or other processes.
- Secondary electrons: electrons emitted from the cathode per incident ion or photon created from ionization in gas.
 - Electrical breakdown occurs when applied voltage is greater than the breakdown voltage

Collision frequency and electron energy gained from electric field are both important to electrical breakdown



 The minimum of the Paschen curve corresponds to the Stoletow point, the pressure at which the volumetric ionization rate is a maximum.



DC electrical glow discharges in gases

 The internal resistance of the power supply is relatively low, then the gas will break down at the voltage V_B, and the discharge tube will move from the dark discharge regime into the low pressure normal glow discharge regime.



Glow discharge in a glass jar







Discharge may enter glow-to-arc transition region if the cathode gets hot enough to emit electrons thermionically



 If the cathode gets hot enough to emit electrons thermionically and the internal impedance of the power supply is sufficiently low, the discharge will make a transition into the arc regime.

DC electrical arc discharges in gases



- An arc is highly luminous and is characterized by high currents (> 1 A) and current densities (A=cm² ≥ kA/cm²).
- Cathode voltage fall is small (≤10 V) in the region of high spatial gradients within a few mm of the cathode.

AC electrical discharges deliver energy to the plasma without contact between electrodes and the plasma

- DC electrical discharge a true current in the form of a flow of ions or electrons to the electrodes.
- AC electrical discharge the power supply interacts with the plasma by displacement current.
 - Inductive radio frequency (RF) electrical discharges
 - Capacitive RF electrical discharges
 - Microwave electrical discharges
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- Optical (laser) produced plasma

RF can interact with plasma inductively or capacitively





The plasma is generated by the induced electric field from the oscillating magnetic field



High voltage initiation is usually required for inductive RF plasma torches







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Symmetrical capacitive RF discharge model



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Microwave plasma reactor configurations



Waveguide coupled reactor

 Resonant or multimode cavity – if the impedance matching is good, more energy can be fed into the cavity.



Strong absorption occurs when the frequency matches the electron cyclotron frequency

• Electron cyclotron resonance (ECR) plasma reactor



Electron cyclotron frequency depends on magnetic field only

$$m_e \frac{d \, \vec{v}}{dt} = -\frac{e}{c} \, \vec{v} \times \vec{B}$$

• Assuming $\overrightarrow{B} = B\widehat{z}$ and the electron oscillates in x-y plane

$$m_e v_x = -\frac{e}{c} B v_y \qquad m_e v_z = 0$$
$$m_e v_y = \frac{e}{c} B v_x \qquad m_e v_z = 0$$
$$\ddot{v}_x = -\frac{eB}{m_e c} \dot{v}_y = -\left(\frac{eB}{m_e c}\right)^2 v_x$$
$$\ddot{v}_y = -\frac{eB}{m_e c} \dot{v}_x = -\left(\frac{eB}{m_e c}\right)^2 v_y$$



• Therefore

$$\omega_{\rm ce} = \frac{eB}{m_e c}$$

Electrons keep getting accelerated when a electric field rotates in electron's gyrofrequency

$$m_e \frac{d \vec{v}}{dt} = -\frac{e}{c} \vec{v} \times \vec{B} - e \vec{E} \qquad \vec{B} = B_0 \hat{z} \qquad \vec{E} = E_0 [\hat{x} \cos(\omega t) + \hat{y} \sin(\omega t)]$$

$$m_e \dot{v}_x = -\frac{e}{c} B v_y + E_0 \cos(\omega t) \qquad m_e \dot{v}_y = -\frac{e}{c} B v_x + E_0 \cos(\omega t) \qquad m_e \dot{v}_z = 0$$

$$\ddot{v}_x = -\frac{eB}{m_e c} \dot{v}_y - \frac{E_0}{m_e} \omega \cos(\omega t) = -\omega_{ce}^2 v_x - \frac{E_0}{m_e} (\omega_{ce} + \omega) \cos(\omega t)$$
$$\ddot{v}_y = -\frac{eB}{m_e c} \dot{v}_x + \frac{E_0}{m_e} \omega \sin(\omega t) = -\omega_{ce}^2 v_y + \frac{E_0}{m_e} (\omega_{ce} + \omega) \sin(\omega t)$$





Electric field in a circular polarized electromagnetic wave keeps rotating as the wave propagates

• Right-handed polarization

Left-handed polarization



Only right-handed polarization can resonance with electron's gyromotion



FIGURE 13.5. Basic principle of ECR heating: (*a*) continuous energy gain for righthand polarization; (*b*) oscillating energy for left-hand polarization (after Lieberman and Gottscho, 1994).

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Dielectric-barrier discharges (DBDs)


Atmospheric-pressure cold helium microplasma jets





J. L. Walsh, et al., J. Phys. D: Appl. Phys., 43, 075201 (2010) 37

Atmospheric-Pressure Plasma







https://www.itri.org.tw/chi/Content/Publications/contents.aspx?Sitel D=1&MmmID=2000&MSid=745416417706673311 Plasma medicine, by Alexander Fridman and Gary Friedman

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Laser is absorbed in underdense plasma through collisional process called inverse bremsstrahlung



Electrons accelerated by electric fields

Electrons collide with other electrons / ions

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Applications of plasma



- 1. Material Processing
- 2. Plasma in space
- 3. Biomedical application
- 4. High energy particle accelerator
- 5. Electric propulsion
- 6. Controlled thermonuclear fusion

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A semiconductor device is fabricated by many repetitive production process



A semiconductor device is fabricated by many repetitive production process





Sputtering deposition



A semiconductor device is fabricated by many repetitive production process



There are two types of etching: isotropic vs anistropic





A semiconductor device is fabricated by many repetitive production process



Plasma-immersion ion implantation (PIII)



- Silicon doping ions such as B, P, As are implanted
- Surface hardening of metals N, C are implanted

A semiconductor device is fabricated by many repetitive production process



Ultraviolet lithography (EUVL) is one of the key technologies in semiconductor manufacturing nowadays

The process technology of Taiwan Semiconductor Manufacturing **Company Limited (TSMC):**



190, dep, 200, 400, 200, 200, 100, 000, 980, 880,

- Optical diffraction needs to be taken into account.
- Shorter wavelength is preferred.
 - Light source with a center wavelength of 13.5 nm is used.

https://www.tsmc.com/chinese/dedicatedFoundry/technology/logic.htm

EUV light with λ =13.5 nm is used

T SAL

• Multilayer mirrors is needed for reflecting EUV light.



Reflected Light: Combination of 6 Beams

https://www.edmundoptics.com/knowledge-center/trending-in-optics/extreme-ultraviolet-optics/ V. Bakshi, EUV sources for lithography

EUV light is generated when material is heated to 35~40 eV (~450,000 K)



Wavelength (nm)

- At T=35-40 eV (~450,000 K), in-band emission occurs.
- Xenon:
 - $4p^{6}4d^{8} \rightarrow 4p^{6}4d^{7}5p$ from single ion stage Xe¹⁰⁺
 - UTA @ 11 nm
- Tin:
 - $4p^{6}4d^{N} \rightarrow 4p^{5}4d^{N+1} + 4p^{6}4d^{N-1}4f$ (1 \leq N \leq 6) in ions ranging from Sn⁸⁺ to Sn¹²⁺
 - UTA @ 13.5 nm

UTA: unresolved transition array

EUV light sources from laser-produced plasma (LPP)





UTA @ 13.5 nm •

Tin:

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Earth's magnetic field







https://www.nasa.gov/mission_pages/sunearth/news/gallery/Earthsmagneticfieldlines-dipole.html http://www.pas.rochester.edu/~blackman/ast104/emagnetic.html

Aurora occurs when energetic electrons penetrating into atmosphere in the pole regions



- O₂: green or dark red
- N₂: blue or purple



https://flashpack.com/insights/2014/11/20/aurora-australis-forget-thenorthern-lights-have-you-heard-about-the-southern-lights/

J. Atoms Terr. Phys., **32** (1970) 1015-1045 Johnson, 1969; Luhmann, 1995

Reconnection





https://www.youtube.com/watch?v=7sS3Lpzh0Zw

Reconnections occur in many locations



• The Aurora Borealis:

https://www.youtube.com/watch?v=IT3J6a9p_o8

http://www.natalia-robba.com/myblog/travel/the-aurora-borealis-thenorthern-lights-everything-you-need-to-know/

Applications of plasma



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Biomedical applications of low temperature plasma







Plasma medicine, by Alexander Fridman and Gary Friedman Biochem Biophys Res Commun. 2006 May 5; 343(2): 351–360.

Melanoma shrinks after the treatment



- Day 0-3: 3 applications of 100 pulses (300 ns, 40 kv/cm, 0.5 Hz), 30 min apart
- Day 4: single application using 5 <u>mm dia</u>meter parallel plate electrode

Biochem Biophys Res Commun. 2006 May 5; 343(2): 351–360.

Applications of plasma



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4. High energy particle accelerator

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Electrons can be accelerated by a plasma wake generated by a short pulse laser



http://cuos.engin.umich.edu/researchgroups/hfs/research/laser-wakefield-acceleration/ https://i.ytimg.com/vi/CA-SDf1wvTQ/maxresdefault.jpg

Electrons with a maximum energy of 320 MeV are generated



Plasma density (cm-3) x 1019



c

Applications of plasma



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Comparison between liquid rockets and ion thrusters



- Liquid rockets
 - u~4500 m/s
 - Isp~450 s
 - Energy ~ 100GJ
 - Power ~ 300MW
 - Thrust ~ 2x10⁶ N
- Ion thrusters
 - u~30000 m/s
 - Isp~3000 s
 - Energy ~ 1000GJ
 - Power ~ 1kW
 - Thrust ~ 0.1 N





https://www.grc.nasa.gov/WWW/K-12/airplane/Irockth.html https://defence.pk/pdf/threads/isro-to-test-electric-propulsion-on-satellites.411176/

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The "iron group" of isotopes are the most tightly bound



http://hyperphysics.phy-astr.gsu.edu/hbase/nucene/nucbin.html

Nuclear fusion and fission release energy through energetic neutrons



Nuclear fusion provides more energy per atomic mass unit (amu) than nuclear fission

Fusion of ²H+³H:
$$\frac{Q}{A} = \frac{17.6 \ MeV}{(3+2) \ amu} = 3.5 \ \frac{MeV}{amu}$$

Fission of ²³⁵U: $\frac{Q}{A} = \frac{200 \ MeV}{236 \ amu} = 0.85 \ \frac{MeV}{amu}$

	Half-life (years)
U235	7.04x10 ⁸
U238	4.47x10 ⁹
Tritium	12.3
Fusion is much harder than fission



D (🕇

- **Fission:** $n + {}^{235}_{92} U \rightarrow {}^{236}_{92} U \rightarrow {}^{144}_{56} Ba + {}^{89}_{36} Kr + 3n + 177 \text{ MeV}$
- **Fusion:** $D + T \to He^4 (3.5 \text{ MeV}) + n (14.1 \text{ MeV})$







^{*}NRL Plasma Formulary, Naval Research Laboratory, Washington, DC 203785-5320

The plasma is too hot to be contained

 Solution 1: Magnetic confinement fusion (MCF), use a magnetic field to contain it. P~atm, τ~sec, T~10 keV (10⁸ °C)



https://www.euro-fusion.org/2011/09/tokamak-principle-2/ https://en.wikipedia.org/wiki/Stellarator

There is a long way to go, but we are on the right path...



• ITER



- Schedule of ITER:
 - Dec 2025
 - 2035

First Plasma Deuterium-Tritium Operation begins

Wendelstein 7-X

Plasma is confined by its own inertia in inertial confinement fusion (ICF)





A spherical capsule can be imploded through directly or indirectly laser illumination





Laboratory for Laser Energetics, University of Rochester is a pioneer in laser fusion

- **OMEGA** Laser System
 - 60 beams
 - >30 kJ UV on target
 - 1%~2% irradiation nonuniformity
 - Flexible pulse shaping

- OMEGA EP Laser System
 - 4 beams; 6.5 kJ UV (10ns)
 - Two beams can be highenergy petawatt
 - 2.6 kJ IR in 10 ps
 - Can propagate to the OMEGA or OMEGA EP target chamber





The OMEGA Facility is carrying out ICF experiments using a full suite of target diagnostics



The 1.8-MJ National Ignition Facility (NIF) will demonstrate ICF ignition and modest energy gain



OMEGA experiments are integral to an ignition demonstration on the NIF.

Targets used in ICF







Nature letter "Fuel gain exceeding unity in an inertially confined fusion implosion"



Fuel gain exceeding unity was demonstrated for the first time.

We are really closed!





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