

# Pulsed Power system

PI

Prerequisite courses:

Electric Circuits.

Engineering Mathematics / Phys Mathematics (ODE)

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② No office hour, please feel free to stop by my office whenever my door is open & nobody is in my office. Or you may email me to schedule a meeting.

2018 (E) 14:10 ~ 17:00

③ class time : 9:10 ~ 12:00  
→ 9:10 ~ 11:30  
11:30 ~ 12:00

English ~~class~~ with 10 mins break  
~~class~~ Mandarin for gr

④ Assignments : 70% → No roll call.

Presentations : 30%  
Pulsed Power by Gennady A. Mesyats.  
Foundations of pulsed power by Technology by  
Pulsed power systems by Jane Lehr & Pratheepon  
Circuits analysis by Cunningham and Stoller  
Pulse power formulary by Richard J. Adler

⑤ References:  
Additional References:  
Pulsed Power by Gennady A. Mesyats

J. C. Martin on Pulsed Power

\* Class material: myweb.ncku.edu.tw/~pchang

## \* Course outline:

- Introduction to pulsed-power system. - (9/14)  $\xrightarrow[2016]{}$  9/21. 9/12  $\xrightarrow[2017]{}$  9/21. 9/12  $\xrightarrow[2018]{}$  p2
- Review of circuit analysis - 9/21. 9/12  $\xrightarrow[2017]{}$  9/21. 9/12  $\xrightarrow[2018]{}$  4W. of kcc circuits

72. Static and dynamic breakdown strength of dielectric material. - (9/28, 10/5)  $\xrightarrow[2017]{}$  9/28  $\xrightarrow[2018]{}$  9/26

- [ Gas.  $\rightarrow$  avalanche, Townsend condition, Paschen Law. \*
- [ Liquid
- [ Solid.

73 Energy storage. (10/12 - 10/19.)  $\xrightarrow[2017]{}$  10/3, 10/17  $\xrightarrow[2018]{}$

- [ pulsed discharge capacitors

- Marx Generators.

- [ Inductive energy storage.

- nw. of exploding wire

74 Switches. 10/26 - ~~11/2~~. 11/9  $\xrightarrow[2017]{}$

- ~~electron gun~~  
solving poisson's eq.

- [ Closing switches  $\rightarrow$  gas switches

- [ Opening switches  $\rightarrow$

75 Pulse-forming networks

~~11/2~~; ~~11/16~~ 11/23

$\xrightarrow[2017]{}$  11/10, 11/11

- [ Transmission lines

- [ RLC Networks

$\xrightarrow[2017]{}$  11/30

76 Pulse transmission and transformation  $\xrightarrow[2017]{}$  ~~11/2~~ - ~~11/3~~ 11/17

- [ self-magnetic insulation in vacuum lines

- [ pulse transformers

- [ High voltage power supply

- [ Transformation lines

$\xrightarrow[2017]{}$  11/28, 11/29  
 $\xrightarrow[2018]{}$

37. Power and voltage adding ~~12/14~~  
12/17 12/2  
2018 P3

- └ Adding of power
- └ voltage adding

38. Diagnostics. 12/1 12/20 (12/9 12/6)  
12/17 2018

- └ Electromagnetic - Field Sensors
  - └ Capacitive sensor
  - └ Inductive
- └ Current - viewing resistors (CVRs)
- └ Current measurements based on Faraday Effect.
- └ Z - field - - - - - Electro-optic effects.
- └ Magnetic ion energy analysers
- └ Vacuum voltage monitors.

39. Applications of pulsed-power system 1/4 1/2  
2018 2018

⊗

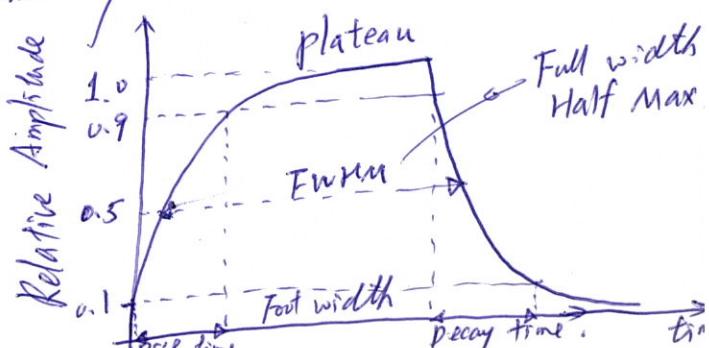
### 3 Introduction to pulsed-power system

P4

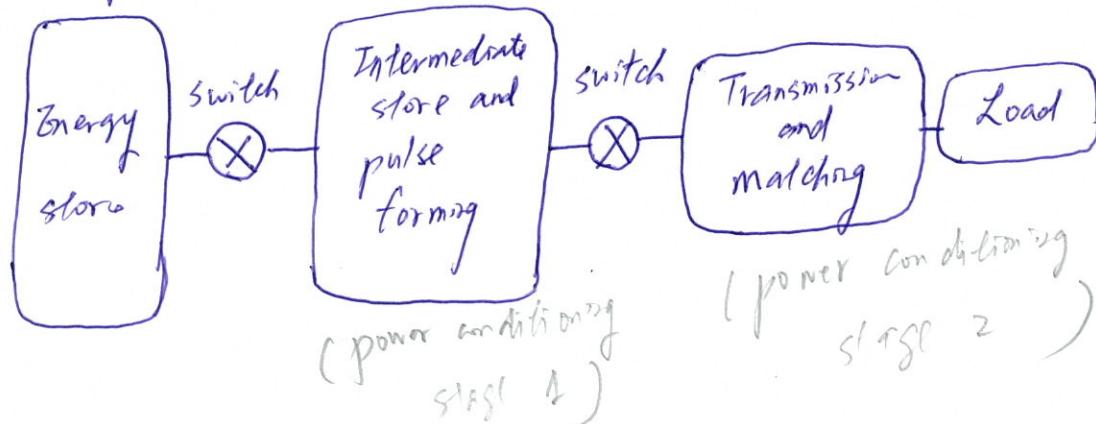
- \* Pulsed power is a scheme where stored energy is discharged as electrical energy into a load in a short pulse or as short pulses with a controllable repetition rate.
- \* Example of pulsed power in daily life:
  - Driven piles
  - Hammer.
  - making ~~steamy~~ rice cake. → great example of short pulses with a controllable repetition rate
- \* Pulsed power in general:
  - $P \sim 10^9 \text{ W}$  ( $1 \text{ GW}$ )
  - $E \gg \text{kJ}$

The highest energy and power that have been achieved in a single pulse are in the order of  $100 \text{ MJ}$  & few  $\mu\text{J}$  TW, respectively.

  - $V: 10 \text{ kV} \sim 50 \text{ MV}$
  - $I: 1 \text{ kA} \sim 10 \text{ MA}$ .
- \* A pulse is characterised by its shape, i.e., by its rise & fall times and its plateau region



- Pulse rise time - the time it takes the voltage to rise from 10% to 90%. P5
- Pulse fall time - decay fall - - - - - 90% to 10%.
- Both the fall and the rise time of a pulse depend on the evolution of the "Load impedance," which in most cases varies with time.
- Pulse duration - no unique definition.
  - ↳ FWHM
  - ② ~~sometimes~~ It is defined as the duration at 90% of the peak amplitude.
  - ⇒ Flatness of the plateau region is an important requirement for driving some ~~loads~~ such as Pockels cells.
- A ~~generator~~ generator scheme for the production of high-power electrical pulses is always based on an energy store that is charged slowly at a relatively low charging power and is discharged rapidly by acting a switch.
- To achieve the desired power magnification factor and to shape the pulse, the above process can be repeated several times.

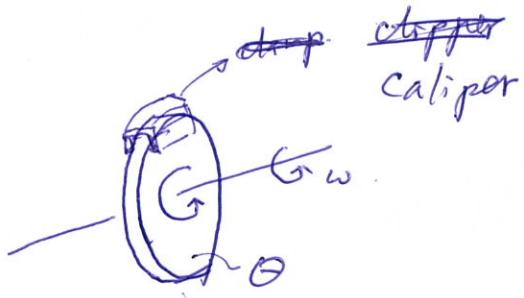


- \* The energy can be stored either chemically, mechanically, or electrically.

### Six: Mechanical energy:

$$W_{kin} = \frac{1}{2} \Theta \omega^2$$

↑                              ↓  
moment of inertia          angular frequency



For a massive cylinder:  $\Theta = \frac{1}{2} M r^2$

↑                              ↓  
mass                            radius

$$\Rightarrow W_{kin} = \frac{1}{2} \cdot \frac{1}{2} M r^2 \cdot \omega^2$$

$$\Rightarrow \text{Stored energy density: } \omega = \frac{W_{kin}}{M} = \frac{1}{4} r^2 \omega^2$$

- The ultimate energy density is limited by the tensile strength of the material used to construct the rotor.

$$\begin{aligned} d\Sigma &= \frac{dF}{A} \\ &= \frac{(rds)dr\sigma}{rds \cdot s} \cdot r^2 \\ &= \int r^2 \sigma dr \\ &= \int_0^R r^2 \sigma dr \\ &= \frac{1}{2} \int r^2 \sigma^2 dr \\ &= \int r^2 \sigma dr \end{aligned}$$

$$\Sigma = \int r^2 \omega^2 \frac{r^2}{2} dr \quad \text{for a stainless steel cylinder.}$$

↑                              ↓  
tensile strength                  $\Sigma = \int r^2 \omega^2 \frac{r^2}{2} dr$

$$\omega_{max} = 400 \text{ rad/s.} \quad \text{AISI 302}$$

300  
stainless steel

$$\Sigma = 520 / 860 \text{ MPa}$$

↑                              ↑  
yield strength                 ultimate tensile strength.

$$\rho = 8.19 \text{ g/cm}^3 = 8190 \text{ kg/m}^3$$

$$\omega = \sqrt{\frac{\Sigma}{\rho r^2}} = \sqrt{\frac{860 \times 10^6}{8190 \times 1}} = 324 \text{ rad/s.} \quad 300$$

$$W_{kin} = \frac{1}{4} r^2 \omega^2 = \frac{1}{4} \cdot 1^2 \cdot \frac{400^2}{300} = \frac{4 \times 10^4}{4} \text{ J/kg} \Rightarrow 1.6 \times 10^8 \text{ J/m}$$

High strength alloy ASTM A514 steel

$$\rho = 7.8 \text{ g/cm}^3. \quad \Sigma = 690 / 760 \text{ MPa}$$

↑                              ↑  
yield strength                 ultimate tensile strength.

$$\omega = \sqrt{\frac{2 \times 690 \times 10^6}{7800 \times 1^2}} = 420 \sim 400 \text{ rad/s.}$$

$$W_{kin} = \frac{1}{4} r^2 \omega^2 = \frac{1}{4} \times 1 \times 400^2 = 4 \times 10^4 \text{ J/kg} = 3.1 \times 10^8 \text{ J/m}^3$$

- The problem with mechanical storage is to release the energy in a sufficiently short time. P7
- Several electrical compression stages are needed in combination with the mechanical storage to achieve the desired power level.

Sx.: Electrical energy can be stored either capacitively in an electric field or inductively in a magnetic field.

Sx1: Electric field:

$$W_e = \frac{1}{2} \epsilon_0 E^2$$

for oil/impregnated paper:  $\epsilon = 6$ , breakdown strength  $E = 0.78 \times 10^8 \text{ V/m}$

$$\Rightarrow W_e = \frac{1}{2} \times 6 \times 8.85 \times 10^{-12} \cdot (0.78 \times 10^8)^2 = 161 \text{ kJ/m}^3$$

With the finite packing density:

$$E \text{ for } E_{\text{re}} = \frac{1}{2} CV^2, C = \epsilon_0 \cdot \frac{A}{d}$$

$\Rightarrow d \rightarrow, E_{\text{re}} \rightarrow$  space is occupied by the electrode.

$\Rightarrow$  to estimate the energy storage in space

$$W_e' \approx \frac{1}{2} \times W_e \approx 80 \text{ kJ/m}^3$$



Sx2: Magnetic field:

$$W_B = \frac{\mu_0 I^2 \pi D^2}{32 \mu_0} \cdot \frac{B^2}{2 \mu_0}$$



The maximum energy density is limited by the onset of melting at the conductor surface or by the mechanical strength of the storage inductor.

$$C_o \cdot g \cdot T = \frac{B^2}{2 \mu_0} \cdot 2g \cdot \frac{1}{2 \mu_0} B^2 \vartheta$$

heat capacity  
per unit mass  
mass density  
surface temperature

a factor of order unity depending on the form of the pulse

$$B \cdot l = \mu_0 N I$$

$$\Rightarrow B = \mu_0 N I \propto I \quad \text{resistor.}$$

$$E = P \cdot t = I^2 \cdot R \cdot t \propto B^2 \cdot R \cdot t$$

$$\Rightarrow C_0 \beta T = \frac{1}{2\mu_0} B^2 \cdot l \approx \frac{B^2}{2\mu_0} \quad \text{take } \beta = 1$$

$$B^2 \approx \sqrt{2\mu_0 \cdot C_0 \cdot \rho \cdot T} = \sqrt{2 \times 4\pi \times 10^{-7} \times \frac{0.381 J}{10^3 \text{ kg} \cdot \text{K}}} \times 8960 \cdot (1081 - 25)$$

Copper:  $C_0 = 0.381 \text{ J/g} \cdot \text{K}$   $= 96 \text{ T} \approx 100 \text{ T}$

melting T:  $1081^\circ\text{C}$ .

$$\rho = 8.96 \text{ g/cm}^3 = 8960 \text{ kg/m}^3$$

$$B \leq \Sigma \rightarrow \text{yield stress} \quad \Sigma = 70 \text{ MPa for Cu}$$

$$\Rightarrow \frac{B^2}{2\mu_0} \leq \Sigma \rightarrow B \leq \sqrt{2\mu_0 \Sigma} = \sqrt{2 \times 4\pi \times 10^{-7} \times 70 \times 10^6} = 13 \text{ T}$$

$$\Rightarrow W_B = \frac{1}{2} \mu_0 B^2 = \frac{1}{2} \times 4\pi \times 10^{-7} \times 13^2 \Rightarrow W_B = \frac{1}{2} \frac{\mu_0 B^2}{\mu_0 \mu_0}$$

$$\Rightarrow W_B = \frac{1}{2} \frac{13^2}{4\pi \times 10^{-7}} = 6.7 \times 10^7 \text{ J/m}^3$$

$$= 67000 \text{ kJ/m}^3$$

$\Rightarrow$  The energy density stored in a magnetic field can be about 2 orders of magnitude higher than that storable in an electric field!!

\* Capacitive storage - requires one or more closing switches which remain open during charging and hold the charging voltage.

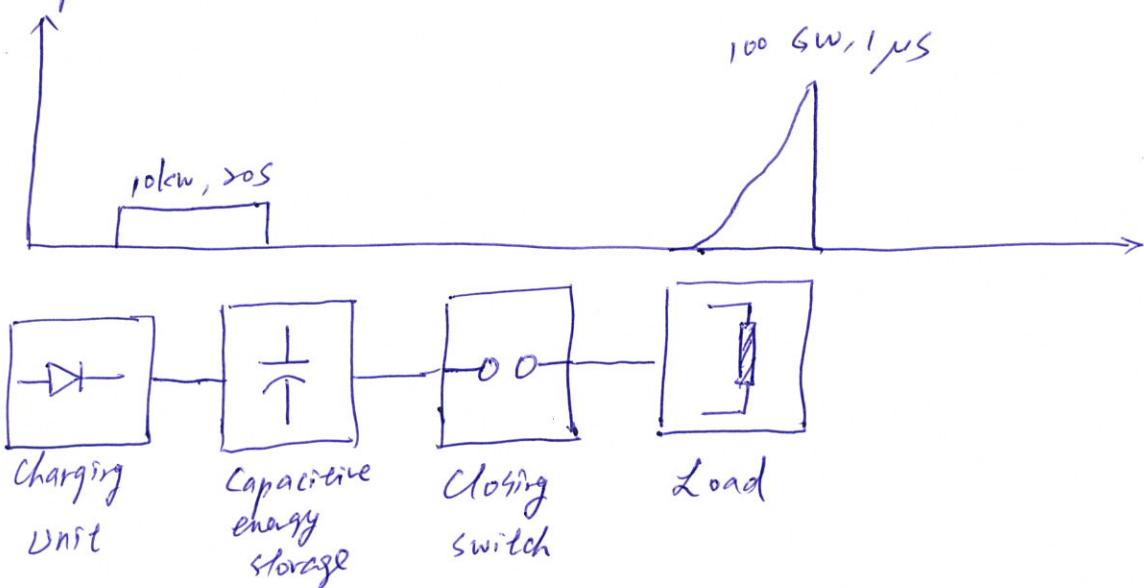
- power multiplication is done by current amplification.

\* Inductive storage - requires an opening switch which is closed during charge-up, carrying a large current at this stage.

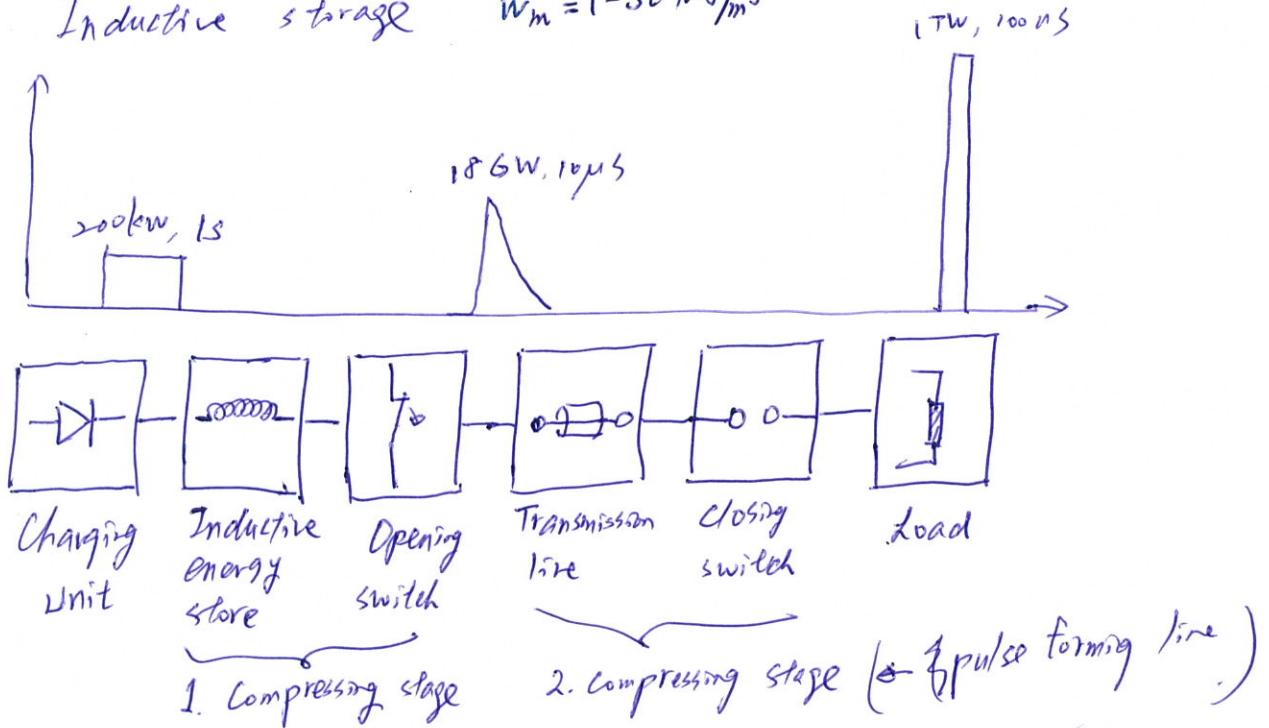
- power multiplication is done by voltage amplification.

Capacitive storage  $W_e = 10 - 80 \text{ kJ/m}^3$

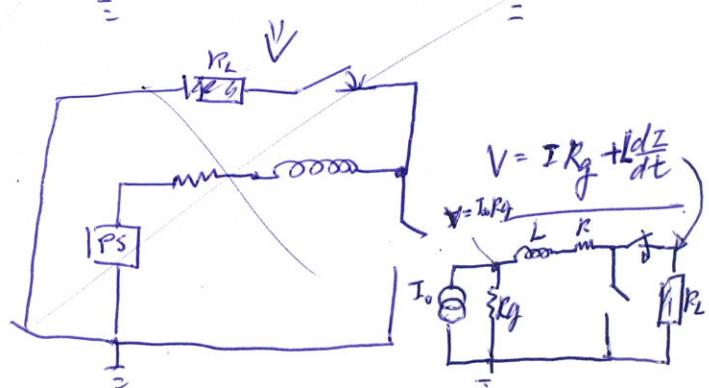
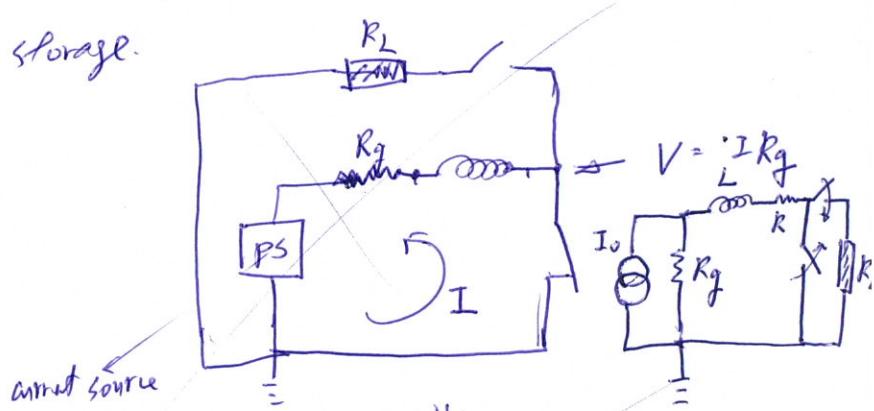
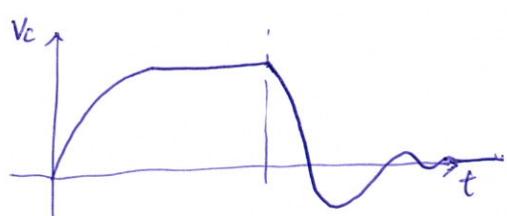
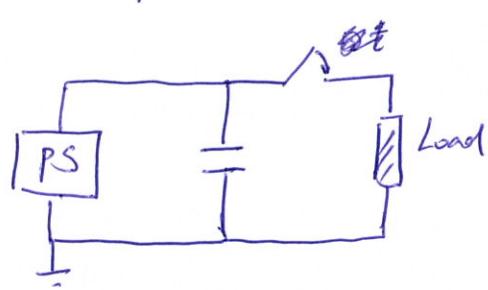
p9



Inductive storage  $W_m = 1 - 50 \text{ MJ/m}^3$



Example of Capacitive storage.



## 3) Review of circuit analysis

### \* Kirchhoff's Current Law.

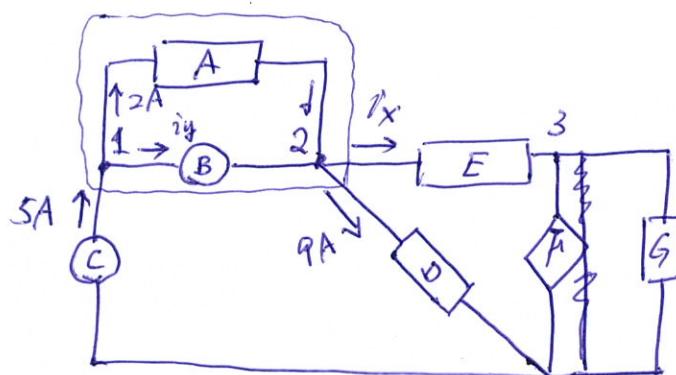
- At any instant in time, the algebraic sum of all currents leaving any closed surface is zero

$$i_1 + i_2 + \dots + i_N = 0,$$

or in abbreviated notation:

$$\sum_{k=1}^N i_k = 0$$

where  $i_k$  is the  $k^{th}$  current of the  $N$  currents leaving the closed surfaces.



$$\begin{aligned}
 i_y + 2 - 5 &= 0 \\
 \Rightarrow i_y &= 3 \text{ (A)} \\
 -5 + i_x + 9 &= 0 \\
 \Rightarrow i_x &= -4 \text{ (A)}
 \end{aligned}$$

### \* Kirchhoff's Voltage Law.

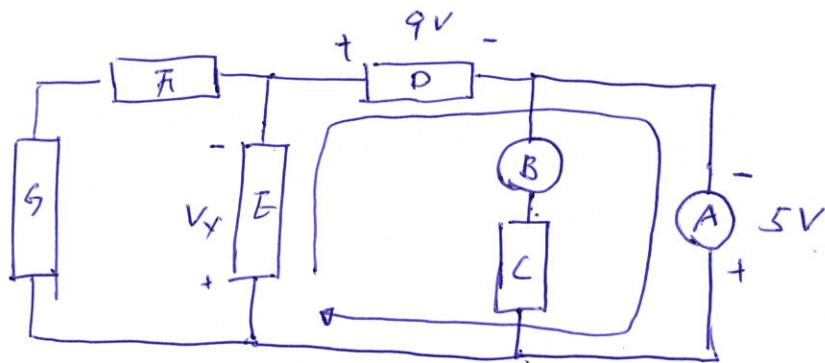
- At any instant in time, the algebraic sum of all voltage drops taken around any closed path is 0:

$$V_1 + V_2 + \dots + V_N = 0.$$

or in abbreviated notation:

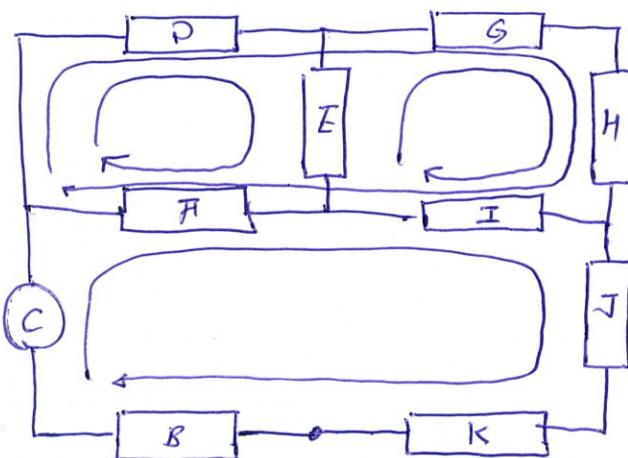
$$\sum_{k=1}^N V_k = 0$$

where  $V_k$  is the voltage drop, taken in the direction of the path along the  $k^{th}$  segment of the  $N$  segments in the closed path.

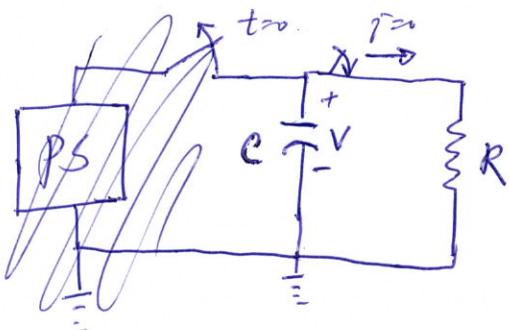


$$-V_x - 9 + 5 = 0 \Rightarrow V_x = -4 \text{ V}$$

\* Loops, Meshes, and Planar Networks



\* Source-free  $RC$  circuit.



\* Assuming  
Assuming that the capacitor is  
fully charged to  $V_0$ .  
At  $t=0$ , the switch is opened.

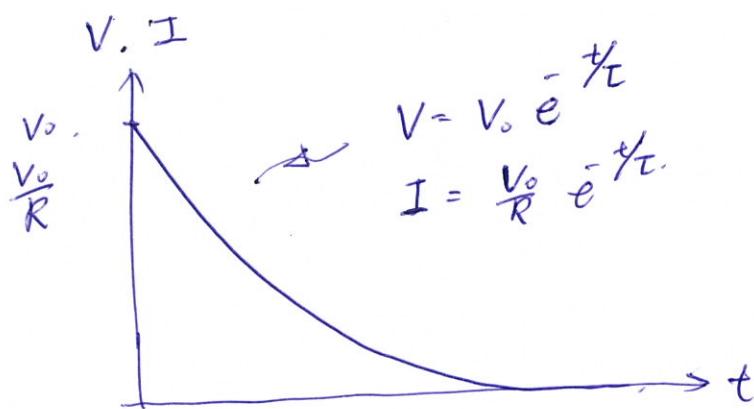
$$V_C - IR = 0 \quad I = \frac{dQ}{dt} = -C \frac{dV}{dt} \quad C = \frac{Q}{V}$$

$$\Rightarrow V_C + RC \frac{dV}{dt} = 0 \quad \text{or} \quad \frac{dV}{dt} + \frac{1}{RC} V = 0$$

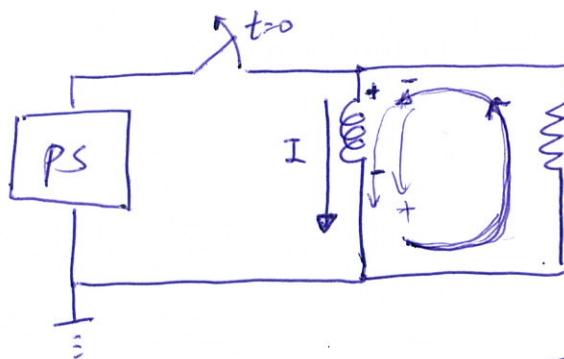
$$\Rightarrow \int \frac{dV}{V} = -\frac{1}{RC} \int dt \quad \Rightarrow \ln \frac{V(t)}{V_0} = -\frac{t}{RC}$$

$$\Rightarrow V(t) = V_0 e^{-\frac{t}{RC}}$$

$$I = -C \frac{dV}{dt} = V_0 C \left( +\frac{1}{RC} \right) e^{-\frac{t}{RC}} = \frac{V_0}{R} e^{-\frac{t}{RC}}$$



### \* Source - free $RL$ circuit



\* Assuming the current is at steady state for  $t \leq 0$ ,  $I(t) = I_0$   
At  $t \geq 0$ , the switch is open

~~$$V_L = IR + V_R \Rightarrow V_L = L \frac{dI}{dt}$$~~

$$-IR - V_L = 0 \quad V_L = L \frac{dI}{dt}$$

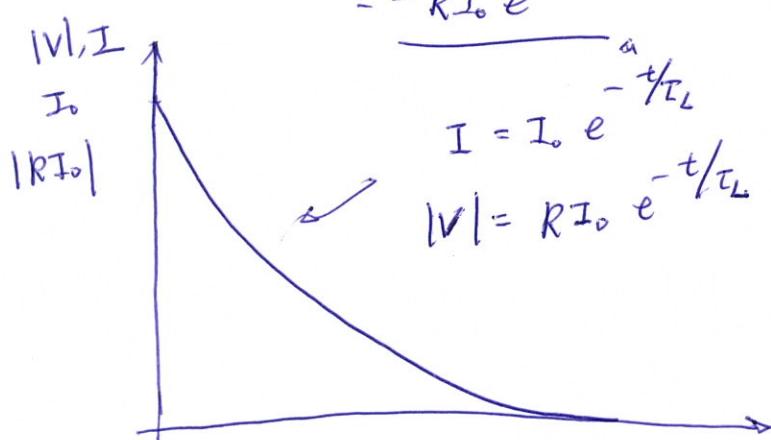
$$\Rightarrow IR + L \frac{dI}{dt} = 0 \quad \Rightarrow \frac{dI}{dt} + \frac{R}{L} I = 0$$

$$\Rightarrow \int \frac{dI}{I} = -\frac{R}{L} dt \quad \Rightarrow \ln \frac{I(t)}{I(0)} = -\frac{R}{L} t = -\frac{t}{T_L} \quad T_L = \frac{L}{R}$$

$$\Rightarrow I(t) = I_0 e^{-\frac{t}{T_L}} = I_0 e^{-\frac{t}{T_L}}$$

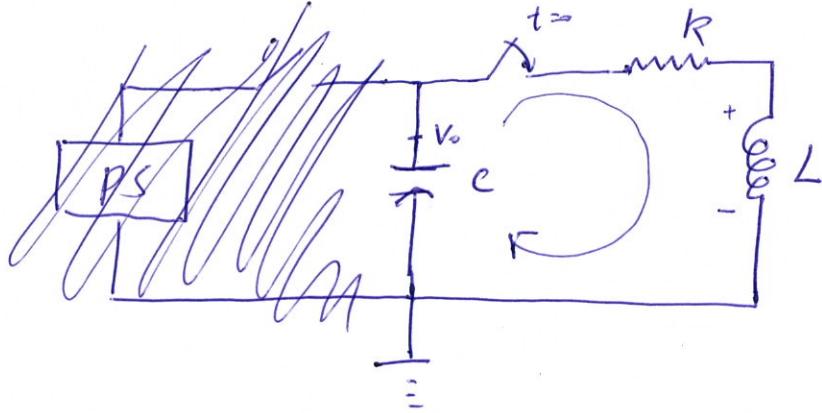
$$V(t) = L \frac{dI}{dt} = L \cdot I_0 \cdot \left(-\frac{1}{T_L}\right) e^{-\frac{t}{T_L}} = \frac{L}{T_L} I_0 e^{-\frac{t}{T_L}}$$

$$= -RI_0 e^{-\frac{t}{T_L}}$$



\* Series RLC circuit

PB



Assuming that the capacitor is fully charged to  $V_0$ ,  $I(0)=0$   
At  $t=0$ , the switch is opened,

$$V_0 - IR - L \frac{dI}{dt} = 0 \quad I = \frac{dQ}{dt} = -C \frac{dV}{dt}$$

$$\Rightarrow V + RC \frac{dV}{dt} + LC \frac{d^2V}{dt^2} = 0$$

$$\frac{d^2V}{dt^2} + \frac{R}{L} \frac{dV}{dt} + \frac{1}{LC} V = 0$$

$$D^2 + \frac{R}{2L} D + \frac{1}{LC} = 0 \quad \Rightarrow D = \frac{-\frac{R}{2} \pm \sqrt{\left(\frac{R}{2}\right)^2 - \frac{1}{LC}}}{2}$$

$$\Rightarrow V = e^{-\frac{R}{2L}t} \left( \alpha e^{\sqrt{\left(\frac{R}{2L}\right)^2 - \frac{1}{LC}}t} + \beta e^{-\sqrt{\left(\frac{R}{2L}\right)^2 - \frac{1}{LC}}t} \right)$$

$$\text{If } \left(\frac{R}{2L}\right)^2 - \frac{1}{LC} < 0 \quad \Rightarrow V = e^{-\frac{R}{2L}t} \left( \alpha e^{i\sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2}t} + \beta e^{-i\sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2}t} \right)$$

$$V(t=0) = V_0 = \alpha + \beta$$

$$\Rightarrow V = V_0 e^{-\frac{R}{2L}t} \cos \sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2 t}$$

$$V = V_0 e^{-\frac{R}{2L}t} \left[ V_0 \cos \left( \sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2} t \right) + \beta \sin \left( \sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2} t \right) \right]$$

$$I = -C \frac{dV}{dt} = -C \left\{ -\frac{R}{2L} e^{-\frac{R}{2L}t} \left[ V_0 \cos(\sqrt{\frac{R}{2L}}t) + \beta \sin(\sqrt{\frac{R}{2L}}t) \right] + \frac{R}{2L} t \left[ -\sqrt{V_0} \sin(\sqrt{\frac{R}{2L}}t) + \sqrt{\beta} \cos(\sqrt{\frac{R}{2L}}t) \right] \right\} \quad P14$$

$$I(0) = 0 \Rightarrow C \left\{ -\frac{R}{2L} \cdot V_0 + \sqrt{\beta} \right\}$$

$$\Rightarrow \beta = \frac{R}{2L} V_0 \cdot \frac{1}{\sqrt{\frac{R}{2L}}} = V_0 \frac{k/2L}{\sqrt{\chi_c - (\frac{R}{2L})^2}}$$

$$= \frac{V_0}{\sqrt{\frac{4L^2}{k^2} \cdot \frac{1}{\chi_c} - 1}} = \frac{V_0}{\sqrt{\frac{4L}{k^2 C} - 1}}$$

$$V(t) = V_0 e^{-\frac{R}{2L}t} \left[ \cos\left(\sqrt{\frac{1}{\chi_c} - \left(\frac{R}{2L}\right)^2} t\right) + \frac{k/2L}{\sqrt{\frac{1}{\chi_c} - \left(\frac{R}{2L}\right)^2}} \sin\left(\sqrt{\frac{1}{\chi_c} - \left(\frac{R}{2L}\right)^2} t\right) \right]$$

~~$$I(t) = -C \left\{ -\frac{R}{2L} e^{-\frac{R}{2L}t} \left[ V_0 \cos(\sqrt{\frac{R}{2L}}t) + \beta \sin(\sqrt{\frac{R}{2L}}t) \right] + \left( -\frac{R}{2L} t \right) \sqrt{V_0} \sin(\sqrt{\frac{R}{2L}}t) \right\}$$~~

$$I(t) = -C \left\{ -\frac{R}{2L} e^{-\frac{R}{2L}t} \left[ V_0 \cos(\sqrt{\frac{R}{2L}}t) + \frac{V_0 \cdot k/2L}{\sqrt{\chi_c - (\frac{R}{2L})^2}} \sin(\sqrt{\frac{R}{2L}}t) \right] + \frac{R}{2L} t \left[ -\sqrt{V_0} \sin(\sqrt{\frac{R}{2L}}t) + \cancel{\frac{V_0 k/2L}{R} \cos(\sqrt{\frac{R}{2L}}t)} \right] \right\}$$

$$= -C V_0 e^{-\frac{R}{2L}t} \left\{ \left( -\frac{R}{2L} V_0 + \frac{V_0 k/2L}{\sqrt{\chi_c - (\frac{R}{2L})^2}} \right) \cos(\sqrt{\frac{R}{2L}}t) - \left( \frac{(\frac{R}{2L})^2}{\sqrt{\chi_c - (\frac{R}{2L})^2}} + \sqrt{\frac{R}{2L}} \right) \sin(\sqrt{\frac{R}{2L}}t) \right\}$$

$$= +C V_0 e^{-\frac{R}{2L}t} \frac{\cancel{\frac{R}{2L} V_0} + \frac{1}{\cancel{\frac{R}{2L}}} \cancel{\frac{V_0 k/2L}{\sqrt{\chi_c - (\frac{R}{2L})^2}}}}{\sqrt{\frac{R}{2L} - \left(\frac{R}{2L}\right)^2}} \sin(\sqrt{\frac{R}{2L}}t)$$

$$= \frac{V_0}{L} \frac{1}{\sqrt{\frac{R}{2L} - \left(\frac{R}{2L}\right)^2}} e^{-\frac{R}{2L}t} \sin(\sqrt{\frac{R}{2L}}t) = \frac{V_0}{\sqrt{\frac{4L^2}{k^2} - 1}} e^{-\frac{R}{2L}t} \sin(\sqrt{\frac{1}{\chi_c} - \left(\frac{R}{2L}\right)^2} t)$$

$$\begin{aligned}
 I(t) &= -\frac{V_0}{2} C e^{-\frac{R}{2L}t} \left\{ \left(1 + \frac{\kappa_{2L}}{\sqrt{L}}\right) \left(\sqrt{-\frac{L}{2\kappa_{2L}}} - \left(1 - \frac{\kappa_{2L}}{\sqrt{L}}\right)\right) e^{\sqrt{L}t} - \left(1 - \frac{\kappa_{2L}}{\sqrt{L}}\right) \left(\sqrt{-\frac{L}{2\kappa_{2L}}} + \left(1 + \frac{\kappa_{2L}}{\sqrt{L}}\right)\right) e^{-\sqrt{L}t} \right\} \\
 &= -\frac{C V_0}{2} e^{-\frac{R}{2L}t} \left\{ \frac{(\sqrt{L})^2 - \kappa_{2L}^2}{\sqrt{L}} e^{\sqrt{L}t} - \frac{\sqrt{L}^2 - \kappa_{2L}^2}{\sqrt{L}} e^{-\sqrt{L}t} \right\} \\
 &\quad \cancel{V_0} \cancel{e^{-\frac{R}{2L}t}} \cancel{\sqrt{L}^2 - \kappa_{2L}^2} \quad \cancel{C} \cancel{e^{\sqrt{L}t}} \cancel{-} \\
 &= + \frac{C V_0}{2} e^{-\frac{R}{2L}t} \cdot \frac{+\kappa_{2L}}{\sqrt{(\kappa_{2L})^2 - \frac{1}{L}}} \left[ e^{\sqrt{(\kappa_{2L})^2 - \frac{1}{L}}t} - e^{-\sqrt{(\kappa_{2L})^2 - \frac{1}{L}}t} \right] \\
 &= V_0 e^{-\frac{R}{2L}t} \frac{1}{\sqrt{(\frac{R}{2L})^2 - \frac{1}{L}}} \left[ \frac{e^{\sqrt{(\kappa_{2L})^2 - \frac{1}{L}}t} - e^{-\sqrt{(\kappa_{2L})^2 - \frac{1}{L}}t}}{2} \right] \\
 &= \frac{V_0}{\sqrt{(\frac{R}{2L})^2 - \frac{1}{L}}} e^{-\frac{R}{2L}t} \sinh\left(\sqrt{(\frac{R}{2L})^2 - \frac{1}{L}}t\right)
 \end{aligned}$$

Plot 3 conditions !!

$$\Rightarrow \left(\frac{R}{2L}\right)^2 - \frac{1}{LC} = 0 \Rightarrow D = -\frac{R}{2L}$$

$$-\frac{R}{2L}t$$

$$V = (\alpha + \beta t) e^{-\frac{R}{2L}t}$$

$$V(0) = V_0 = \alpha \Rightarrow V = (V_0 + \beta t) e^{-\frac{R}{2L}t}$$

$$I(t) = -c \frac{dV}{dt} = -c \left[ \beta e^{-\frac{R}{2L}t} + -\frac{R}{2L} (V_0 + \beta t) e^{-\frac{R}{2L}t} \right]$$

$$I(t=0) = -c \left[ \beta - \frac{R}{2L} V_0 \right] = 0 \Rightarrow \beta = \frac{R}{2L} V_0$$

$$\Rightarrow V = \left( V_0 + \frac{R}{2L} V_0 t \right) e^{-\frac{R}{2L}t} = V_0 \left( 1 + \frac{R}{2L} t \right) e^{-\frac{R}{2L}t}$$

$$I = -c \frac{dV}{dt} = -c \left[ \frac{R}{2L} V_0 e^{-\frac{R}{2L}t} - \cancel{\frac{R}{2L} V_0 e^{-\frac{R}{2L}t}} - \frac{R}{2L} \cdot \frac{R}{2L} V_0 t e^{-\frac{R}{2L}t} \right]$$

$$= c \cdot \left(\frac{R}{2L}\right)^2 V_0 t e^{-\frac{R}{2L}t} = \cancel{c} \cdot \frac{1}{4} V_0 t e^{-\frac{R}{2L}t}$$

$$= \frac{V_0}{L} \cdot t \cdot e^{-\frac{R}{2L}t}$$

→  $v_I$

$$3) \quad \left(\frac{R}{2L}\right)^2 - \frac{1}{LC} > 0$$

$$V = e^{-\frac{R}{2L}t} \left( \alpha e^{\sqrt{\left(\frac{R}{2L}\right)^2 - \frac{1}{LC}}t} + \beta e^{-\sqrt{\left(\frac{R}{2L}\right)^2 - \frac{1}{LC}}t} \right)$$

~~$\alpha e^{\frac{R}{2L}t} + \beta \sinh(\sqrt{\frac{R}{2L}}t) + \beta \cos(\sqrt{\frac{R}{2L}}t)$~~

$$V(t=0) = V_0 = \alpha + \beta$$

$$I = -c \frac{dV}{dt} = -c \left\{ -\frac{R}{2L} e^{-\frac{R}{2L}t} \left[ \alpha e^{\sqrt{t}} + \beta e^{-\sqrt{t}} \right] + \right.$$

$$\left. -\frac{R}{2L} e^{-\frac{R}{2L}t} \left[ \alpha \sqrt{t} e^{\sqrt{t}} - \beta \sqrt{t} e^{-\sqrt{t}} \right] \right\}$$

~~Drc~~

$$I(t=0) = 0 \Rightarrow \left\{ -\frac{R}{2L} [\alpha + \beta] + (\alpha\sqrt{-} - \beta\sqrt{-}) \right\} = 0 \quad P16$$

$$\Rightarrow \left( \sqrt{-} - \frac{R}{2L} \right) \alpha - \left( \sqrt{-} + \frac{R}{2L} \right) \beta = 0$$

$$\Rightarrow \begin{cases} \alpha + \beta = V_0 \\ \left( \sqrt{-} - \frac{R}{2L} \right) \alpha - \left( \sqrt{-} + \frac{R}{2L} \right) \beta = 0 \end{cases} \Rightarrow \alpha = \frac{\sqrt{-} + \frac{R}{2L}}{\sqrt{-} - \frac{R}{2L}} \beta$$

$$\beta \left[ 1 + \underbrace{\frac{\sqrt{-} + \frac{R}{2L}}{\sqrt{-} - \frac{R}{2L}}}_{\alpha} \right] = V_0 \Rightarrow \beta = \frac{V_0}{2} \frac{\sqrt{-} - \frac{R}{2L}}{\sqrt{-}}$$

$$\frac{\sqrt{-} - \cancel{\frac{R}{2L}} + \sqrt{-} + \cancel{\frac{R}{2L}}}{\sqrt{-} - \frac{R}{2L}} = \frac{2\sqrt{-}}{\sqrt{-} - \frac{R}{2L}} = \frac{V_0}{2} \left( 1 - \frac{\frac{R}{2L}}{\sqrt{-}} \right)$$

$$\alpha = \frac{\sqrt{-} + \frac{R}{2L}}{\cancel{\sqrt{-} - \frac{R}{2L}}} \cdot \frac{V_0}{2} \frac{\cancel{\sqrt{-} - \frac{R}{2L}}}{\sqrt{-}} = \frac{V_0}{2} \frac{\sqrt{-} + \frac{R}{2L}}{\sqrt{-}} = \frac{V_0}{2} \left( 1 + \frac{\frac{R}{2L}}{\sqrt{1 - \frac{4L}{R^2}}} \right)$$

$$= \frac{V_0}{2} \left( 1 + \frac{1}{\sqrt{1 - \frac{4L}{R^2}}} \right)$$

$$\Rightarrow V(t) = e^{-\frac{R}{2L}t} \cdot \frac{V_0}{2} \left[ \left( 1 + \frac{1}{\sqrt{1 - \frac{4L}{R^2}}} \right) e^{+\sqrt{\frac{(R/2L)^2 - V_0^2}{R^2}}} t + \left( 1 - \frac{1}{\sqrt{1 - \frac{4L}{R^2}}} \right) e^{-\sqrt{\frac{(R/2L)^2 - V_0^2}{R^2}}} t \right]$$

$$I(t) = -C e^{-\frac{R}{2L}t} \left\{ -\frac{R}{2L} [\alpha e^{\sqrt{-}t} + \beta e^{-\sqrt{-}t}] + \alpha \sqrt{-} e^{\sqrt{-}t} - \beta \sqrt{-} e^{-\sqrt{-}t} \right\}$$

$$= -C e^{-\frac{R}{2L}t} \left\{ \alpha \left( \sqrt{-} - \frac{R}{2L} \right) e^{\sqrt{-}t} - \beta \left( \sqrt{-} + \frac{R}{2L} \right) e^{-\sqrt{-}t} \right\}$$

## 72 Static and Dynamic Breakdown Strength of Dielectric Materials

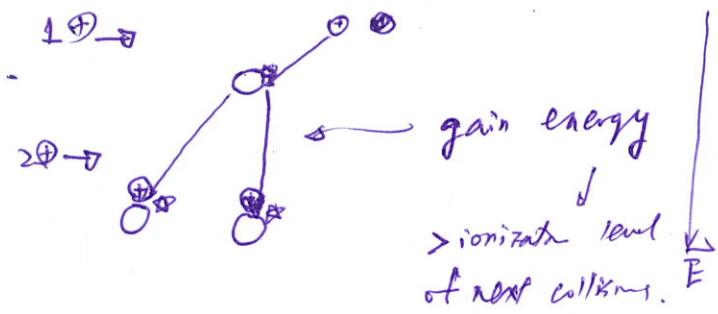
P18

### 72.1 Introduction

- \* We will ~~speak~~ talk about the gas, liquid, and solid dielectrics.
- \* Dielectric substances serve both as "insulators" in generator components such as capacitors, HV transmission lines, & transformers, and as "working media" in switches.
- \* The properties of these devices are strongly depend on electric breakdown strength.
  - [ dielectric constant.]
- \* The dielectric strength of an insulant can be defined as "the maximum field stress that the material can ~~with~~ withstand for a given time".

D  
ΔV/P

- \* Integrated field-time action:  
failure probability:  $\ln [1 - F(E, t)] = -\alpha \int_0^t E^b t^a dt$   
 $F(E, t)$ : probability of ~~not~~ failure after time  $t$ .  
 $a, b \rightarrow$  determined experimentally.
- \* Electric strength ~~also~~ depends on the sample "geometry", "pressure", "temperature", and the "electrode material".
- \* At the microscopic level, breakdown requires the presence of sufficiently energetic charge particles that have acquired enough energy from the applied electric field between two energy-dissipating collisions to ionise the material and to create more charge particles.

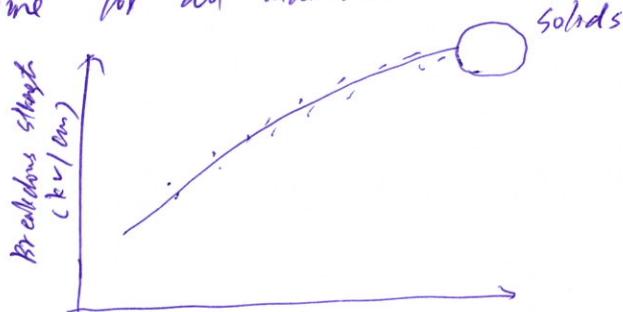


- \* In most cases, electrons dominate the breakdown process since the mobility is much larger than that of ions.
- $$E_k = \frac{1}{2} m V^2 \Rightarrow V = \sqrt{\frac{2 E_k}{m}} \Rightarrow S = Vt \Rightarrow t = \frac{S}{V}$$

$$\Rightarrow t = \frac{S}{\sqrt{2 E_k / m}} \sim \frac{n^{-1/3}}{\sqrt{2 E_k}} \sqrt{m}$$

$$n = \frac{N}{V} \sim \frac{1}{S^3} \Rightarrow S \sim n^{-1/3}$$

~~With  $t \propto S^{1/3}$~~
- \* In order for an electron to acquire enough energy between collisions, its mean free path in the material must be sufficient large.
- \* Mean free path depends essentially on the density of the material, the electric breakdown strength should be the same for all materials with the same density.



- \* Gaseous or liquid dielectric - self-repairing after a breakdown.
- Solid dielectric - remains irreversibly destroyed.
- Liquid dielectric - preferred if large heat losses have to be removed.

~~by gas~~

P>0

## 7.2.2 Bases

## 37.2.1 Static Breakdown

- \* The electric strength of a gas is determined by the magnitude of its atomic and molecular reaction cross-sections for electron collisions.  $\Rightarrow$  ionisation and attachment cross-sections.

$\sigma$ : cross section of each atom.

$n$ : # atom per unit volume have not collided on anything

A diagram of a rectangular element of area  $A$  and width  $dx$ . The top surface is divided into three regions labeled  $\sigma$ ,  $\sigma$ , and  $\sigma$ . A vertical force vector labeled  $N$  acts on the left side. A small differential force vector labeled  $\Delta N$  acts at the top center. A label  $N' = N + \Delta N < N$  is shown below the rectangle. To the right, the equation  $\# = n \cdot A \cdot dx$  is written above the text "total cross sect:" followed by  $\sigma_{\text{tot}} = \sigma \cdot n \cdot A \cdot dx$ . Below the rectangle, a circled  $dN < 0$  is shown.

probability of a particle carrying an interaction in this layer:

$$P = \frac{\text{Gnd}}{N \sum A dx} = \frac{\sigma n A dx}{A} = \sigma n dx \equiv \sum dx$$

$$\cancel{dN = N \cdot \nabla P} = -\sum N d\chi \Rightarrow \frac{dN}{N} = -\sum d\chi$$

$$\Delta N \Rightarrow -\Delta N = N \sum \delta x$$

$$\frac{\delta N}{N} = -\sum \delta x$$

$$N(x) = N_0 e^{-\sum \delta x}$$

Mean free path - average length of a particle's path

$$\frac{\int x dN'}{\int dN'} = \frac{1}{N_0} \int x \cdot \sum N(x) dx$$

2022.8.28

$$dN' = -dN = \sum N dx$$

$$= \sum_{k=1}^{\infty} \int_0^{\infty} x^k \frac{e^{-x}}{k!} dx \quad u = x \quad dv$$

$$= \sum_{k=2}^{\infty} \int_0^{\infty} x^k \frac{e^{-\lambda x}}{\lambda} dx + \frac{1}{\lambda} \int_0^{\infty} e^{-\lambda x} dx$$

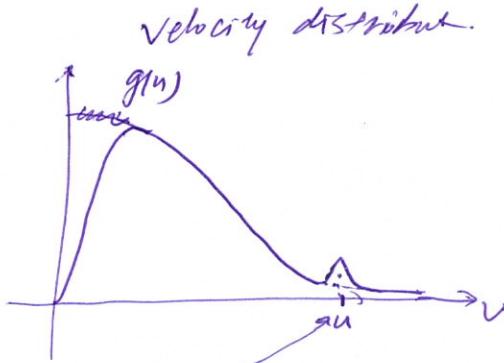
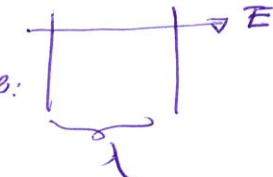
$$= \sum \left[ -\frac{1}{2} x e^{-\Sigma x} \right]_0^\infty + \frac{1}{2} \int e^{-\Sigma x} dx$$

$$= \sum \left[ -\bar{\sum}^{x_0} \right]_0 + \bar{\sum} \int^x dx$$

Between each collision,  
the kinetic energy increases.

$$\lambda \cdot eE = \frac{1}{2} m u^2$$

$$\Rightarrow u = \sqrt{\frac{2eE\lambda}{m}}$$



- Mean time between ionising collisions for electron with velocity  $u$

$$\tau_i = \frac{\lambda}{u} \rightarrow \text{the rate of ionisation is:}$$

$$\frac{1}{\tau_i} = \frac{u}{\lambda} = (\sum_i u)$$

to P21a

(showing different cross section - # of ionising collisions per second leading to growth of the swarm

$$\frac{dN_e}{dt} = \frac{N_e}{\tau} \sum_i u$$

$$\langle \frac{dN_e}{dt} \rangle = \int_0^\infty \frac{N_e \cdot g(u) du}{\tau} = N_e \int_0^\infty (\sum_i u) g(u) du$$

skip

$$\frac{dN_e}{dt} = \frac{S/N}{\tau} \sum_i u \frac{\partial N}{\partial t} + \frac{\partial X}{\partial t} \frac{\partial N}{\partial X} = \frac{\partial N}{\partial t} + u \frac{\partial N}{\partial X}$$

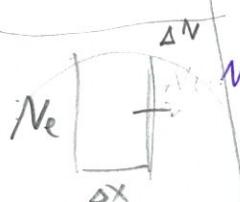
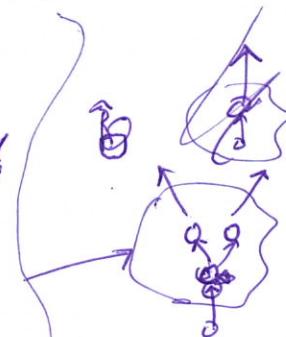
stop all

Assume that the swarm does not spread

$$\text{f.e. } \frac{\partial N}{\partial t} = 0 \rightarrow N(x,t) = N(x)$$

and introduce a mean swarm velocity  $\langle u \rangle$

$$\Rightarrow \frac{dN_e}{dt} = \frac{\partial N}{\partial t} + \langle u \rangle \frac{\partial N}{\partial X} \rightarrow \langle u \rangle \frac{\partial N}{\partial X} = N \int \sum_i u g(u) du$$



$$\Delta N = N_e \cdot \alpha \cdot \Delta X$$

$$\frac{\Delta N}{N_e} = \alpha \Delta X$$

$$\ln \frac{N_e}{N_0} = \alpha X$$

the gas  
of the

Mean swarm velocity  $\langle u \rangle$ : ~~assume  $\frac{\partial N}{\partial X} = N_e \alpha$~~

$$\alpha: \text{ionisation coefficient, } \alpha = \frac{\int \sum_i u \cdot g(u) du}{\int \sum_i (u)^2 \cdot g(u) du}$$

$$\Rightarrow N_e \langle u \rangle = N_0 \exp(\alpha X)$$

$$\# \text{ of ionisation events performed by an electron in a unit length}$$

Notice that  $\frac{d}{P}$  is a unique function of  $E/P$ , where  $P$  is the gas pressure under normal conditions.

$$\frac{\alpha}{P} = F\left(\frac{E}{P}\right)$$

\* some back after page

$\propto$  cross section  $\rightarrow$  collisional cross section:

P21a

- elastic collisions - NO energy exchanges  
Momentum is redistributed.
- inelastic collisions - energy exchanged between  
the collision partners  
 $\rightarrow$  production of molecules &  
particles

$\rightarrow$  Elastic collisions:



$\rightarrow$  Inelastic collisions: a portion of the kinetic energy before collision is converted to potential energy of one of the particles in the system.

• Ionization:  $A + B \rightarrow A + B^+ + e^-$

The process of ionization is dominated by  $e^-$  acceleration in an electric field and is greatly aided by the appearance of ionizing electrons.

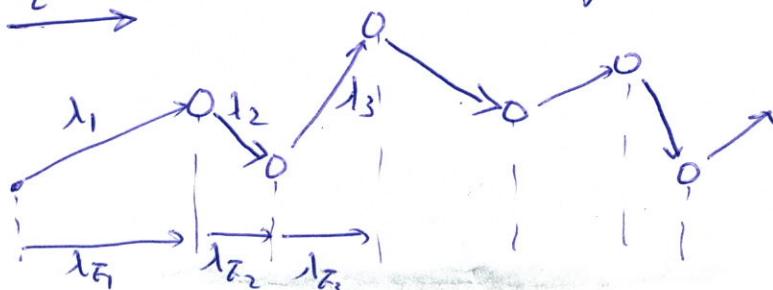
electrons { ionization in the gas.  
emission from the cathode.

$e^-$  impart ionization.  $A + e^- \rightarrow A^+ + e^- + e^-$   $\leftarrow$  dominated.

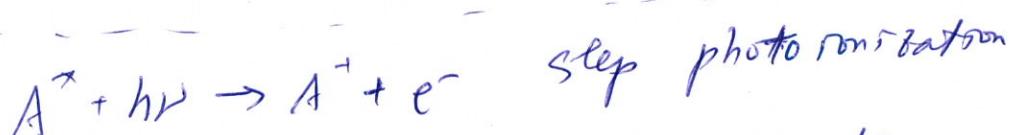
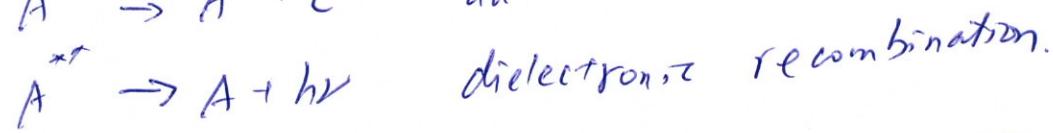
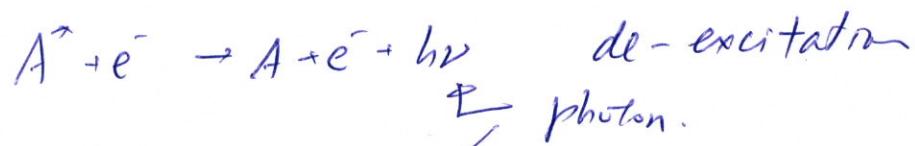
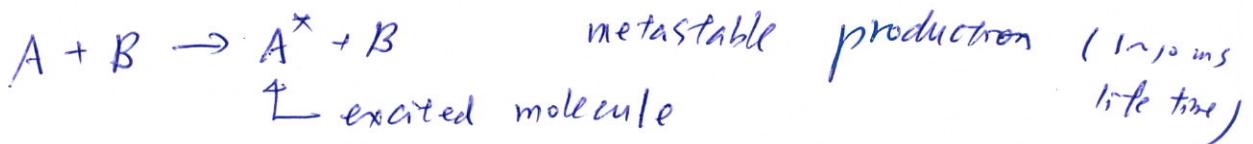
The most important process in the breakdown of gases but is not sufficient alone to result in breakdown.

$$g_e \cdot E \cdot \lambda_{EI} \geq g_e V_i \quad \leftarrow \text{requirement}$$

$\overline{E}$   $\rightarrow$  ionization potential



- Photoionization & collisions w/ excited molecules p21 b



photoionization is very complex:  
 $h\nu$  w/  $\lambda = 125 \text{ nm (UV)}$   $\Rightarrow 9.9 \text{ eV}$  can ionize

almost all gases despite that almost all molecules &  
 atom have ionization energy  $> 9.9 \text{ eV}$ . !!

- dust or water vapor  $\rightarrow$  emit  $e^-$  through ~~absorber~~

- All photoionization occurs between  $6 \sim 50 \text{ eV}$

→ Penning ionization:



- May be from impurities or engineered mixture →  
Penning mixture

A penning mixture is a mixture of an inert gas w/ a  
small amount of a quench gas.

↑  
lower ionization potential than the 1<sup>st</sup>  
excited state of the inert gas.

Ex: Neon lamp: Ne + <2% Ar

plasm display: He/Ne + Xe.

Gas ionization detector: Ar/Xe, Ne/Ar, Ar/acetylene

→ More complex collisions:



3-body collision.



on impact excitation



on impact ionization.



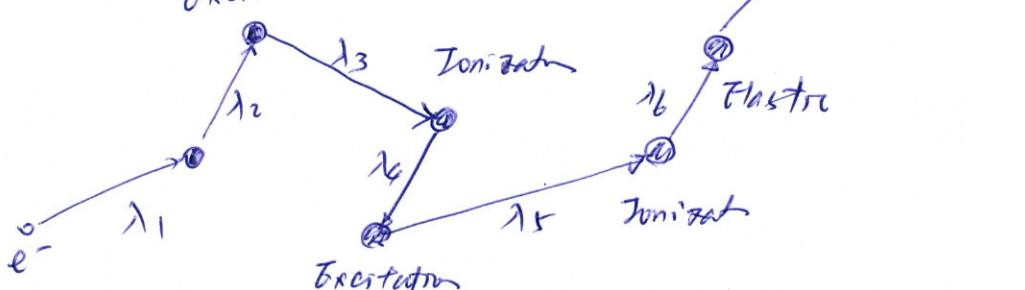
Total collisional cross section:

$$\left( \sigma(v) = \sigma_{el} + \sigma_{ex} + \sigma_{ion} \right)$$

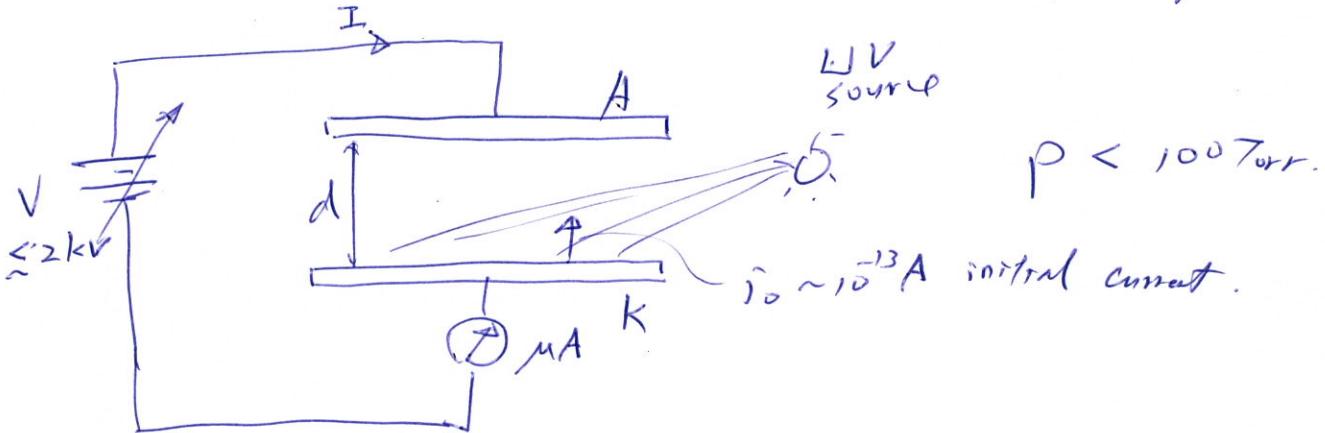
↑  
electro impact      ↑  
excitation      ↑  
sep. ionizatn.  
dominated.)

$$\sigma(v) = \sum \sigma_i$$

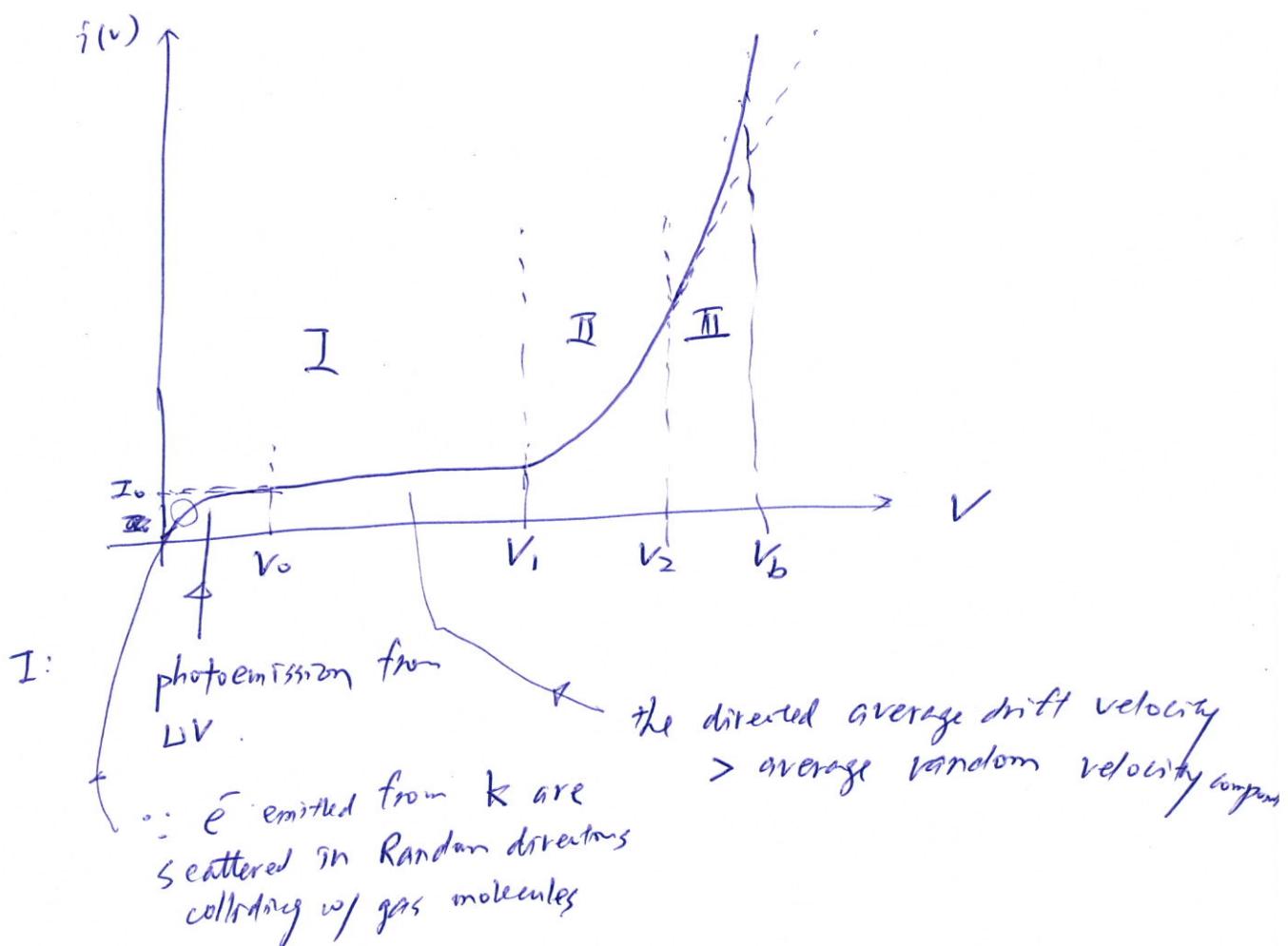
Excitation



\* Electric breakdown - Townsend's experiments



$V \neq \cancel{0} \Rightarrow I(V) \neq 0$  till spark was produced.



II: The Townsend 1<sup>st</sup> ionization region

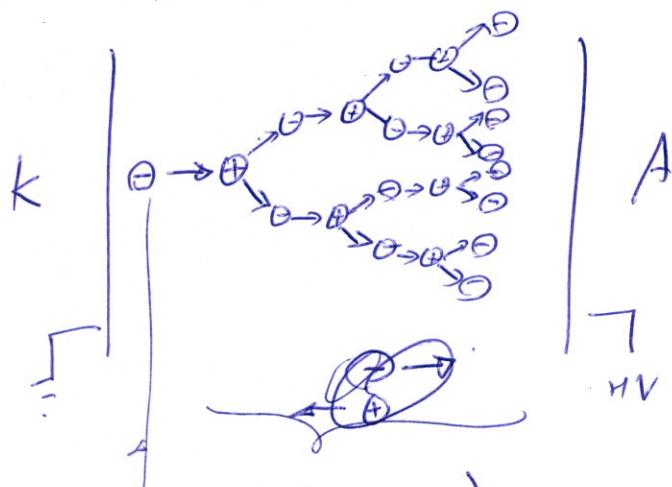
$$\textcircled{O} \cdot I(d) \cancel{\propto} = I_0 e^{\frac{d}{l}}$$

III: The Townsend 2<sup>nd</sup> ionization region

- Single-electron avalanche is not sufficient to carry the circuit-limited current
- Successor avalanches are formed by positive ions, resulting from ionization collisions w/ primary  $e^-$ , bombarding ~~w/~~ K, and liberating  $e^-$

## \* Electron Avalanche.

p21 e



present naturally.

or photon

or cosmic rays

static charge

cascade ionization

$$\left( I = \beta_e \cdot n \cdot V_d \right)$$

$\uparrow$   
e<sup>-</sup> drift velocity

go back to  
p21. w/ ~~☆~~

$$dn = n(x) \cdot \alpha \cdot dx$$

$\underbrace{\qquad\qquad\qquad}_{\text{ionizat. coefficient}}$

$$\Rightarrow \frac{dn}{n} = \alpha / dx \Rightarrow n(x) = n_0 e^{\alpha x}$$

electron drift toward anode

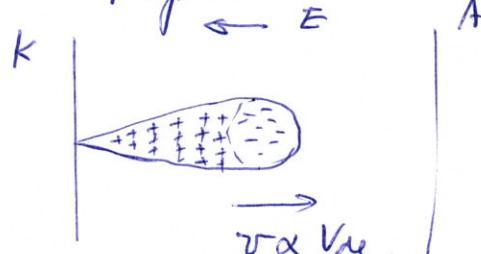
$V_{de} \sim 10^7 \text{ cm/sec}$

$V_{di} \sim 10^5 \text{ cm/sec}$

non

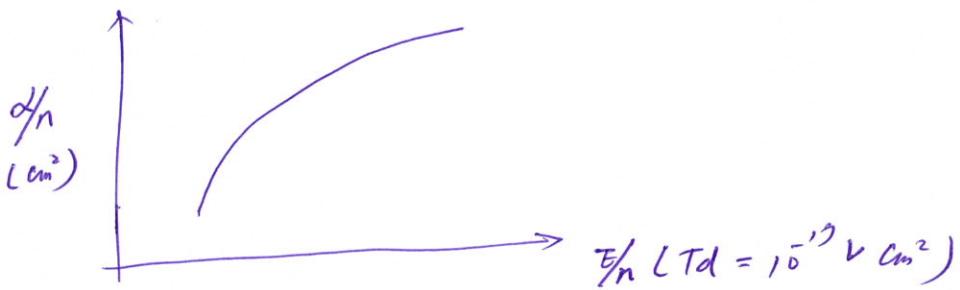
$\Rightarrow$  separation of charges.

Additionally, e<sup>-</sup> in the avalanche repulsion of like charges. head diffuse:

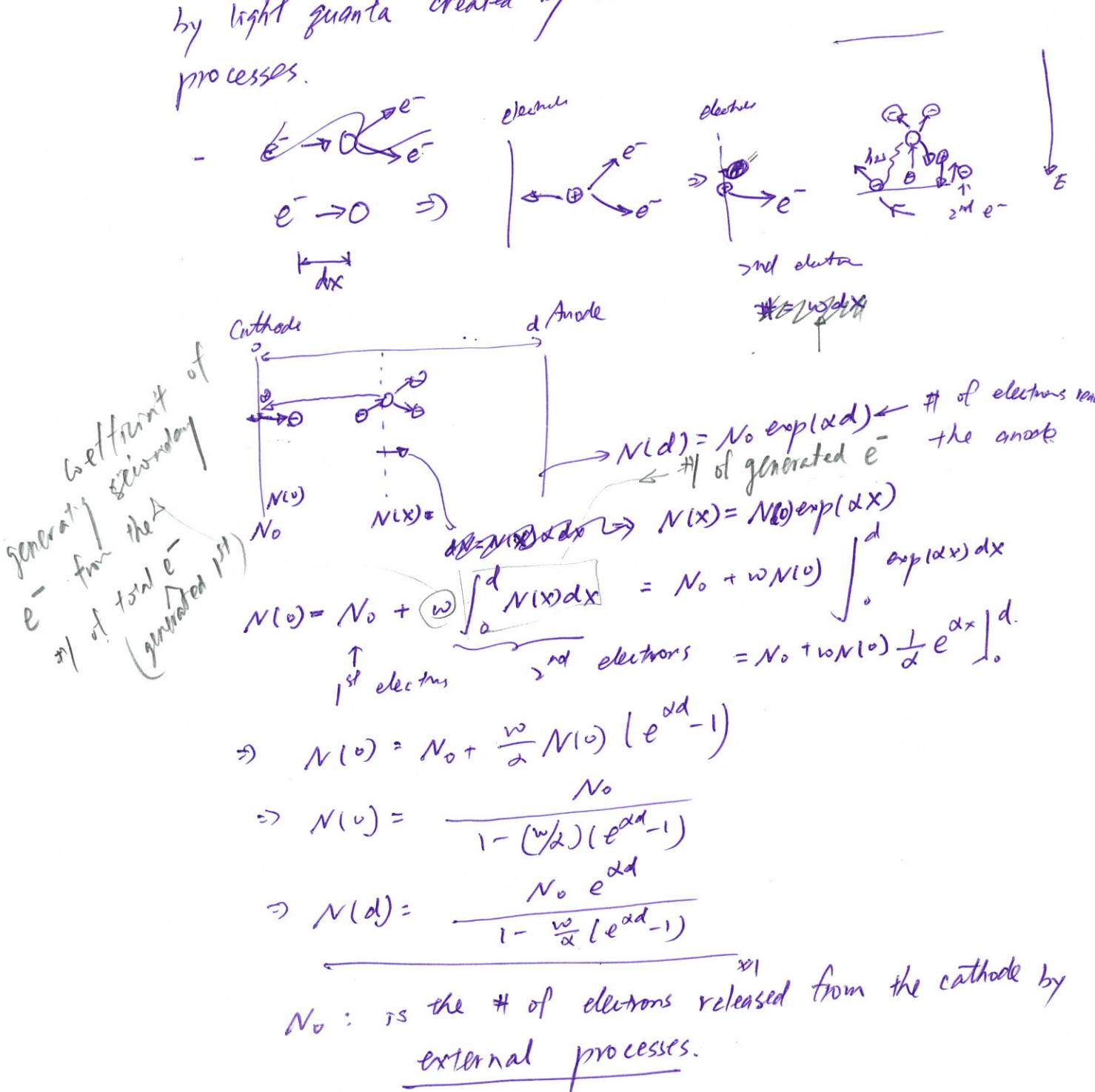


ipme  
charge  
effekt

$\Rightarrow \frac{d\phi}{dx}$  or  $\frac{d\phi}{dn}$  can be determined experimentally.



- Secondary electrons - electrons released from the cathode by ions that have drifted to the electrode, as well as by light quanta created by recombination and de-excitation processes.



\* Avalanche grows oceans when the denominator equals to 0 103

$$1 - \frac{\omega}{\alpha} (e^{\alpha d} - 1) = 0 \quad \text{or} \quad \frac{\omega}{\alpha} (e^{\alpha d} - 1) = 1$$

This is called the "Townsend condition" for ignition.

→ In this case, the insulation of the cathode-anode gap breaks down and a self-sustained discharge is created.

To P<sup>239</sup>

\* Experiments show that  $\frac{\omega}{P}$  is also a function of  $E/P$

$$\text{i.e. } \frac{\omega}{P} = f(E/P), \quad \frac{\omega}{P} = F(E/P)$$

$$\Rightarrow \frac{\omega}{\alpha} (e^{\alpha d} - 1) = 1 \Rightarrow \frac{\omega/P}{\alpha/P} (e^{E/P \cdot pd} - 1) = 1$$

$$\Rightarrow \frac{f(E/P)}{F(E/P)} (e^{F(E/P) \cdot pd} - 1) = 1$$

~~∴ pd can be determined if  $f(E/P)$  &  $F(E/P)$  are known~~

$$\therefore E = \frac{U}{d}, \quad \text{i.e. } \frac{E}{P} = \frac{U}{pd}$$

∴  $U$  can be solved for a given  $pd$  if

$f(E/P)$  &  $F(E/P)$ , i.e.,  $f(Pd)$  &  $F(U/d)$ , are known.

$$\Rightarrow U_b = \Pi(pd)$$

Paschen Law: The breakdown voltage  $U_b$  of a uniform-field gap is a unique function  $\Pi$  of  $pd$ .

\* In certain region

$$\cancel{f(Pd) \propto A e^{-B \frac{E}{P}}} \quad \frac{\omega}{P} = A e^{-\frac{B P/E}{pd}}$$

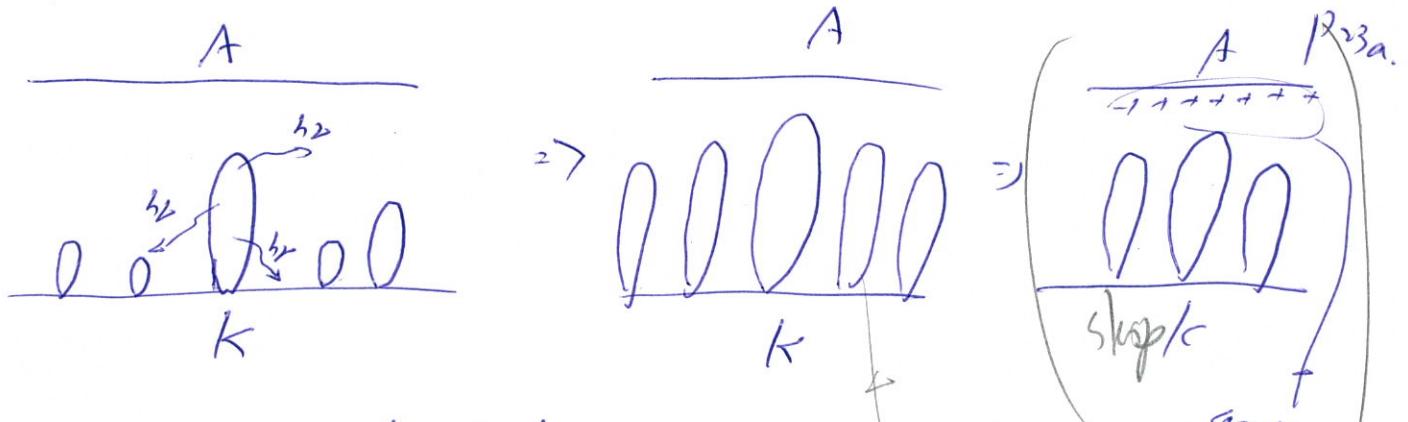
$A$  &  $B$  are constants for a given gas.

At  $\gamma = \frac{\omega}{\alpha} = \frac{f(E/P)}{F(E/P)} = Y(E/P)$ , which is a slowly varying function of  $E/P$  over a wide range.

$$\Rightarrow \gamma (e^{\alpha d} - 1) = 1 \Rightarrow \gamma (e^{-\frac{\alpha \cdot pd}{B \cdot pd}} - 1) = 1 \Rightarrow e^{-\frac{\alpha \cdot pd}{B \cdot pd}} = \gamma = \ln(1 + \frac{1}{\gamma})$$

$$\frac{\alpha}{P} \cdot pd = \ln(1 + \frac{1}{\gamma}) \Rightarrow A e^{-\frac{\ln(1 + \frac{1}{\gamma})}{pd}} = \frac{1}{pd} \Rightarrow e^{B \cdot pd / \gamma} = \frac{A \cdot pd}{\ln(1 + \frac{1}{\gamma})}$$

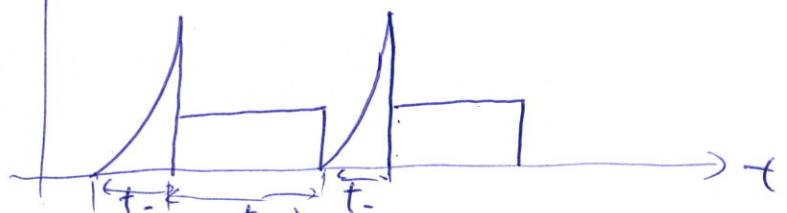
$$\Rightarrow \frac{B \cdot pd}{U} = \ln \left[ \frac{A \cdot pd}{\ln(1 + \frac{1}{\gamma})} \right] \Rightarrow U_b = \frac{B \cdot pd}{\ln \left[ \frac{A \cdot pd}{\ln(1 + \frac{1}{\gamma})} \right]}$$



\* Multiple 2<sup>nd</sup> Mechanisms

$i(t)$

untill the  
ionized  $\beta$  is emitted  
by the  $p$  system

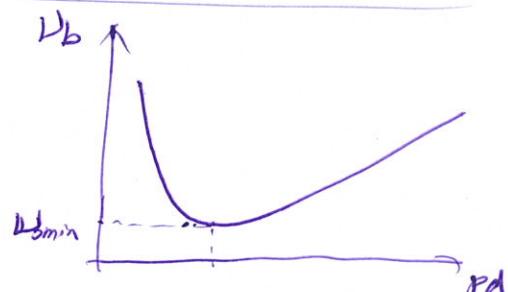


from photon      from ion bombardment.  
 slow  $\therefore$  ion drift velocity  $\beta$  slow.  
 from photon  $\sim 10^{10} \text{ cm/s}$        $\sim 10^5 \text{ cm/s}$

\* 2<sup>nd</sup> electron generation are strongly dependent  
on the cathode material.

back to p<sup>23</sup>

Gas	A (1/mm bar)	B (kV/mm bar)	Range of $E_p$ for validity (kV/(mm bar))
Air	1130	27.4	11-45
$N_2$	977	25.5	8-45
$H_2$	376	9.8	11-30
He	>10	2.6	2-11
Ar	1020	13.5	8-45
$CO_2$	1500	34.9	37-75

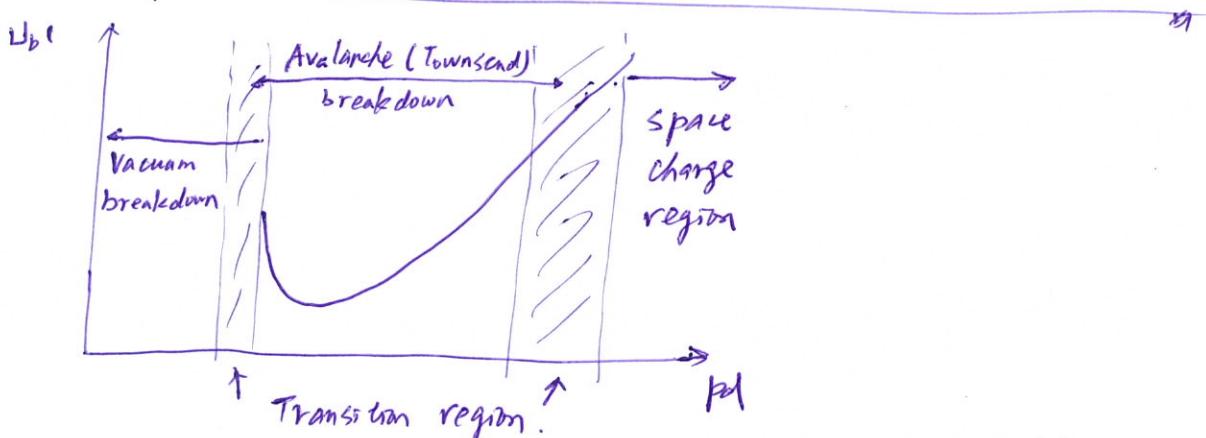
$$U_b = \frac{B \cdot pd}{\ln [A \cdot pd / \underbrace{\ln(1 + \gamma_c)}_{\approx C}]} \quad * \quad U_b = \frac{B \cdot X}{\ln [A \cdot X / C]} \quad X \equiv pd$$


$$\frac{dU_b}{dX} = \frac{B \cdot \ln [A \cdot X / C] - BX \cdot \frac{1}{A \cdot X}}{\ln^2 [A \cdot X / C]} = \frac{B [\ln (A \cdot X / C) - 1]}{[\ln (A \cdot X / C)]^2} = 0$$

$$\Rightarrow \ln (A \cdot X / C) - 1 = 0 \Rightarrow X = e \cdot \frac{C}{A}$$

$$U_b = \frac{B \cdot X}{\ln [e \cdot \frac{C}{A} \cdot \frac{X}{C}]} = \frac{B \cdot X}{\ln e} = B \cdot X = e \cdot C \cdot \frac{B}{A}$$

$$\Rightarrow U_{b \min} = e \cdot \ln [1 + \frac{1}{\gamma_c}] \cdot \frac{B}{A} \quad \textcircled{D} \quad pd_{b \min} = e \frac{\ln (1 + \frac{1}{\gamma_c})}{A}$$



\* With a voltage lower than  $U_{b \min}$ , it is impossible to cause the breakdown of a gap with a uniform field distribution.

\* At <sup>very</sup> high field strengths, field emission of electrons from the electrodes occurs. (far left & far right of Paschen curve)

\* The most commonly used high-strength gas is SF<sub>6</sub>. P25

SF<sub>6</sub> belongs to a group of "electronegative gases", which are characterised by the ability to attach electrons to the molecule, which then becomes a "negative ion".

$\Rightarrow$  attachment coefficient:  $\gamma$  - attachment coefficient probability of an electron per unit path length.

\* other electronegative: compounds containing Halogens (Cl, F, I, ... & O<sub>2</sub>)

Effective ionisation coefficient:  $\alpha_e = \alpha - \gamma = P f\left(\frac{E}{P}\right)$

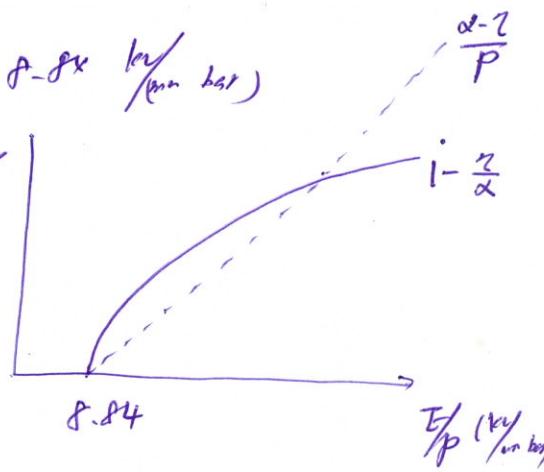
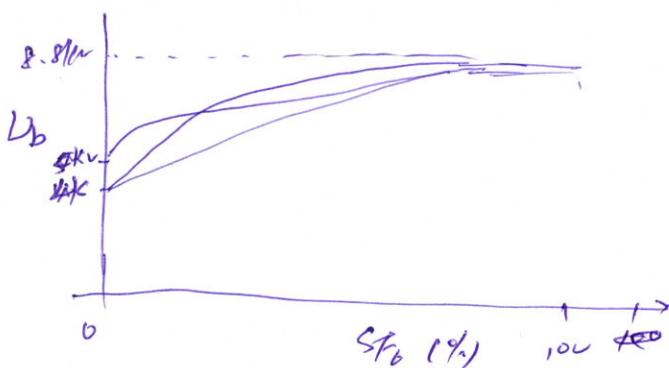
$\Rightarrow$  Electron avalanche formation becomes possible only if  $\alpha_e > 0$ .  $\text{Sx: } \frac{E}{P} > 8.84 \text{ kV/mm bar}$  is needed for SF<sub>6</sub>

$$\frac{\alpha - \gamma}{P} = k \left[ \frac{E}{P} - \left( \frac{E}{P} \right)_0 \right]$$

for SF<sub>6</sub>:  $k = 27.2 \text{ kV} \cdot \left( \frac{E}{P} \right)_0 = 8.84 \text{ kV/mm bar}$

20.  $L_b = Pd \cdot 8.84 \left[ \text{kV/mm bar} \right]^{10-5 \text{ kV}}$   
derivate see next page.

\* SF<sub>6</sub> maintains a high electric strength even if it is diluted with another gas.



\* Vapours of higher strength than SF<sub>6</sub> are known, but most of them liquefy at atmospheric pressure and room temperature.

$$\text{eq 2.8: } \gamma(e^{\alpha d} - 1) = 1 \Rightarrow \alpha d = \ln(1 + \frac{1}{\gamma})$$

$$\text{Eq 2.15: } \frac{\alpha_e}{P} = \frac{\alpha-1}{P} = K \left[ \frac{E}{P} - \left(\frac{E}{P}\right)_0 \right] = K \left[ \frac{U}{pd} - \left(\frac{E}{P}\right)_0 \right]$$

$$\Rightarrow \alpha_e d = \frac{\alpha_e}{P} \cdot pd = pd \cdot K \left[ \frac{U}{pd} - \left(\frac{E}{P}\right)_0 \right] = \ln(1 + \frac{1}{\gamma})$$

$$\Rightarrow U_b = pd \left(\frac{E}{P}\right)_0 + \frac{1}{K} \ln(1 + \frac{1}{\gamma})$$

$$= pd \cdot 8.84 (\text{kv/mm bar}) + 0.5 \text{ kv} \text{ for SF}_6$$

\* Quadratic ansatz  $\rightarrow$  for gases are not electronegative or are only weakly so:

$$\frac{\alpha_e}{P} \sim \left[ \frac{E}{P} - \left(\frac{E}{P}\right)_0 \right]^2$$

$$\Rightarrow \frac{\alpha_e}{P} \sim \left[ \frac{U}{pd} - \left(\frac{E}{P}\right)_0 \right]^2$$

$$\alpha_e d = \frac{\alpha_e}{P} \cdot pd = pd \cdot \left[ \frac{U}{pd} - \left(\frac{E}{P}\right)_0 \right]^2 = \ln(1 + \frac{1}{\gamma})$$

$$\Rightarrow \sqrt{pd} \left[ \frac{U}{pd} - \left(\frac{E}{P}\right)_0 \right] = \sqrt{\ln(1 + \frac{1}{\gamma})}$$

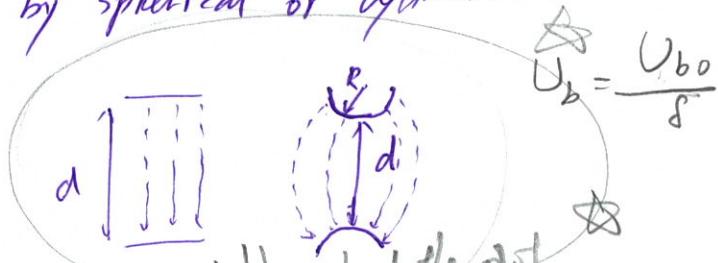
$$U = \left(\frac{E}{P}\right)_0 \cdot pd + \sqrt{\ln(1 + \frac{1}{\gamma})} \cdot \sqrt{pd} \rightarrow \text{eq 2.16}$$

Gas	$(E/P)_0$ (kv/mm bar)	$C$ (kv/mm mm)
$\text{CO}_2$	3.21	5.88
Air	2.44	2.12
$\text{N}_2$	2.44	4.85
$\text{H}_2$	1.01	2.42

plot to  
compare  
to path  
curve.

\* The mean breakdown strength can change considerably if a gap is bounded by spherical or cylindrical electrodes especially  $d > R$

$$U_b = \frac{\left(\frac{E}{P}\right)_0 \cdot pd + C(pd)^{1/2}}{\delta}$$



tell's about the plot

$$\delta = (R/r - 1) / \ln(R/r)$$

~~$\delta \propto X^{1/2} r$~~

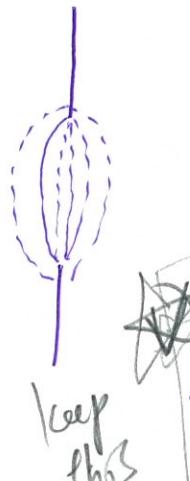
$$\delta \propto X^{1/2} r \text{ for } X/r \gg 1 \text{ where } X = d - r$$

- concentric cylinders

- equal spheres

- equal parallel cylinders  $\delta \approx \frac{X}{2r \ln(X/r)}$  for  $X/r \gg 1$  where  $X = d - r$

→ For very inhomogeneous field configurations  
(needle geometries) P25



$$E_{\text{needle}} > E_{\text{flat}}$$

Slep

$$U_b = \left(\frac{E}{P}\right)_0 pd + c(pd)^{1/2} \rightarrow \text{can only be used}$$

but with  $d_{\text{eff}}$

$d_{\text{eff}}$ : It's defined as the distance where the field has dropped to about 80% of its maximum value

\* For spherical and cylindrical electrodes,

$$\Rightarrow d_{\text{eff}} = 0.115 r \approx 0.23r$$

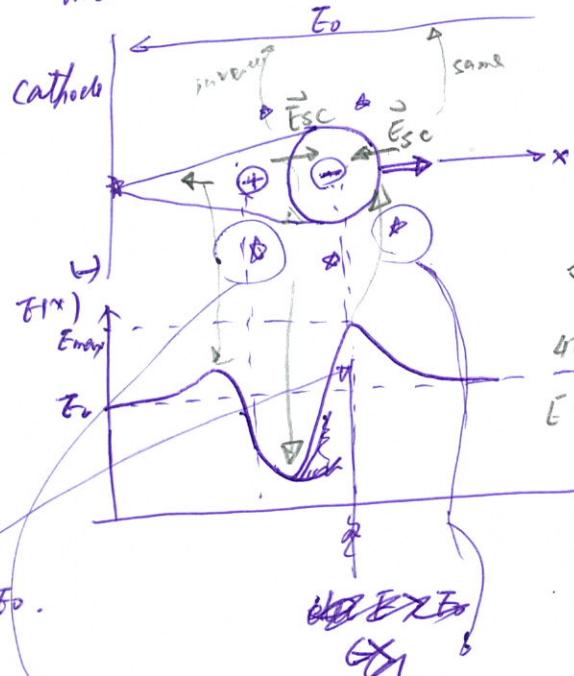


### 3.2.2.1-1 Space charge effects.

\* The space charge was neglected that is created in the electron avalanche was neglected!! But it can not be neglected if there are  $10^6 \sim 10^8$  particles in a gas at atmospheric pressure.

\* immobile ions stay behind in the avalanche tail.  
mobile electrons form the spherical avalanche head.

If there are  $N$  charged particles



$$\Delta E = \frac{eN}{E_0}$$

$$E = \frac{eN}{4\pi b_0 P^2}$$

$$E_{\text{esc}} = \frac{eN}{4\pi b_0 (\gamma\alpha)^2} = 1.5 \times 10^7 \frac{N}{(\gamma\alpha)^2}$$

$$\text{For } N = 10^7, \alpha^2 = 10^2 \text{ cm}^2$$

$$E_{\text{esc}} = 15 \text{ kV/cm} \approx \text{applied field.}$$

⇒ "Streamer mechanism"

⇒ UV light emitted in recombination and de-excitation.

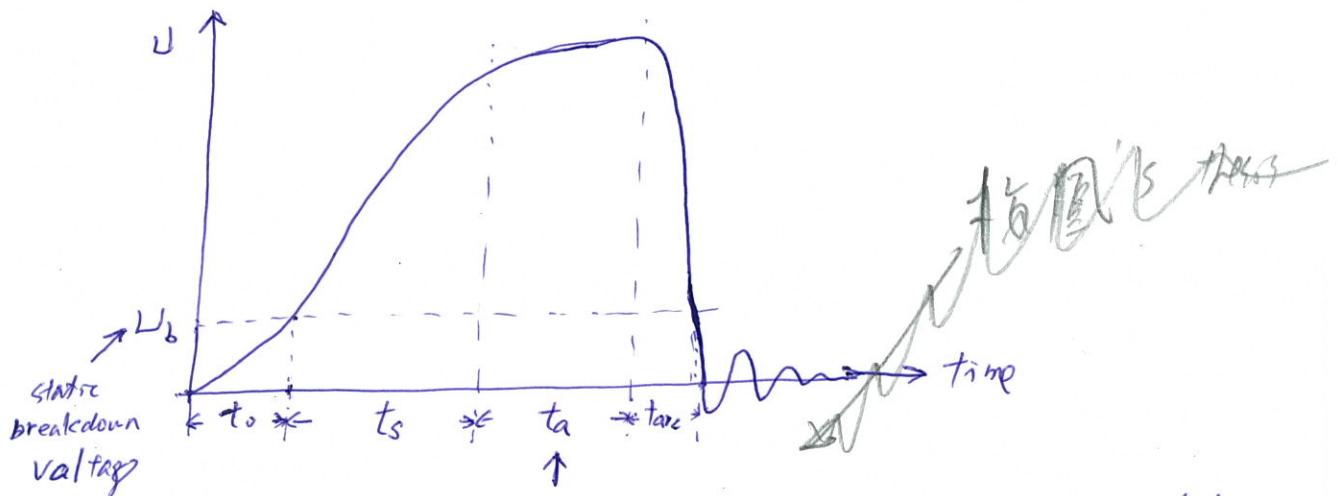
⇒ creates electrons by "photoionisation" ahead & behind the avalanche  $\Rightarrow$  form a conducting bridge between anode & cathode

- \* Creating photoelectrons at larger distances from the main streamer can advance the growth of the breakdown ~~at~~ channel rapidly.

add slope  $\Rightarrow V = 100 - 1000 \text{ cm}/\mu\text{s}$  was observed.  
at atmospheric pressure

### 3.2.2.2. Pulsed breakdown.

- \* If a fast-rising pulse across the gap, we must take into account the fact that it takes a finite time before breakdown can occur.



$t_0$ : the time until the static breakdown  $U_b$  is exceeded.

$t_s$ : statistical delay time until an electron able to create an avalanche occurs.

$t_a$ : the avalanche build-up time until the critical charge density is reached.

$t_{arc}$ : the time required to establish a low-resistance arc across the gap.

\* results from the statistics of electron appearance.

\* Free electrons can be created by illuminating the gap volume or the cathode surface with electromagnetic radiation, sun particular UV light, X-rays &  $\gamma$ -radiation.

initiate the gas  $h\nu$   $\rightarrow$   $e^-$   $\rightarrow$  photoemission.

get p32 after this page

## \* Streamer Mechanism.

- For long, atmospheric air gaps  $\rightarrow$  can't be explained using Townsend's model  
Ex)  $d \sim 1\text{ cm}$ .  $\rightarrow$  short delay time ( $< 1\mu\text{s}$ )

For Townsend's model: successive avalanches ~~are~~  
are determined by ion drifting velocity  
 $\Rightarrow \Delta t \sim \frac{1\text{ cm}}{10^5\text{ cm/sec}} \sim 10\mu\text{s}$

Ex②: breakdown ~~is~~ appears to be independent of cathode material.

Ex③: Townsend discharge: broad development from the cathode. ~~is~~

However, existence of narrow, luminous discharges originating ~~is~~ from either the anode or from the middle of the gap may happen!!

$\Rightarrow$  streamers - evocative of a thin band of bright light, attached at one end to an electrode and floating toward the other - "kanals", channel in German.

\* Cathode-directed (positive) streamers (from A  $\rightarrow$  k)

Anode-directed (negative) streamers (from k  $\rightarrow$  A)

\* single-electron avalanche  $\rightarrow$  streamer

~~when~~ Streamers develop when the charge density at the head of the avalanche becomes so large that it distorts the applied electric field.

i.e. space charge in the avalanche head generates a self-electric field that is on the order of the applied electric field.

\* Criterion for Streamer Onset:

p28 b

$$E_r \sim E_0$$

↑

generated by the space charge at the head of the avalanche.

$$\text{N}_e \sim 10^8 \text{ cm}^{-3}$$

↑

# of  $e^-$  in

$$\text{cm}^3$$

from Ark

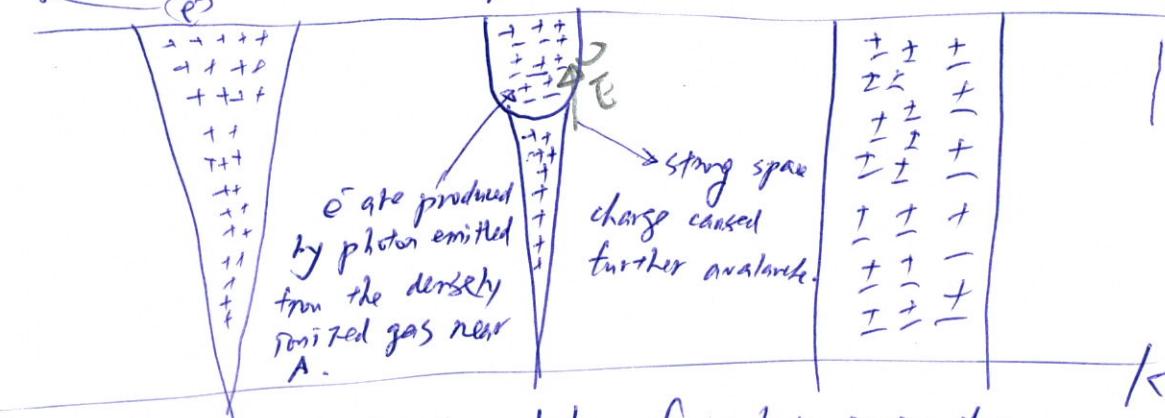
~~Space charge  
made to  
p/n~~

\* Cathode-directed (Positive) streamer:

- When the avalanche has crossed the gap, the  $e^-$  are swept into the anode, the ions remaining in a cone-shaped volume ~~extending positive~~

across the gap

are gone  
when they  
reach A



- grows w/ the help of photoionization

\* Anode-directed (Negative) streamer:

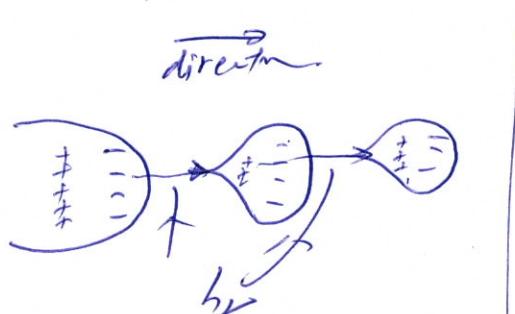
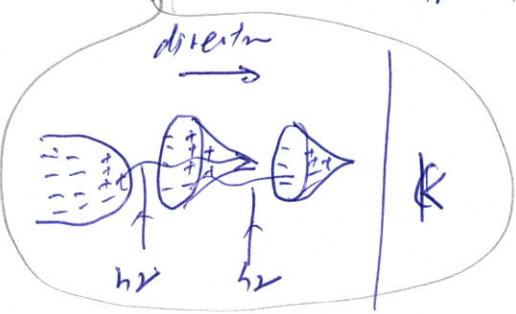
- When the primary avalanche becomes sufficiently strong before reaching the anode.

$$\# \text{ of } e^- \sim 10^8$$

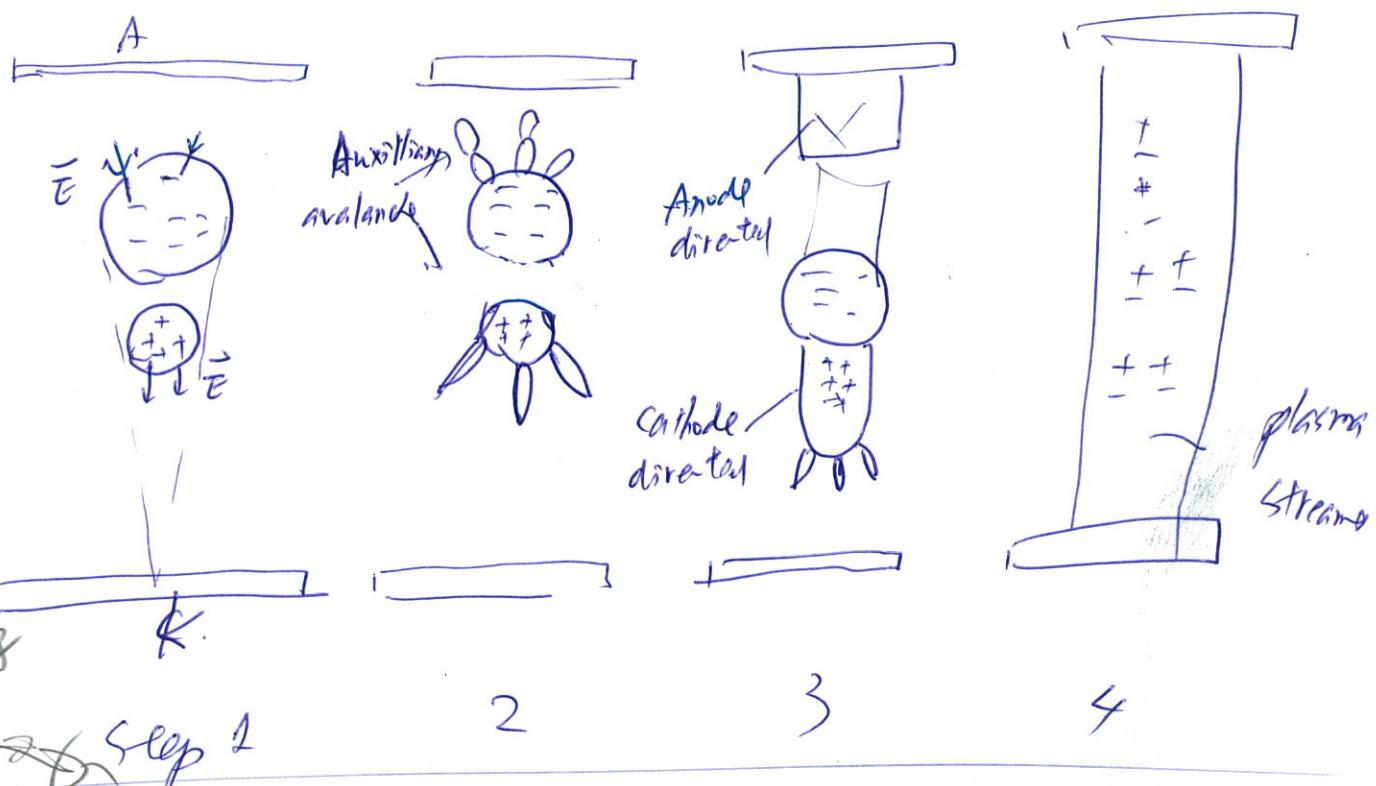
direction →

direction →

Anode



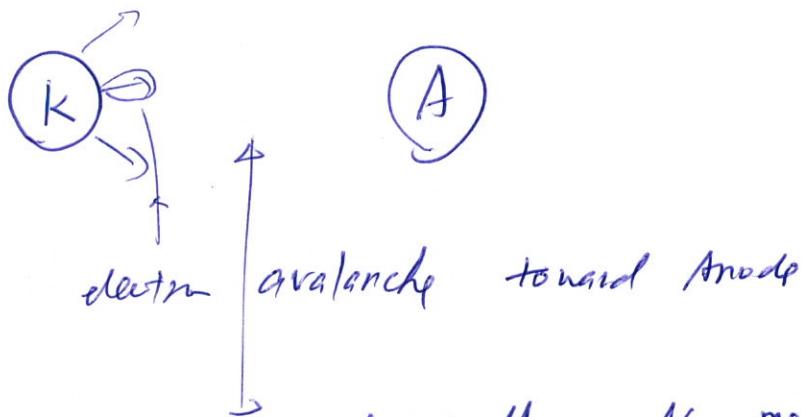
→ Overvolted Streamer:



→ The Corona dis charge.

- (after PzC)
- Corona is a luminous, audible discharge that occurs when an excessive localized electric field gradient causes ionization in the ~~surrounding~~ surrounding gas.
  - It manifests easily in highly nonuniform ~~E~~ field geometry
  - colored glow frequently visible in darkened environment
  - subtle hissing sound volume w/  $\sqrt{f}$
  - $O_3^{\bullet}$  can be generated  $\rightarrow$  rubber can be destroyed  
~~Ozone~~  
 $\rightarrow NO_3^-$  can be generated w/ moisture.

## - Negative point corona (Frichel pulses) P28



$E$  is too small  $\rightarrow$  No more ionization

$\Rightarrow e^-$  are slowed down  $\therefore$  ions left behind

$\Rightarrow$  attach to gas molecules forming  $\text{O}_2^+$  ions

$\Rightarrow E$  field cancel the external  $E$  field

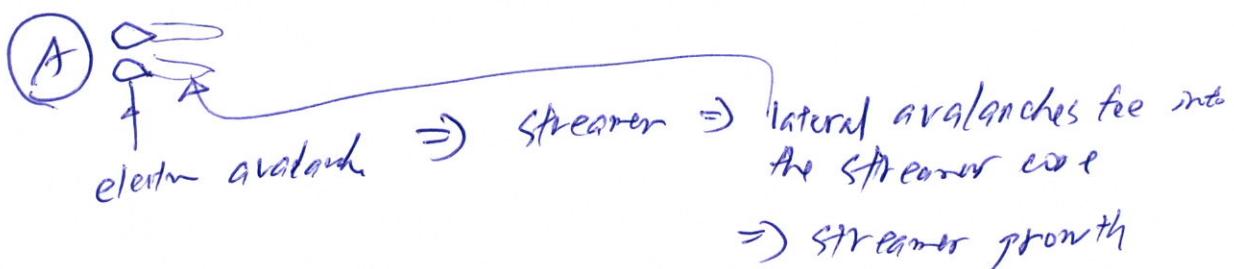
$\Rightarrow \text{O}^+$  &  $\text{O}_2^+$  ions drift to each electrode (current)

$\Rightarrow$  No more  $E$  field

$\Rightarrow$  corona again

$\Rightarrow$  steady-state corona current when  $V$  is high enough

## - Positive point corona



$\Rightarrow$  lateral avalanches feed into the streamer core

$\Rightarrow$  streamer growth

## \* Corona - power loss

- RF interference.

- service life  $\downarrow$

go back to P36 aq

\* Natural radioactivity & cosmic radiation

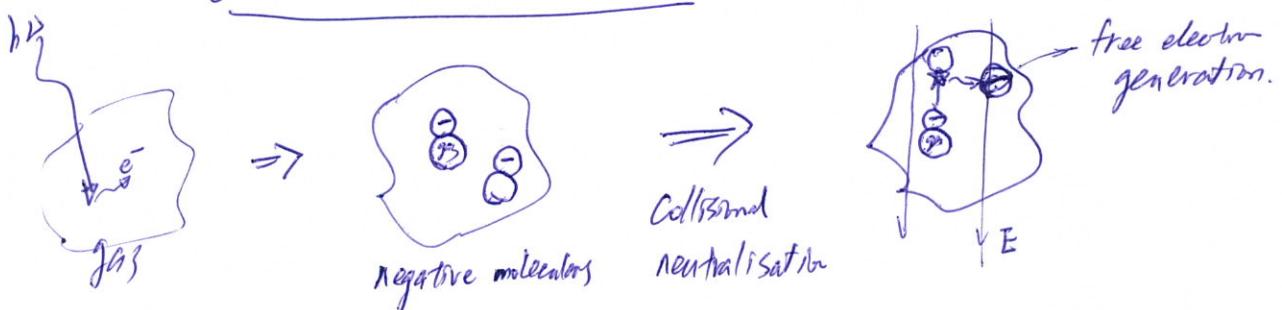
$\rightarrow n_1 \sim 10^6$  free electron /  $\text{cm}^{-3}\text{-s}$  in a gas at atmosphere.

$\rightarrow$  the electron can attach to the gas molecules

$\rightarrow$  few thousand negative moleculars /  $\text{cm}^3\text{-few minutes}$

( $SF_6$ :  $2500 SF_6^-$  ions/ $\text{cm}^3$  in 5 minutes was measured)

$\rightarrow$  With electric field  $\rightarrow e^-$  can be liberated through Collisional neutralisation  $\rightarrow$  free electron generation



$$i_s(t) = \delta \cdot N_n \cdot u_n$$

$$u_n = \mu_{\text{mix}} \cdot E$$

$i_s$ : rate of electron detachment / unit volume

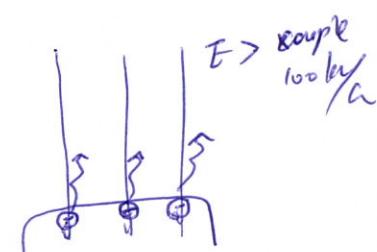
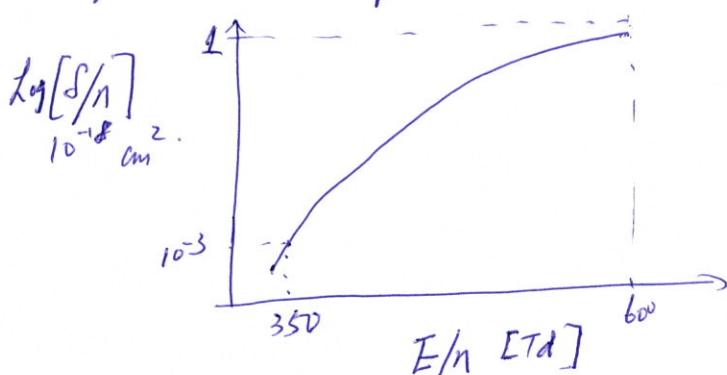
$N_n$ : density of negative ion

$\delta$ : coefficient of collisional electron detachment

$u_n$ : ion drift velocity

$\mu_{\text{mix}}$ : mobility - depends on the kind of ions

gas composition.



\* If  $E >$  few times  $100 \text{ kV/cm}$   $\rightarrow$  more electrons can leave the metal surface through the tunnel effect

The current density (Fowler-Nordheim eq. 1928)

$$J = \frac{1.54 \times 10^{-6} \beta^2 E^2}{\phi} \exp \left\{ - \frac{6.83 \times 10^7 \phi^{3/2} (1/y)}{\beta E} \right\}$$

$$0.1/y = 0.956 - 1.06 \sqrt{\beta E}$$

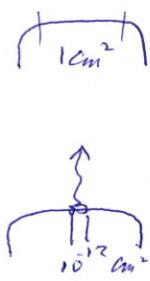
$y = 3.8 \times 10^{-4} \sqrt{\beta E}$   
 $\phi \propto \text{work function}$   
 $eV$

Enhancement factor - take into account of the spectral conditions at localised emission centers on the metallic surface.

- \* The importance of localised emission site

To generate  $10^6 \text{ e}/\text{sec}$ . from a flat metal/e surface of area  $1\text{cm}^2$ .

$$E \geq 1.2 \times 10^7 \text{ V/cm}$$
 is needed



For a localised emission site possessing a field enhancement of  $\beta=100$

$$\Rightarrow E \geq 2.4 \times 10^5 \text{ V/cm}$$
 is needed for an area of  $10^{-2} \text{ cm}^2$

- \* Most important emission centers:

- dielectric inclusions

- metallic microprotrusions (whiskers)

- absorbed gases

- \* Total number of electrons in the gap:

$$N(t) = N_{\text{no}} + N_{\text{f}}(t) + N_{\text{s}}(t)$$

$N_{\text{no}}$ : # of naturally occurring electrons in the gap, independent of  $t$

$N_{\text{f}}(t)$ : # rate of field-emission field-emitted electrons

$N_{\text{s}}(t)$ : rate of electron detachment.

- \* Note that not every electron released from into the gap is able to initiate an avalanche even if the voltage is above the static breakdown value  $V_b$ .

→ Avalanches can grow only in those parts of the gap volume where the local field strength exceeds a certain critical value.

→ For electronegative gases,  $E_{\text{cr}}$  is when the ionisation coefficient  $\alpha > \gamma$  or the electron capture coefficient.

- \* After electron

→ The probability for a single electron to initiate an avalanche:

$$g\left(\frac{E}{P}\right) = 1 - \frac{1}{\alpha} \quad \begin{cases} \text{for greater } \alpha, g\left(\frac{E}{P}\right) \text{ is larger} \\ \text{smaller } \gamma \end{cases}$$

$$\dot{N}(t) \rightarrow \dot{N}_a(t) = \int_{\text{F}}^{} g\left(\frac{E}{P}\right) \cdot N_{Fi}(t) dt + \int_{V}^{} g\left(\frac{E}{P}\right) [N_g(t) + N_{no}] dV P^3$$

probability that a breakdown has occurred before time  $t$ :

$$F(t) = 1 - e^{-\int_0^t \dot{N}_a dt} \quad (\text{conditional probability})$$

or probability density:

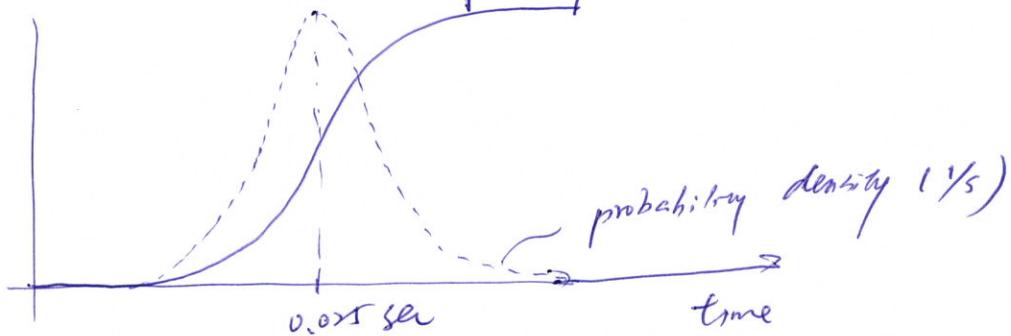
$$f(t) = \dot{N}_a e^{-\int_0^t \dot{N}_a dt}$$

Ex: 1 cm gap w/ 1 bar dry  $N_2$

$\overbrace{\text{1 bar}}^{N_2} \text{ } \boxed{1 \text{ cm}}$

$\Rightarrow$  static breakdown voltage: 31 kV

If the gap is ramped at  $6 \text{ mV/sec}$ .  
probability of avalanche initiation



$$\Rightarrow 0.025 \text{ sec} \times 6 \text{ mV/sec} = 150 \text{ kV} \Rightarrow 31 \text{ kV} \quad !!$$

$\rightarrow$  After the 1st electron avalanche there are two ways to breakdown.  
 1. Townsend breakdown  
 2. Quasi-stable glow discharge  $\rightarrow$  glow-to-spark transition.

streamer mechanism: self-propagation of the avalanche  
 ta are very different between two

$\rightarrow$  assumes that secondary  $e^-$  are released from cathode through interaction with photons & ions  $\Rightarrow$  ~~discharge~~ distributes the discharge over a larger volume

$\rightarrow$  The overvoltage must be sufficiently large such that the critical electron number  $N_{crit}$  is established in the gap during a single avalanche.  
 $\sim 15-20\% >$  static breakdown level  $U_b$

### 3.2.2.3 Spark Formation

P32

- A conducting channel exists between the anode and the cathode after a streamer has bridged the high-voltage gap.



conducting channel. (low resistance)

- An intense current starts to heat the channel and to ionise it further until a low-resistance channel

{ Toepler's model (1924, 1927)

- Pfeiffer's model (1971):

Assuming that a weakly conducting column exists and that its conductivity is increased by collisional ionisation:  
( $\sigma \uparrow$  as ionisation  $\uparrow$ )

$$dN_e = N_e \cdot \alpha \cdot dx \quad \begin{matrix} \text{electron} \\ \text{spreading speed} \end{matrix}$$

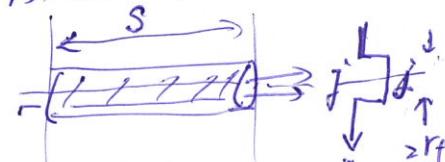
$$= N_e \cdot \alpha \cdot U_e dt \quad \text{drift velocity}$$

$$= N_e \cdot \alpha \cdot \mu_e E \cdot dt \quad \begin{matrix} \text{mean electric field in the spark} \\ \text{channel.} \end{matrix}$$

$$j = N_e \cdot \mu_e \cdot e \cdot E \quad (= N_e \cdot U_e \cdot e)$$

$$\Rightarrow dN_e = \alpha \cdot \frac{j}{e} \cdot dt \quad \Rightarrow N_e = \frac{\alpha}{e} \int_0^t j dt$$

Assuming a homogeneous current density distribution in the column



$$R_f(t) = \frac{U}{I} = \frac{E \cdot S}{j \cdot \pi r_f^2}$$

$$= \frac{E \cdot S}{\alpha (N_e(t) \cdot \mu_e \cdot e \cdot E) \pi r_f^2} = \frac{S}{\alpha \int_0^t \alpha \mu_e \cdot \pi r_f^2 dt}$$

$$= \frac{S}{\alpha \cdot \mu_e \int_0^t I dt}$$

S: channel length

r\_f: radius of the spark channel.

\* This model (Toepfer) says that:

p33

$$R \propto \frac{1}{\int I dt} = \frac{1}{Q} \rightarrow \text{charge that has been flowing through the channel}$$

\* The column expands when it is heated by the current flow.

$\Rightarrow$  It is not considered in the model

$\Rightarrow$  It is only valid for a limited time after the channel is formed, ions in a gas at atmosphere.

\* Weizel & Rompe (1964, 1965) model

- channel expansion is ignored as well.

$$R_f(t) = \frac{s}{\sqrt{2 \frac{a}{p} \int_0^t I^2 dt}}$$

$a \rightarrow \text{constant}$   
 $p \rightarrow \text{gas pressure}$

$\Rightarrow$  \* Braginskii (1958)

- consider the thermal expansion of the plasma channel



- assuming a time independent specific conductivity for the plasma channel.

$$R_f(t) = \frac{s}{\pi \sigma b^2 \int_0^t I^{2/3} dt}$$

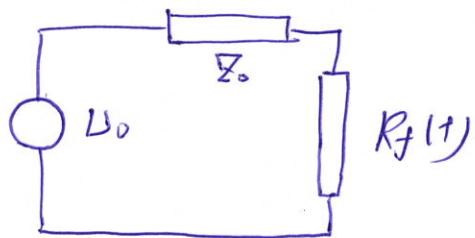
$b$ : a constant depend on density, conductivity & the thermodynamic properties of the plasma

$\sigma$ : mean plasma conductivity.

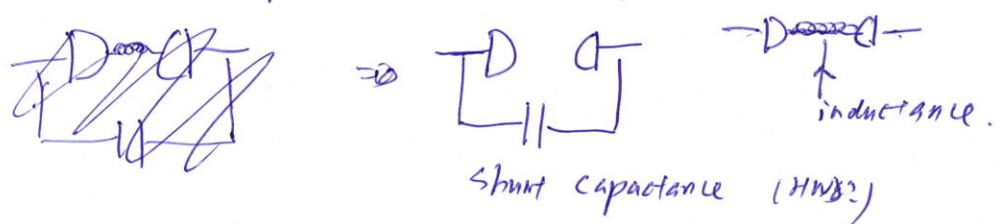
Gas	$k_T = 1/\sigma \mu e$ $(10^4 \text{ Vs/cm})$	$a$ $\text{atm cm}^2/\text{V s}$	$\sigma b^2$ $(10^4 \text{ A}^{1/3} \text{ cm/V s})$
Air	0.5 - 0.6		
$N_2$	0.4	1.1	3.5
$CO_2$	0.5	1.0	3
Argon	0.085	25	10

goto p35a  
after here

\* Let's determine the current increase and the voltage decrease across the spark using Toepfer's relationship. P34



\* Inductance of the spark & shunt capacitance are neglected.



$U_0$ : ignition voltage

$Z_0$ : impedance of the driving source.

$$I_{\max} = \frac{U_0}{Z_0 + R_f} \approx \frac{U_0}{Z_0} \quad (\text{generally, } Z_0 \gg R_f)$$

$$I = \frac{U_0}{Z_0 + R_f} = \frac{U_0}{Z_0 + \frac{S}{\alpha \mu_0} \int_0^t I dt} = \frac{U_0}{Z_0 + \frac{S \cdot k}{\int_0^t I dt}}$$

$$\frac{I}{I_{\max}} \equiv y = \frac{\frac{U_0}{Z_0}}{\frac{U_0}{Z_0} + \frac{S \cdot k}{\int_0^t I dt}} = \frac{\frac{Z_0}{U_0}}{1 + \frac{S \cdot k}{Z_0} \int_0^t \frac{1}{I} dt}$$

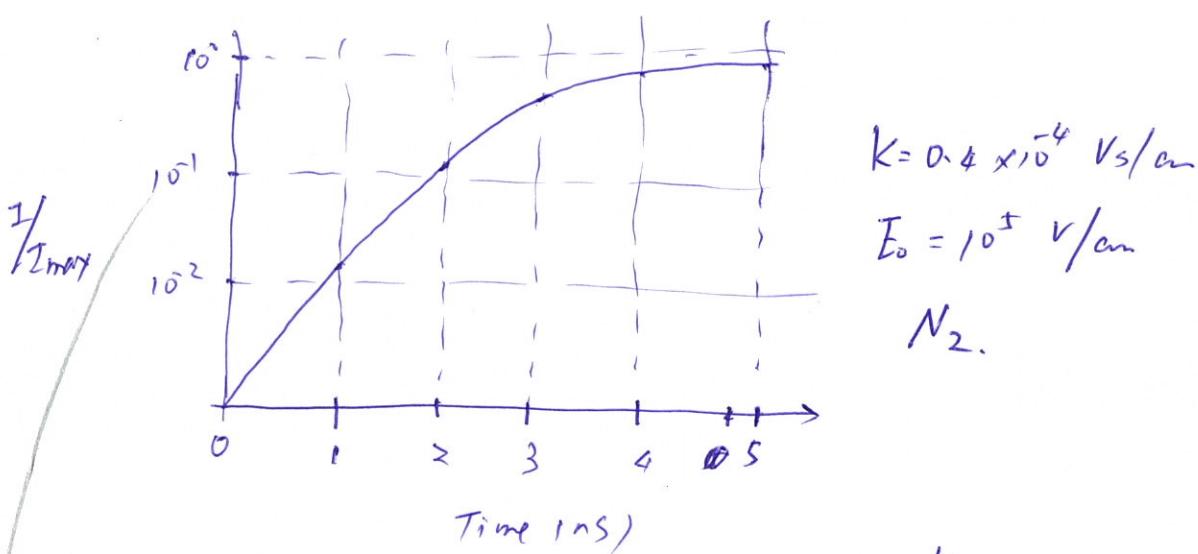
$$\Rightarrow y = \frac{1}{1 + \frac{k}{E_0} \int y dt} \Rightarrow \frac{1}{y} - 1 = \frac{k}{E_0} \int y dt$$

$$\Rightarrow \int y dt = \frac{k}{E_0} \frac{y}{1-y} \Rightarrow y = \frac{k}{E_0} \frac{dy}{dt} \cdot \frac{(1-y)+y}{(1-y)^2}$$

$$\Rightarrow dt = \frac{k}{E_0 y} \frac{dy}{(1-y)^2} \Rightarrow t = \frac{k}{E_0} \left[ \ln \left( \frac{y}{1-y} \right) + \frac{1}{1-y} + C \right]$$

Assuming that spark current begins with  $y = \frac{I}{I_{\max}} = 10^{-3}$

$$\Rightarrow C = 5.906$$



$$\text{rise time: } T_{0.1-0.9} = 13.2 \frac{K}{E_0}$$

$$\text{efolding time: } T_r = 6.84 \frac{K}{E_0}$$

$\checkmark$  J. C. Martin's (1996) formula:

$$T_r = \frac{88}{Z_0^{1/3} E_0^{4/3}} \sqrt{\frac{P}{P_0}} \quad (\text{ns})$$

$Z_0$ : impedance driving the channel.

$E_0$ : the field at the beginning of breakdown.  
in unit of  $10 \text{ kV/cm}$

$P$ : the density of the gas

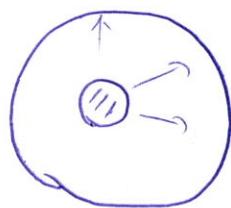
$P_0$ : - - - air under normal condition.  
(atmosphere)

# ? The corona discharge.

P35  
q

Corona - a luminous, audible discharge that occurs when an excessive localized electric field gradient causes ionization in the surrounding area.

- It manifests easily in highly nonuniform electric field geometries



colored glow wifrequently visible in darkened environment.

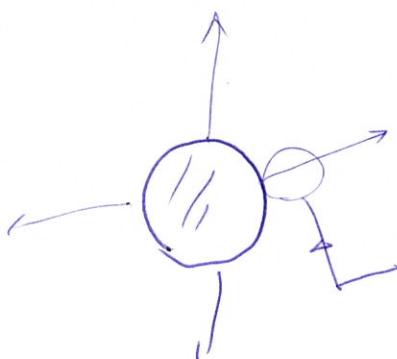
↳ a subtle hissing sound,  $\nexists w/ \nexists v$

$\Rightarrow$  Ozone is generated.

$\Rightarrow$  rubber is destroyed,  $\Rightarrow$   $\Delta E^*$   
by  $O_3$

$N_0^{+}$  is generated w/ moisture

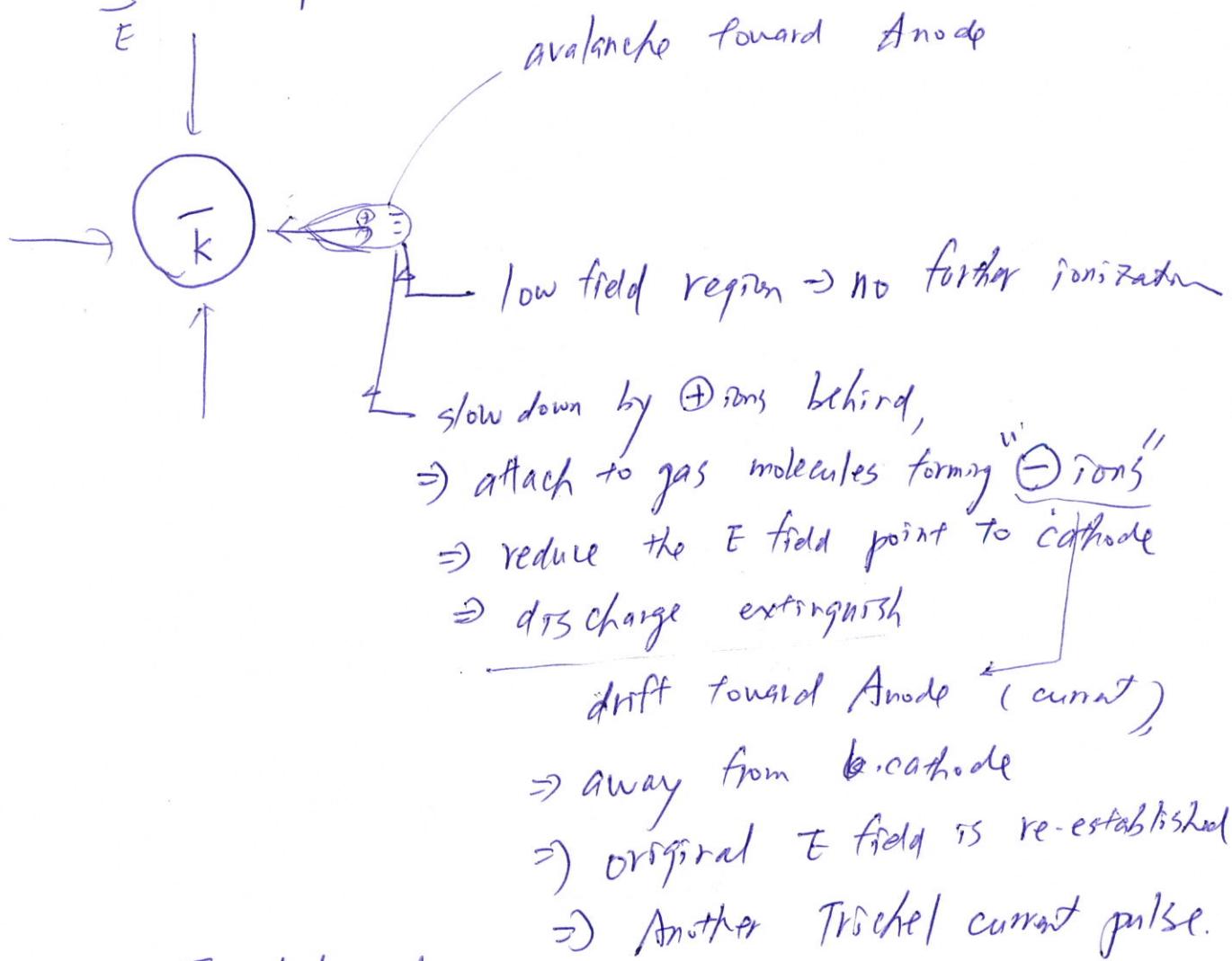
$$E \propto \frac{1}{r^2}, V \propto \frac{1}{r}$$



Townsend breakdown occurs in small region only  
 $\Rightarrow$  luminous glow w/ hissing noise.

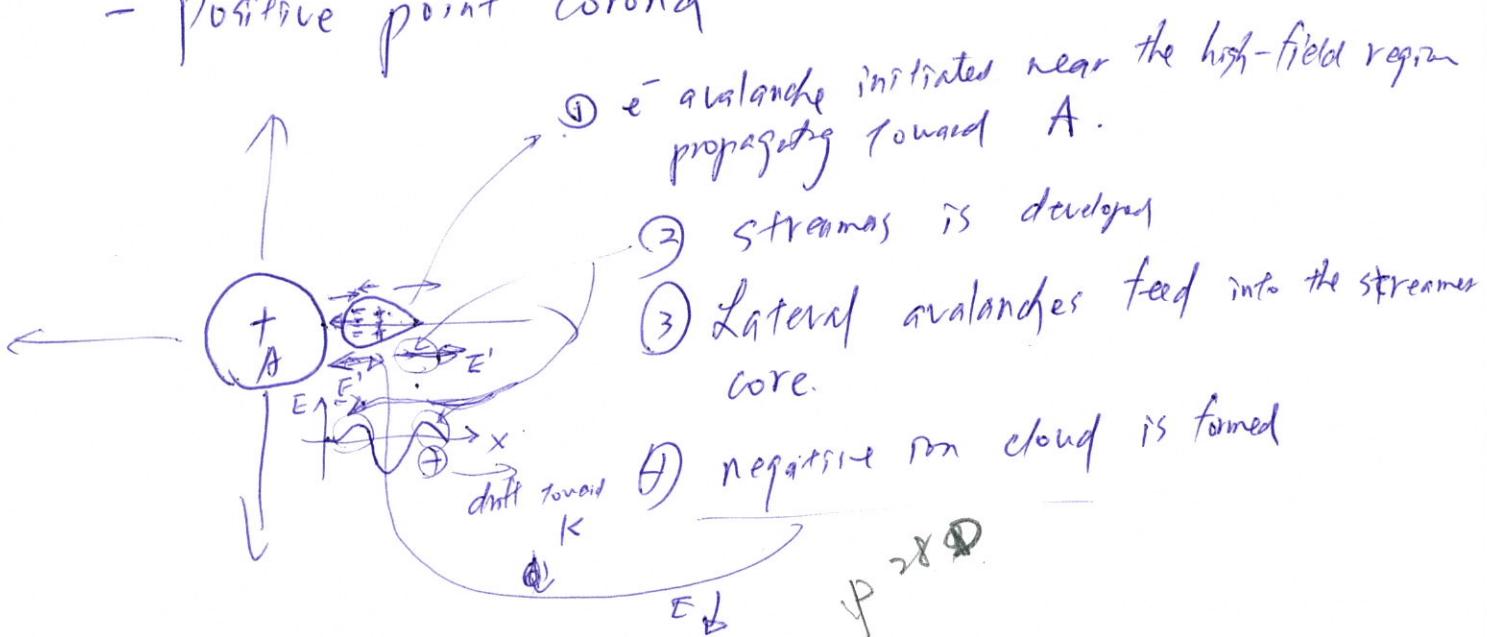
current pulses I randomly  
I regularly

- Negative point corona - Trichel pulse



- Trichel pulses are regularly spaced and only appear in gases exhibiting some  $e^-$  attachment, notably air & sulfur hexafluoride ( $\text{SF}_6$ )

- Positive point corona



Corona -

- power loss
- RF interference.
- reduce the service life of Solid & liquid insulation
- via initiating partial discharge.
- chemical decomposition

gets  $\uparrow$   $28^{\circ}\text{C}$

## 2.3 Liquids. (Lecture 4)

### 2.3.1 Basic Electrical Processes

p36  
first

- \* Breakdown initiation in the liquid can be divided onto two categories:
  - bulk liquid
  - those associated with the bulk liquid
  - those occurring at the electrodes.

\* Lewis 1985, 1987, 1993, 1994a,b,c, 1996, 1998

Charge in the bulk liquid can arise from

① molecular dissociation (分子離解)

② injection at an electrode

→ no net charge  $\neq$  in the liquid

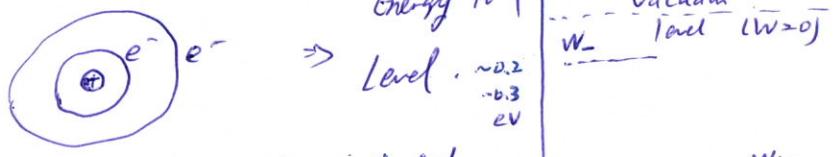
leads to either an excess or a deficiency of  $e^-$   
 $\xrightarrow{\text{excess}}$  不足

\* Charge transport occurs through

① molecular electronic state

② collective states of clusters of short-range order appearing in the liquid

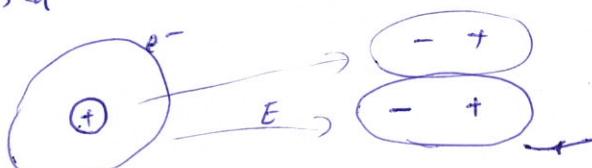
\* In atom:



Positive ion state:  $W_+$   $\rightarrow$  ionisation potential

Negative ion state:  $W_-$   $\rightarrow$  detachment potential

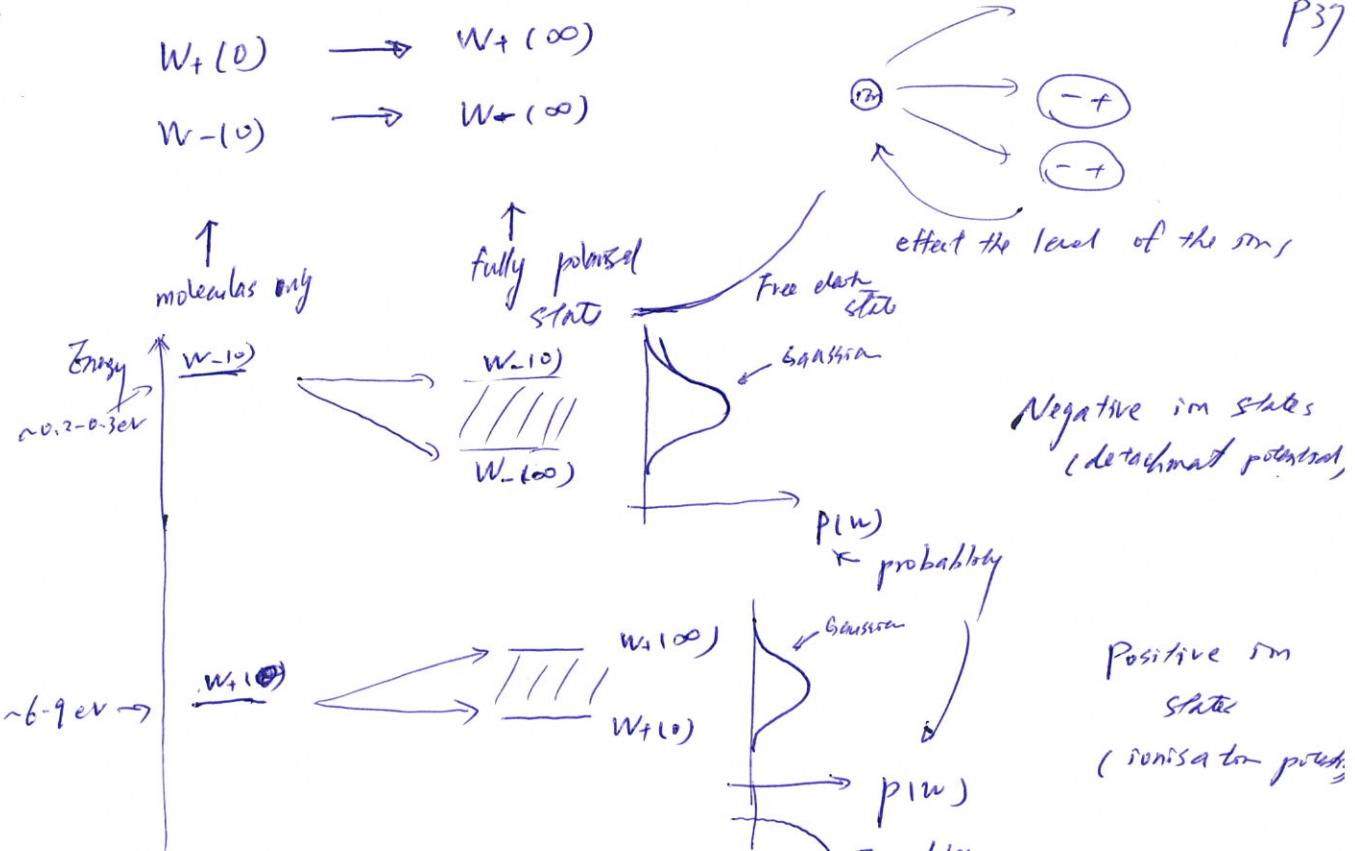
\* In liquid: ionised states are modified by the collective polarisation response of the surrounding molecules, and the energy levels corresponding to the fully polarised states shift to  $W_+(\infty)$  and  $W_-(\infty)$ , respectively.



polarised states in liquid.

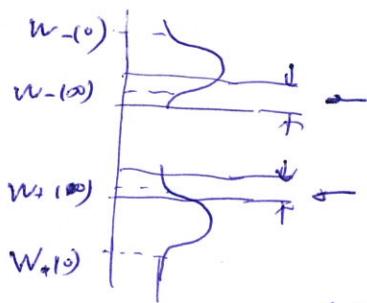
\* To create an electrical discharge in liquid: P36<sub>b</sub>

- ① a discharge in gas which occurs in gas bubbles that either are initially present in the liquid and on the electrodes or are formed under the action of voltage.  
(electrolysis, boiling, degassing of the electrode surfaces, etc.)
- ② a consequence of the avalanche multiplication of free ~~charge~~ carriers in the liquid like the model in gas.



- \* The energy associated to the shift " $W_{(10)} - W_{(\infty)}$ " consists of two parts:
  - i) polarisability of the molecular orbitals
  - ii) collective dielectric response of the more remote molecules.
- \* when the state of an ion changes by gaining or loss of an electron, molecular reorganisation occurs on a much slower timescale than that needed to relocate the electron.
- \* ( $\because$  thermal agitation  $\rightarrow$  Gaussian distribution.)
- \* Electron & hole transport in the bulk liquid can be described by a band model (of negative/positive ion states) similar to that for amorphous solids.  $\rightarrow$  no crystallized structure like liquid.
- \* (Excess) charge carriers can stay in
  - $\boxed{\text{localised}}$
  - $\boxed{\text{quasi-localised}}$
  - $\boxed{\text{quasi-free mobile states in the conduction band.}}$
- \* Quasi-free:  $e^-$  energy  $> W_{(10)}$   
 hole energy  $< W_{(10)}$ 
  - $\boxed{\text{Carriers can be considered free if they move through a sequence of states in the bands without staying long enough to induce the full electronic polarisation.}} \rightarrow \text{mobilities} > 10^{-3} \frac{\text{m}^2}{\text{V} \cdot \text{sec.}} \times \text{volt.}}$

\* Quasi-localized state:  $n_{(0)}$

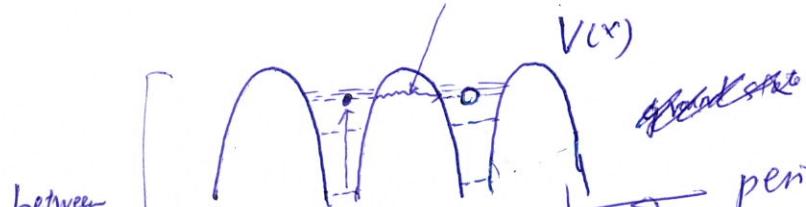


- Elections and holes which have become fully localised drift as ions with their accompanying polarisation shells (polarons), mobility  $< 10^5 \text{ m}^2/\text{V.s}$

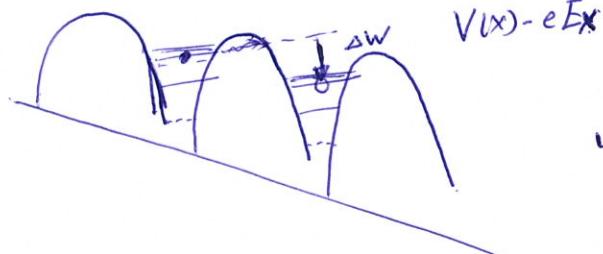


- In incident radiation & high electric field  
→ can free the charge.

resonance tunneling



between  
quasi-localized  
&  
quasi-free

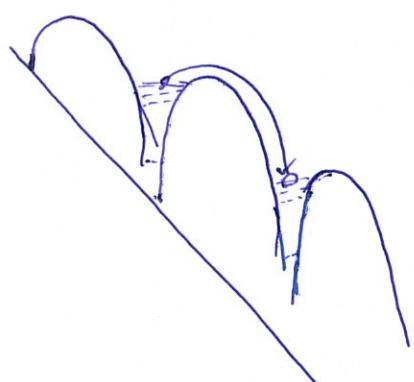


periodic potential in a molecular cluster.  
excitation of phonon energy & heating of the molecules along the electron path.

~~higher electric field:~~

with electric field:  $\Delta W$  is predominantly dissipated as phonon energy → heating of the molecules along the electron path

High electric fields: electron will be able to "jump over" the potential well (chopping process) → dissipated as heat or emission of photons.



- In the quasi-free state: the mobility of electrons (holes) is determined by scattering collisions with the liquid molecules.  
→ excite vibrational modes & loss their energy from the E field



vibration modes.

- \* Electron can be in quasi-free states, some time & in local
  - \* During transit through a liquid, electrons can thus exist for some time in quasi-free and for some time localised states.
- ⇒ effective mobility:

$$\mu_{\text{eff}} = \frac{\mu_f t_f + \mu_t t_t}{t_f + t_t}$$

$f$ : free state  
 $t$ : trapped state.  
 $\mu$ : mobility.

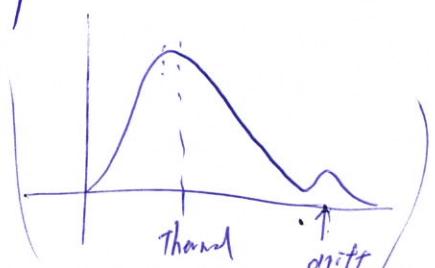
$$t_t = t_0 \exp\left(\frac{E_t}{kT}\right)$$

↑  
reciprocal of an attempt-to-escape frequency?

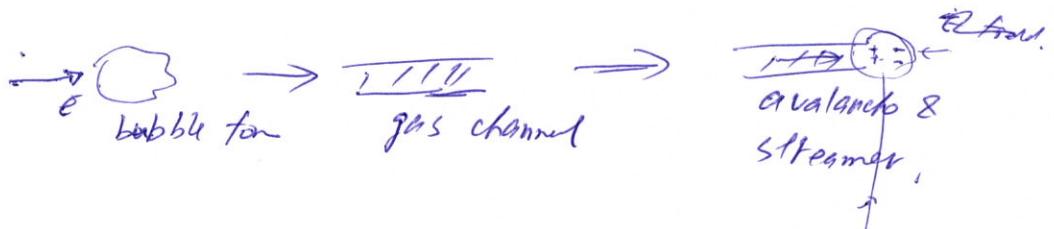
For hydrocarbons:  $E_t \approx 0.24 \text{ eV}$ .

= the time in the trap is determined by the thermal activation energy  $E_t$  necessary to liberate the electrons.

- \* With high E field  $\Rightarrow t_t \rightarrow$
- \* Most of the time, electron transit in conduction band  
 $\Rightarrow$  drift velocity ~~and~~ is limited by collision process (as mentioned in the last page)
- \* At very high field  $\Rightarrow$  drift velocity  $>$  thermal velocity  
 $\Rightarrow$  energy acquisition from the field can become quite high  
 In hydrocarbon (e.g.  $\text{CH}_4$ ), the rate is  $10^{14} \text{ ev/sec}$
- $\Rightarrow$  energy is dissipated by stimulating various molecular vibrational modes with typical quantum energies  $h\nu$  of a few tens of an eV
- $\Rightarrow E_{\text{kin}} > h\nu \Rightarrow$  cross-section for inelastic collisions ~~is~~ drops rapidly  $\Rightarrow$  electron can gain sufficient energy to excite the next mode in terms of energy, up to molecular dissociation and ionisation.
- $\Rightarrow$  Ionisation is very important in the context of breakdown, since it generates a second electron and a positive ion or hole, and an avalanche can build up in the liquid.



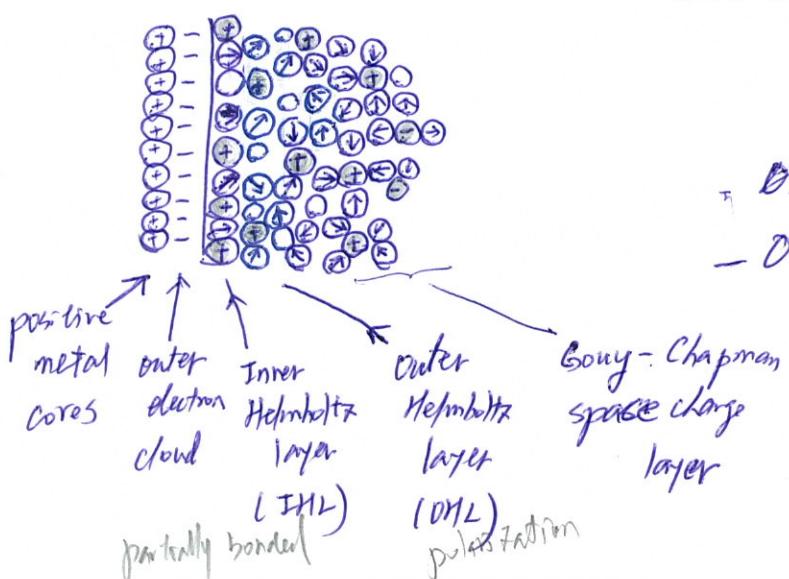
- \*  $\sim 100$  meV is needed to heat the liquid to its boiling point  $\Rightarrow$  a region of low density (RLD) may have been created before avalanching occurs in the liquid & normal density
- $\Rightarrow$  In RLD, electron avalanches can build up at much lower electric field  $\Rightarrow$  form a growing gas channel
- $\Rightarrow$  starting point of a streamer similar in gases



- \* The reported hole mobilities in liquid are typically a factor of .10 smaller than the electron mobility at equal field strength.

### 7. 2.3.1.2 Electrode Processes

- \* Electrode processes play a dominant role in the initiation of breakdown in liquid
- \* Excess electrons (or holes) may be injected from metallic electrodes into the liquid.
- \* metal - dielectric interface

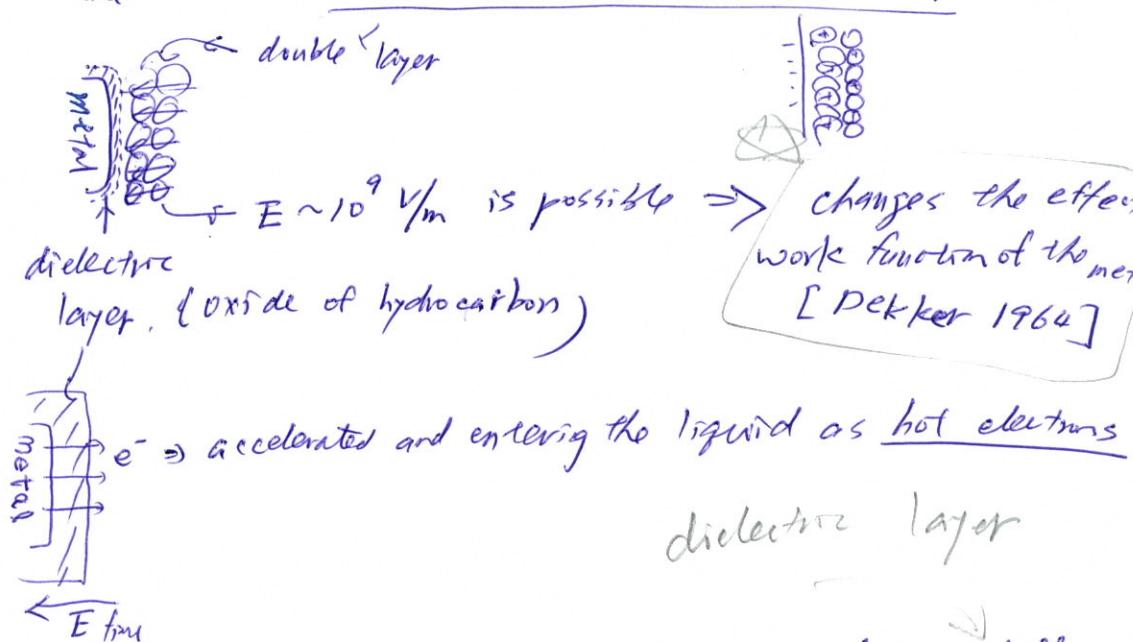


- IHL: a monolayer of ions and molecules chemically or physically bonded.  $\rightarrow$  very different from bulk liquid

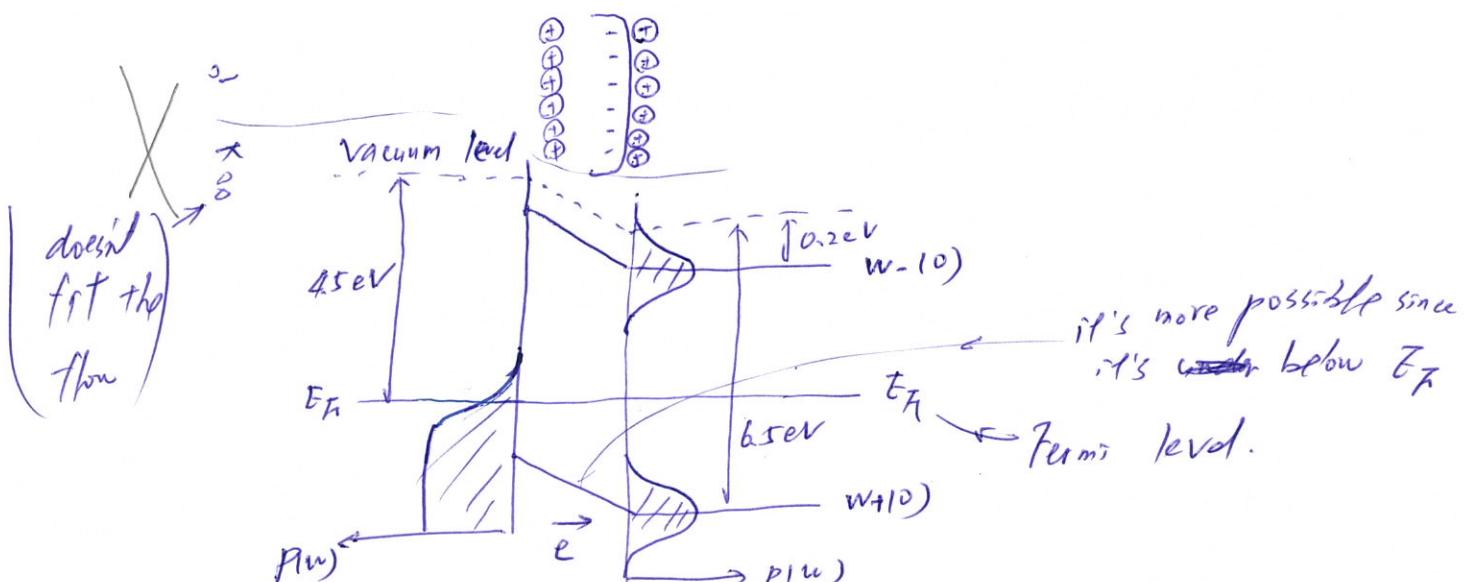
- DL: ions approach the equilibrium polarisation in the bulk liquid.

- \* Gouy-Chapman space-charge layer - a diffuse regm.  $\rightarrow$  the ions attracted into the Helmholtz layers are not sufficient to compensate all of the charge on the electrode, and the residual E field results in an additional charged layer.  $\rightarrow$  may ~~be~~ expand far into the liquid with low ion.

- \* IHL  $\rightarrow$  may become double layer if the ions moving to the surface are not neutralized immediately.



- ~~If the charge transfer through the metal interface is difficult, ions can not be neutralized at the electrodes, the electrodes will become increasingly polarized.  $\Rightarrow$  increase in the resistance of the overall system~~



- \* Less energy is required to expand the nucleation site to a critical size with sufficient low density ( $n < n_c$ ) such that electron impact ionisation can take place and a gas streamer can grow to the critical size.

For water,  ~~$r_c = 10^{-6} \text{ m}$~~ ,  $n_c = 1.4 \times 10^{26} \text{ m}^{-3}$

$$n_c = 1.4 \times 10^{26} \text{ cm}^{-3}$$

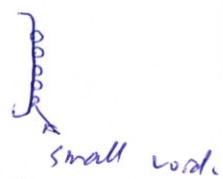
$\overset{+}{\text{H}_2\text{O}}$   
 $1 \mu\text{m}$

- \* It's still unclear how the large electron density can be inflicted to achieve the ~~superheat~~ required superheat.

~~An unrealistically large local field enhancement seems necessary to deliver the necessary electron tunnel current.~~

- Scenario 1: electrocapillarity

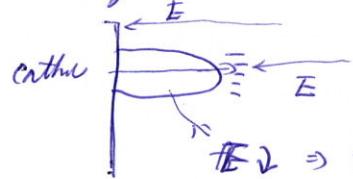
→ creates a tensile stress perpendicular to the applied field and produce voids in the liquid & small cracks in the liquid boundary layer



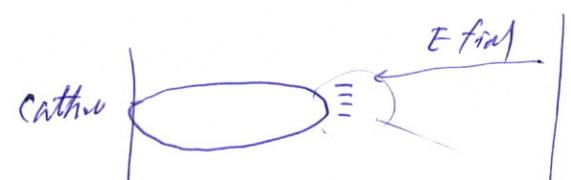
- Scenario 2: stimulated liberation of gas dissolved in the liquid.

→ preferentially at rough surfaces with cracks

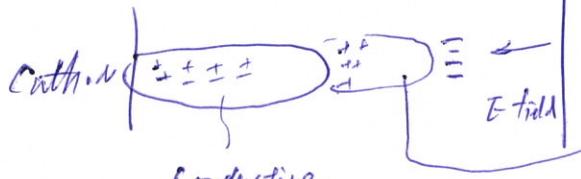
- \* Streamer can stop because of the build-up of a negative space charge in the liquid front of the space



$\Rightarrow$  streamer stop



- \* Electron can be accelerated toward to the streamer tip into the liquid → form a new space charge and start another heating and evaporation cycle.



If it's heated and become a region of low density before the space charge build up  $\Rightarrow$  streamer die.

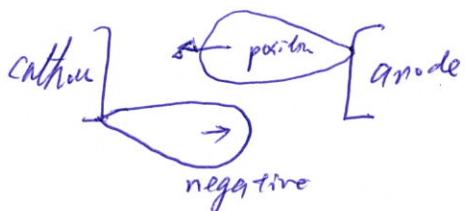
It helps maintaining the potential at the front closed to electrodes by causing streamer die.

7.2.3.7 streamer breakdown

px2

→ figure for power point.

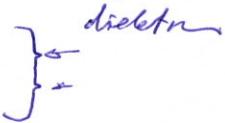
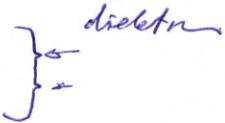
- \* Positive and negative streamers propagate towards the cathode and anode respectively

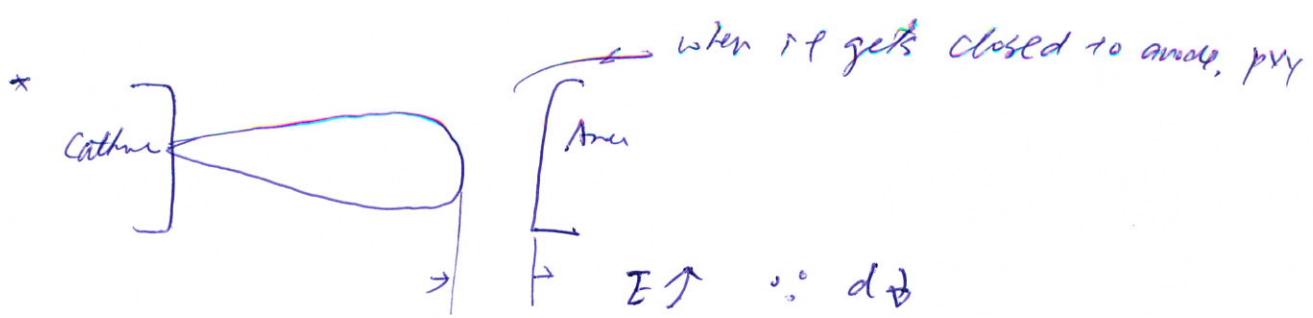


- \* Schlieren diagnostics have shown that a streamer consists of a gaseous phase → breakdown strength should increase with pressure & gas is not formed easily.
- \* Temperature has a minor effect.

#### 7.2.3.2.1 Cathode initiation (negative streamer)

- \* Primary process for the initiation of a negative streamer is the injection of hot electrons into the liquid. This can occur through:
  - ① dielectric (oxide) emission
  - ② metallic microprotrusion.
    - ↳ A) on the electrode surface
    - ↳ B) contaminant particle in the liquid.
- \* If sufficiently large electron current density is injected into the liquid, a gas bubble of critical size & density may form at the electrode surface.
  - $> 10^9 \text{ J/m}^3$  (for water) must be deposited adiabatically in the liquid to create enough superheating [Jones and Kunhardt, 1995.]

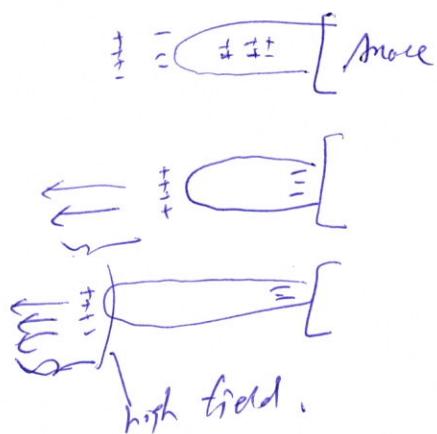




$\Rightarrow$  ~~the~~ initiates a secondary or tertiary streamer.

### 3.2.3.2 Anode initiation (positive streamer)

- \* Initiated by hole injection from an oxide microregion on the anode surface.  $\rightarrow$  liquid-metal interface
  - liquid-plasma boundary of a streamer
- \* Liberation of electrons from traps, quasi-localised states, or molecules with a low ionisation potential through field ionisation in the vicinity of a microprominence on the anode.



### 3.2.3.2 Water:

- \* Important dielectric liquid in pulsed-power application
- High electric breakdown strength ( $\text{up to } 3 \times 10^7 \text{ V/m}$ ) for its electric stress
- High permittivity  $(\epsilon_0)$   $\rightarrow$  store large energy densities for short time.
- water molecules  $\rightarrow$  simple structure,
  - $\hookrightarrow$  intramolecular electron transport is unimportant
- possess large dipole moment
- property ② metal-liquid boundary layer  $\approx$  bulk liquid

- much greater density for the 1<sup>st</sup> layer than in bulk water per  
 $\Rightarrow$  strong impact on electron transfer  
 $\Rightarrow$  - - - the formation of gaps in the boundary layer due to electrocapillarity
- ~~small fraction ( $1 \sim 10^{-3}$ )~~ dissociated into  $H^+$  &  $OH^-$   
 $\Rightarrow$  a residual conductivity  $4 \times 10^{-6} \text{ S/m}$   
 ~~$\checkmark$~~  Inadequate for DC-insulation  
 $\hookrightarrow$  ionic currents do not contribute to the initiation of breakdown for submicrosecond pulses.
- $\checkmark$  can dissolve a lot of gases ( $N_2, O_2, CO_2$ )  $\Rightarrow$  tend to form gas bubbles and thus facilitate the appearance of a streamer.  
 $\checkmark$  pressure  $\nearrow \Rightarrow$  dynamic breakdown strength  $\nearrow$   
 $\checkmark$  time lag to breakdown ~~is longer~~ in "doubly distilled" water without gas  $\nearrow 50\%$

### \* Transformer oil for insulation: (insulating)

- The natural moistening of insulating oils does not change their pulsed electric strength at voltage action times of  $10^{-8} \text{ s}$  even if the dc breakdown voltage changes three times!!.
- Requirements to the purity of the insulating liquids used in pulsed power systems can be moderated.

## Q. 2.4 Solids

P46

The phenomenon of dielectric breakdown in solids is linked inseparably to the progressive destruction of the dielectric medium by electronic or ion charge carriers that have acquired sufficient energy from the electric field.

Insulator material	Dielectric constant $\epsilon$	Breakdown strength (MV/m) kV/mm
Air	1	3.0
Kapton	3.6	275
Mylar	2.5	200 > 20
Polyethylene (PE, 聚乙稀)	2.2	127 12.7
Polypropylene (PP, 聚丙烯)	2.5	328 32.8
Poly sulphone (聚石風)	3.1	315 31.5
Pyrex glass	4-6	20
SF <sub>6</sub>	1.0	8 (per atm)
Teflon	2.0	59.
Transformer oil	2.2	10-40
Water	80	> 10 (for $< 1 \mu\text{s}$ )

\* Strong bonding energies in solid ~ several eV  
impact ionisation ~ 10 - 20 eV

Solid insulators : Breakdown strength ~ 100 MV/m.

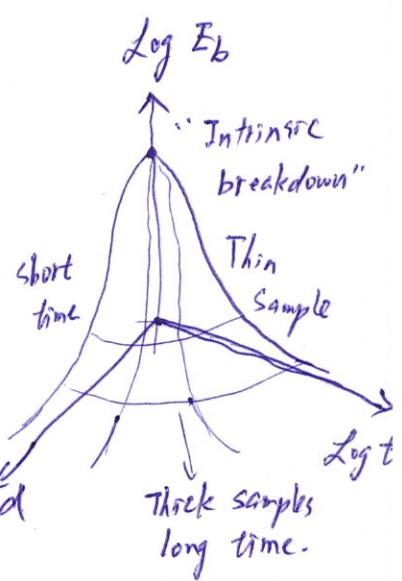
$$\frac{10 \text{ eV}}{100 \text{ MV/m}} = \frac{0.1 \mu\text{m}}{\text{Required MFP}}$$

distance b/w  
electrons gain 10eV in a  
field of 100MV/m

$\Rightarrow$  distance between  $\sim 1\mu\text{m}$  such that electron can gain 10 eV of energy in a field of  $100 \text{ MV/m}$

Typically, mean free path of  $0.1 \sim 1\mu\text{m}$  is required to ~~breakdown~~ break bonds and ionise material at the observed breakdown field strength.

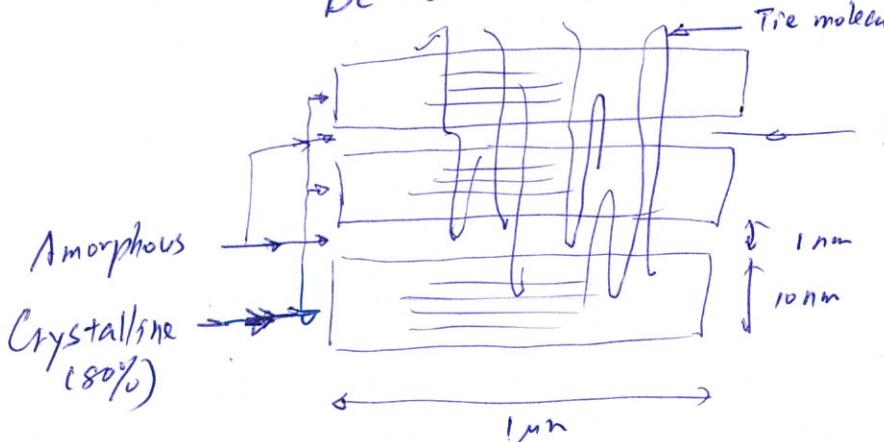
- \* The chance of inducing electron avalanches in 2D or 1D lattices such as those of polymers is very small.
- \* Damage can be done only if either the damage threshold is reduced  $\Rightarrow$  or electrons are allowed to move over significantly longer free paths.
- \* Magnitude of the breakdown field depend on:
  - time dependence of the electric field.
  - geometry of the sample.
  - nature of the electrode.
- \* Breakdown strength reduces ~~with~~ with
  - increasing thickness
  - longer time
- \* "Intrinsic" breakdown strength is where the material is without defects & without external influences.
  - $\sim 2 \sim 3$  orders of magnitude above the design stress in technological applicator
- \* Breakdown strength is temperature-independent in most insulating materials, but drops drastically after critical temp.



- \* The final result of a breakdown is always the formation of a narrow plasma channel.
- \* Electroniz charge carrier injection from the electrodes accelerates the breakdown.
- \* The presence of macroscopic defects in the material (e.g. void or conducting inclusions) shorten the time to breakdown.
- \* The aging of the electric strength of a material is strongly affected by charge carrier injection & trapping.
- \* Damage is done continuously to the material prior to the onset of the final breakdown.
- \* Electrical breakdown must at least ~~start~~ begin at a molecular level →
  - charge transport
  - charge injection
  - breakdown.

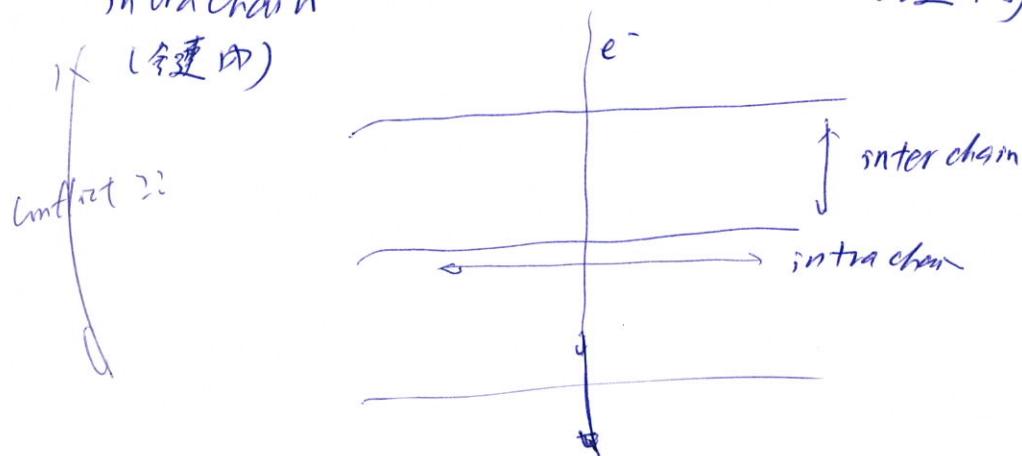
### 7. 24.2-1. Charge transport.

- \* The most important solid insulators in pulsed-power technology or organic polymeric dielectrics such as polyethylene (PE) or cast epoxy.
- long-chain molecules with strong covalent bonding in the chains and weak Van der Waals bonding between chains.

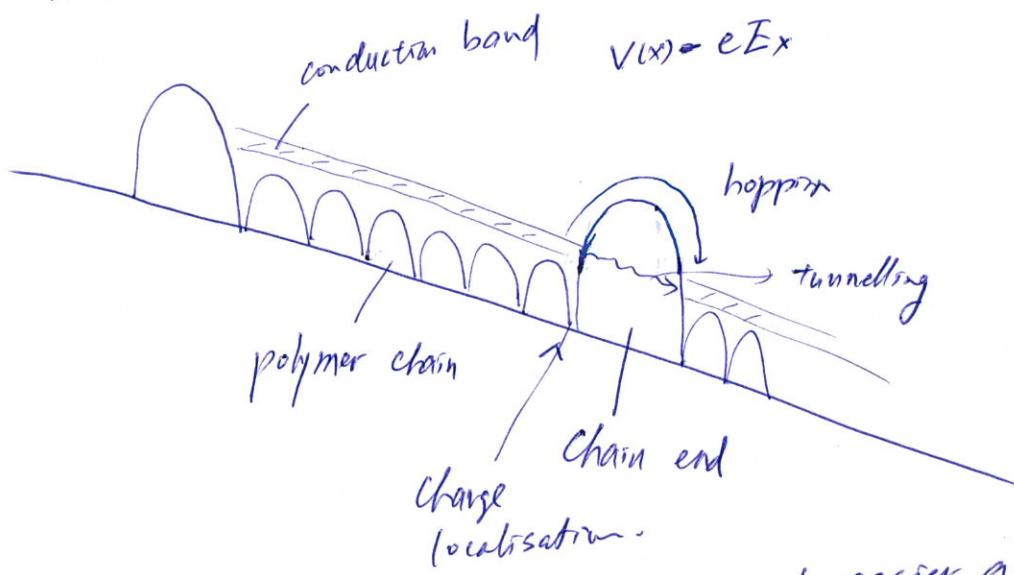


strong covalent bond  
weak van der Waals bond.  
Impurities including gases, water, are relatively easy incorporated in amorphous regions.  
electronic states of a polymeric soln are similar to those of isolated chain molecules.

(\*) Free-electron transport will follow interchain rather than <sup>p49</sup>  
intrachain (金連間)



→ Electrons will move in the ~~per~~ periodic potential along chain surface.

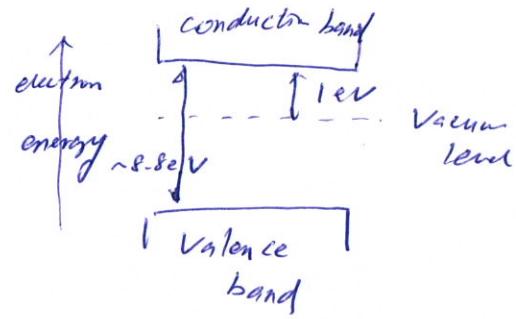


- \* ~~Electrons~~ Free electrons & holes transport easier along chains that happen to lie in the field direction. Chain ends, folds, kinks, and branching will interrupt the periodicity and lead to charge localisation. → hopping & tunnelling.
- \* electrons & holes can become trapped at dopant impurities.

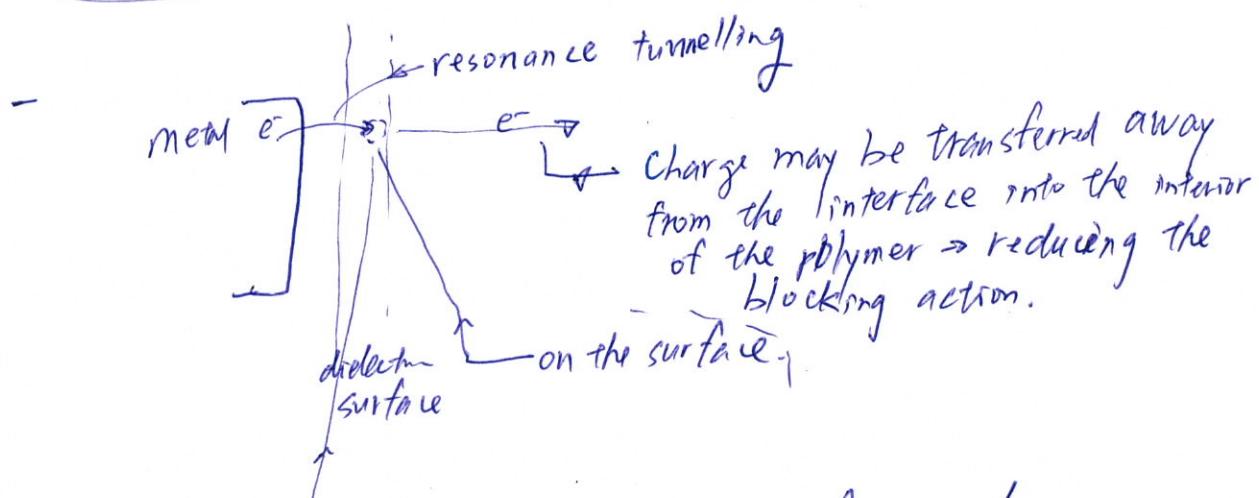
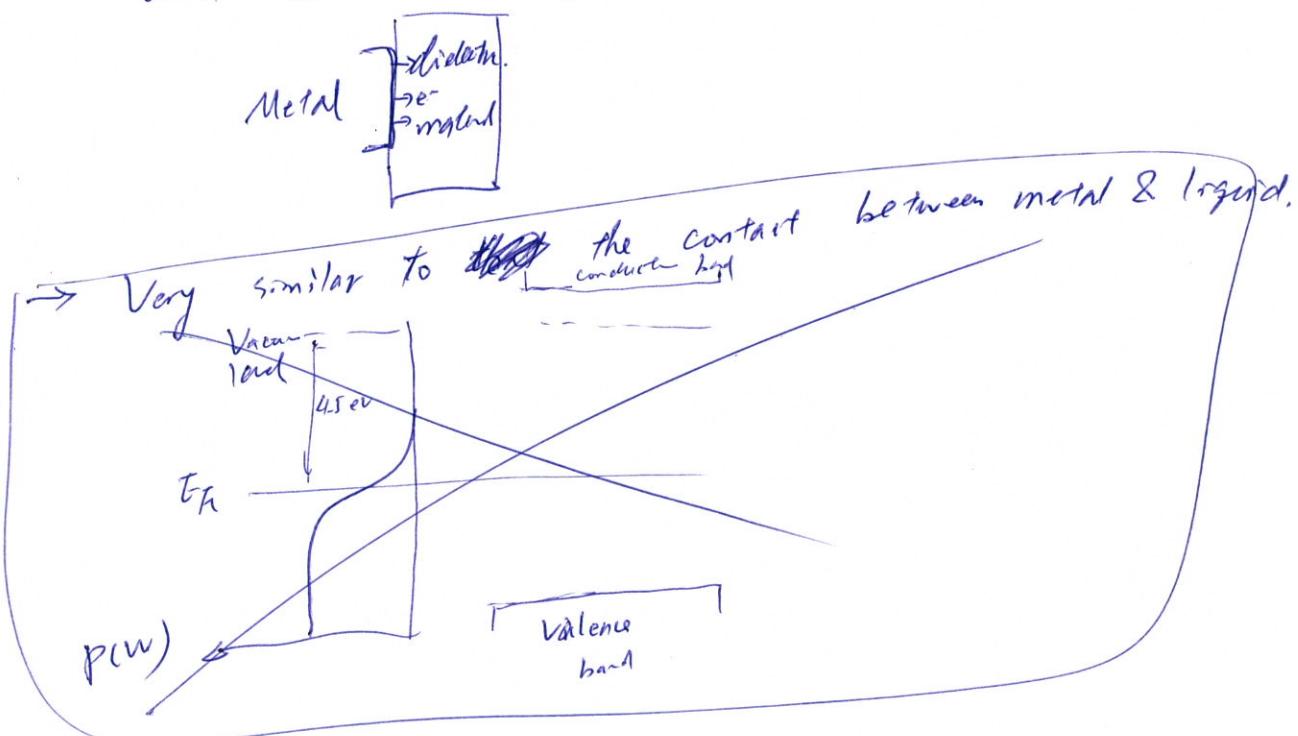
## 7.4.2.2 Metal - Dielectric Contact.

P50

- \* The large band gap of insulating polymers ( $> 8 \text{ eV}$ ) makes it very unlikely that mobile charge carriers can be created thermally.



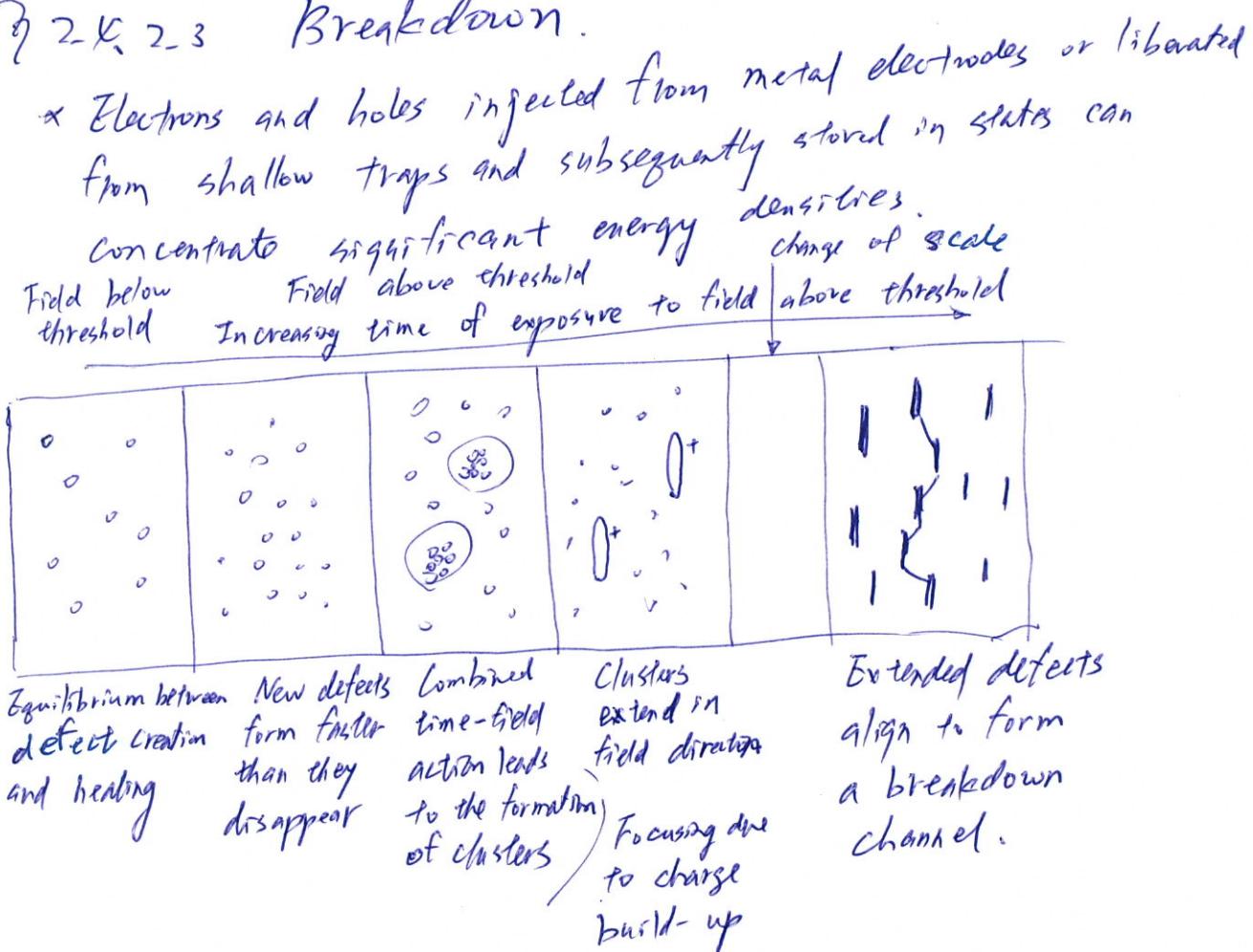
- appropriate dopants or by injection of electrons or holes from metallic electrodes.
- A metal electrode in contact with a dielectric solid will transfer charge into the solid.



If the charge remains at surface states, further tunnelling will stop and current flow across the surface will become blocked.

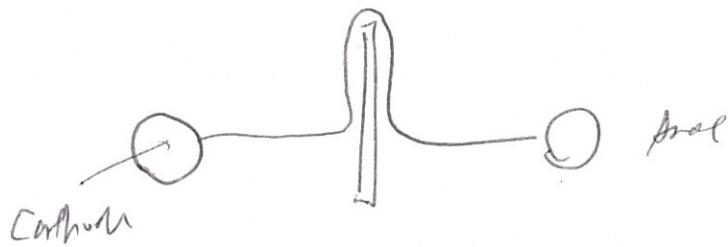
- \* At even bigger larger electric field
  - electrons can reach excited states.
  - Decay from excited states will remove the energy from electrons to the molecular and heat it
- \* At the highest fields
  - electrons can reach the band of extended conduction states.
  - energy-dissipating mechanism becomes scattering from lattice vibrations → kinetic energies sufficient for ionisation can be reached.
- \* Note that it is still restricted that the chain is parallel to the field direction.

### 2.K.2.3 Breakdown.

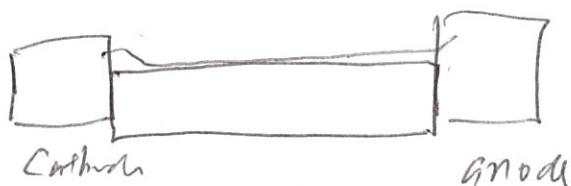


# 7. Flashover of solid dielectric

p.51 a

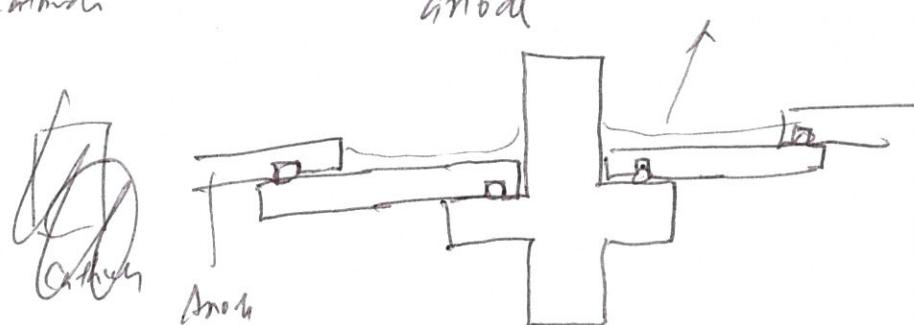


or



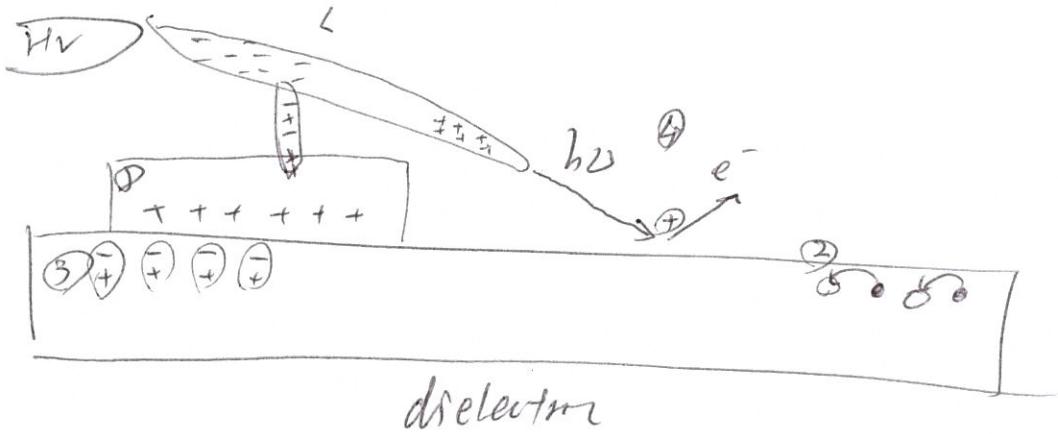
Flashover:

or



Cathode

- ⇒
  - Charge carriers formation near the dielectric.
  - Surface can be a source for the discharge plasma.
  - Generality of mechanisms of surface discharges in different mediums is in interaction of sparks and streamers w/ the surface of dielectrics

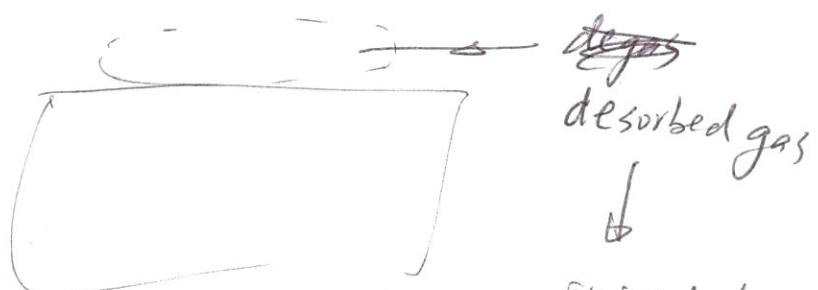


1. surface charge
2. surface conductivity
3. polarization of the insulator
4. photoemission & thermionic emission

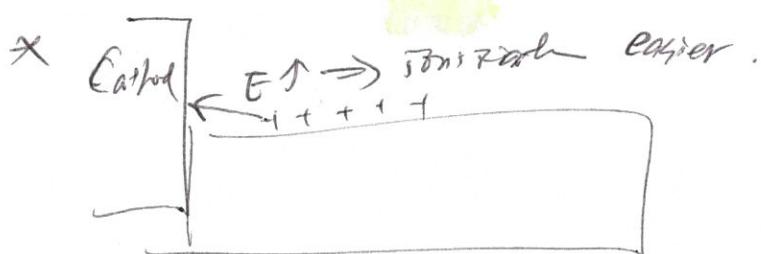
\* 2<sup>nd</sup> electron emission from the dielectric surface → surface is +

\* degas:

(Q)

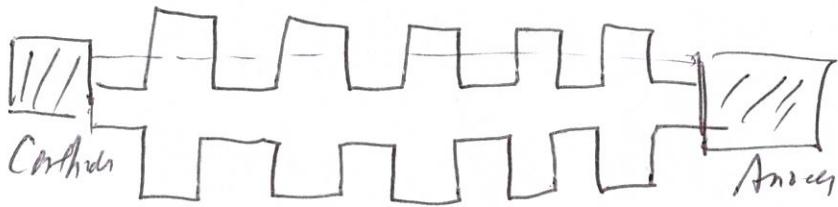


Tonized by  
electn



Solution :

RE  
PSYC



"No line of sight"

---

### 3. Breakdown in solid.

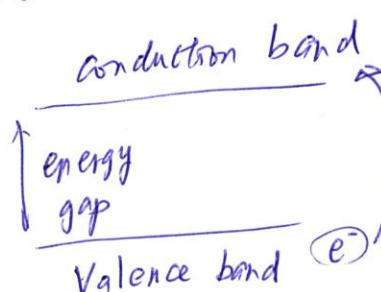
- Solid insulators function as mechanical supports, enclosures, and feed through.
- Thin films of solid insulation are used in energy storage capacitors & pulse-forming line (PFLs) for high energy density storage, and advances in metallized films w/ their self-healing properties are revolutionary.
- Common solid film insulators: *polyethylene terephthalate*, *paper*, *polypropylene (PP)*, *Mylar (PET)*, *& kapton (polyimide)*, *Teflon*, *Acrylic*, *polyvinylidene fluoride (PVDF)*
- Outdoor installations: operate in humid & polluted environment.
- For repetitive pulsed power systems: thermal considerations such as effective cooling becomes important.

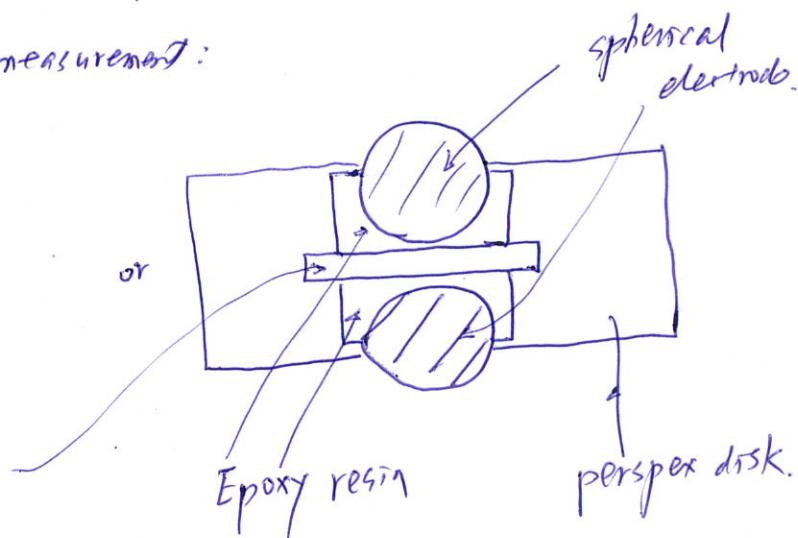
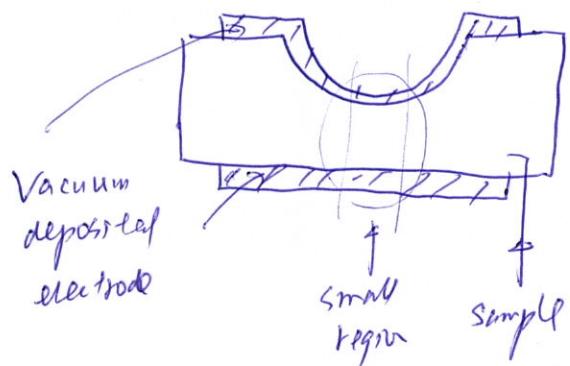
### 3) breakdown Mechanisms in Solids

- Solids are usually permanently damaged when breakdown occurs
- Intrinsic breakdown
- Thermal breakdown
- Electromechanical breakdown
- Partial discharges
- Electrical trees.

## Q Intrinsic breakdown.

P2

- The highest values of breakdown strength when other sources of imperfections in the material and testing are eliminated.
- The timescale ~ in the order of  $10\text{ ns}$
-  when it gains enough energy from a high electric field.
- w/ sufficient  $e^-$  in the conduction band, intrinsic breakdown occurs
- In the range of  $5-10\text{ MV/cm}$ .
- In Lab.: it is measured via eliminating all imperfections:
  - field non uniformity
  - internal discharges from imperfections (foreign particles or voids)
  - external discharges - from weak ambient surrounding the solid dielectric.
  - mechanical damage
  - field induced chemical attacks
- NOT in practical systems.
- Typical setup measurement:



- Very thin specimens of solid dielectric are used. p3
  - reasonable  $V$  ( $E = V/d$ )
  - probability of imperfections (foreign particles, void)
- proper mechanical support is needed,
  - avoid electromechanical force.
- Short duration pulses w/ high voltage rising speed.
  - avoid other breakdown mechanism, such as thermal breakdown from Joule heating.

• Frohlich criterion: (conduction)

If the net energy gained by an electron ~~escapes~~ from the electric field is greater than the energy lost to the lattice, the electron is continuously accelerated, resulting in a state of instability and intrinsic breakdown occurs.

→ does not depend on the specimen thickness or wavefront, or duration of applied field.

high-energy criterion  
 $(\text{Energy gain} \propto E_{\text{dc}}^{3/2})$   
 $> \text{Energy loss} \propto E_{\text{dc}}^{-1/2}$

~~high energy electrons dominate the breakdown~~

low-energy criterion

Avalanche criterion

Conduction electrons gain sufficient energy from the applied field to release further electrons from the lattice, similar to impact ionization in gas.

→ depends on thickness, electrode geometry.  
 "time to breakdown" would depend on the overvoltage applied to the specimen.

by Thermal breakdown.

Px

- happen when  $\underbrace{\text{generating heat}}_{\substack{\text{rate of} \\ \text{due to conduction}}} > \text{dissipation rate}$

due to conduction or dielectric losses (AC)

$\rightarrow$  depends on  $\blacksquare$  Voltage

- If heat gain  $>$  loss  $\Rightarrow$  thermal equilibrium is unstable.  
 $\Rightarrow$  thermal runaway. (热失控)

$HG_{DC} = \frac{\sigma E^2}{\text{conductivity}} - \text{Joule heating.} - DC$

$\rightarrow$  Electric field.

$C_p \frac{dT}{dt}$   $\rightarrow$  Rate of heat accumulation.

$\int_C dt = \text{length of } C$  to a surface

$$\frac{\partial}{\partial x} \left( k_m \frac{\partial T}{\partial x} \right) = \text{heat lost to a surface}$$

$$\Rightarrow Hg_{nc} = \alpha \bar{E}^2 = \underbrace{C_r \frac{\partial T}{\partial t}}_{\text{heat accumulation}} + \underbrace{\frac{\partial}{\partial x} \left( k_m \frac{\partial T}{\partial x} \right)}_{\text{diffusion}}$$

↑  
source & heat accumulation  
(loss+)

For AC, dielectric losses from dipole rotation. ~~heat~~ & joint heating.

$$H_{\text{Soc}} = E^2 \cdot 2\pi f \cdot \epsilon_0 \cdot \epsilon_r \frac{\tan \delta}{\tan \phi}$$

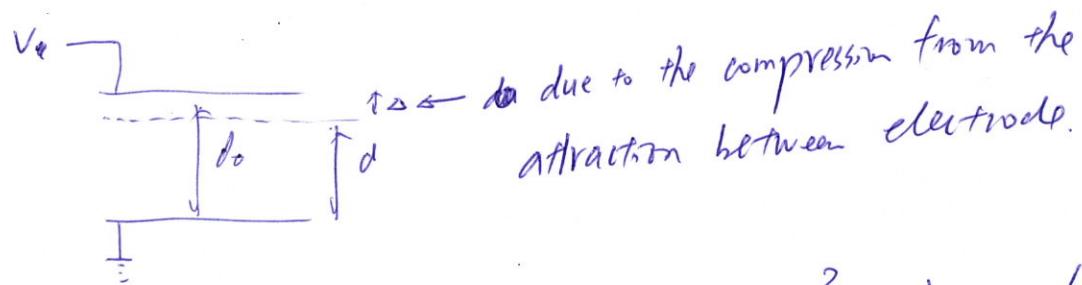
dielectric loss tangent

$$\Rightarrow H_{GAC} = E^2 \frac{\partial f}{\partial t} - g_0 \cdot \dot{r}_x \tan \delta = C_V \frac{\partial T}{\partial t} + \frac{\partial}{\partial x} \left( K_B \frac{\partial T}{\partial x} \right)$$

- Generally, the thermal breakdown need not be considered for DC  
 $\because$  low conductivity of good insulator.
  - For pulsed high electric field, w/ high dielectric losses  $\rightarrow$  H<sub>Gc</sub> is important.  
 ex: Thermal breakdown @ room temperature,  $\sim 10 \text{ MV/cm}$   
 w/  $\sim 100 \text{ kV/cm}$   $\xrightarrow{\text{2 order less}}$  !!.

## 3 Electromechanical breakdown

P5



compressive force :  $P_c = \frac{1}{2} \epsilon_0 \epsilon_r E^2 = \frac{1}{2} \epsilon_0 \epsilon_r \left(\frac{V}{d}\right)^2$

Hooke's law :  $P_c = Y \ln\left(\frac{d_0}{d}\right)$

$$\begin{array}{c} V \\ | \\ \boxed{d_0} \\ | \\ 0 \end{array} \rightarrow \begin{array}{c} V \\ | \\ \boxed{d} \\ | \\ 0 \end{array}$$

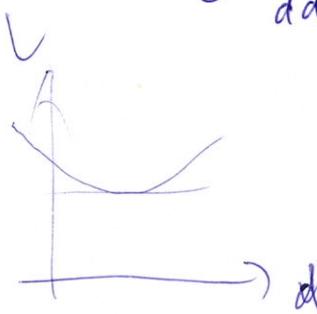
↑ young's modulus

$$\Rightarrow \frac{1}{2} \epsilon_0 \epsilon_r \left(\frac{V}{d}\right)^2 = Y \ln\left(\frac{d_0}{d}\right)$$

$$V^2 = \frac{2Y}{\epsilon_0 \epsilon_r} d^2 \ln\left(\frac{d_0}{d}\right)$$

$$\text{d}V \frac{d}{dd} : 2V \cdot \frac{dV}{dd} = \frac{4Y}{3\epsilon_0 \epsilon_r} d \ln\left(\frac{d_0}{d}\right) + \frac{2Y}{3\epsilon_0 \epsilon_r} d^2 \cdot \frac{d}{d_0} \left(-\frac{d_0}{d^2}\right)$$

$$= \frac{2Y}{3\epsilon_0 \epsilon_r} \left[ 2d \ln\left(\frac{d_0}{d}\right) - d \right]$$



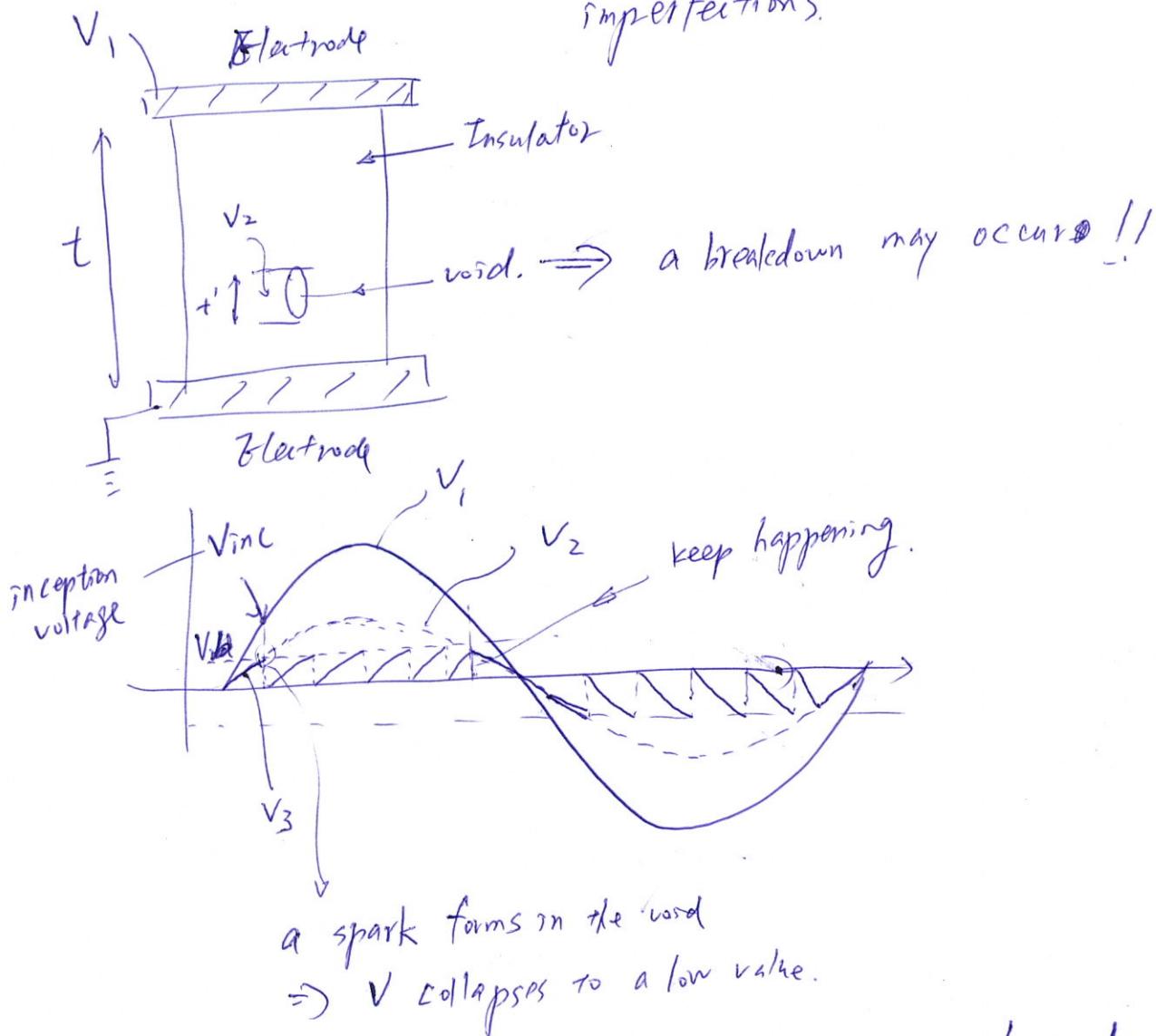
$$\Rightarrow \ln\left(\frac{d_0}{d}\right) > 10.5 \Rightarrow d = d_0 e^{-0.5} = \underline{0.6 d_0}$$

\* If  $V \uparrow \Rightarrow d \downarrow \Rightarrow$  exceeds the strength of the material  
 $\Rightarrow$  mechanical damage.

### 3 Partial discharges (PD)

16

- A PD occurs inside voids embedded in solid dielectrics.



$V_b$  is determined by the Paschen curve where  $d = t'$ ,  $p$  is  $p$  in the void.

- The energy dissipated in the void causes erosion, tracking, treeing and electrochemical deterioration.
- It takes a time period of years.

## 3) Electrical Trees

- dry trees
- water trees

- depends on the properties of dielectric & the environment.

- Over a period of time, may extend to few years, the trees cause the total breakdown.

\* Dry trees: - hollow tubes, resembling the branches of trees, which are formed inside a dielectric due to electrical stress & filled w/

- diameters:  $10 \sim 500 \mu\text{m}$ , mixtures of gases from the decomposition of dielectric material.

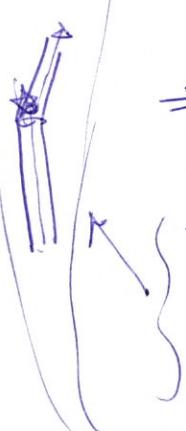
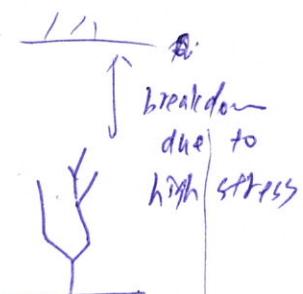
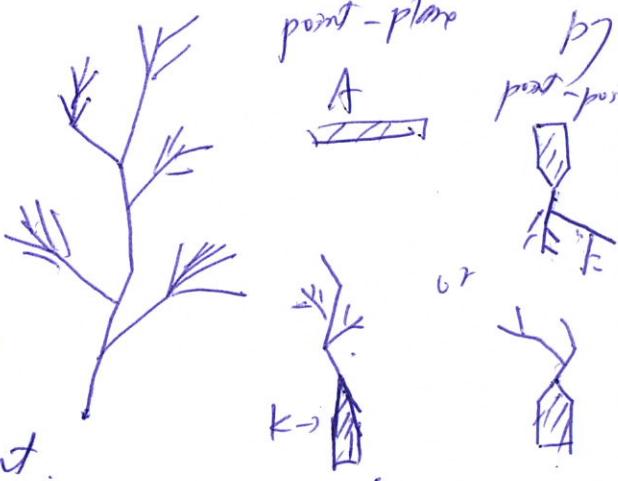
11 \* - Nucleation sites (seed): - localized field enhancements, ex: asperities on electrodes, embedded foreign particles.

- Initiation: Mostly due to electromechanical force  $\rightarrow$  voids, microscopic cracks,

$\Rightarrow$  cause erosion, tracking, gas evolution, decomposed products.

- The accelerated charged particles impact the walls of the cavities w/ high velocities, leading to their growth

- When a tree occupy a major length of the insulator, the remaining unbridged portion of the insulator will be subjected to extremely high stresses, leading to disruptive breakdown



## \* Water Trees

178

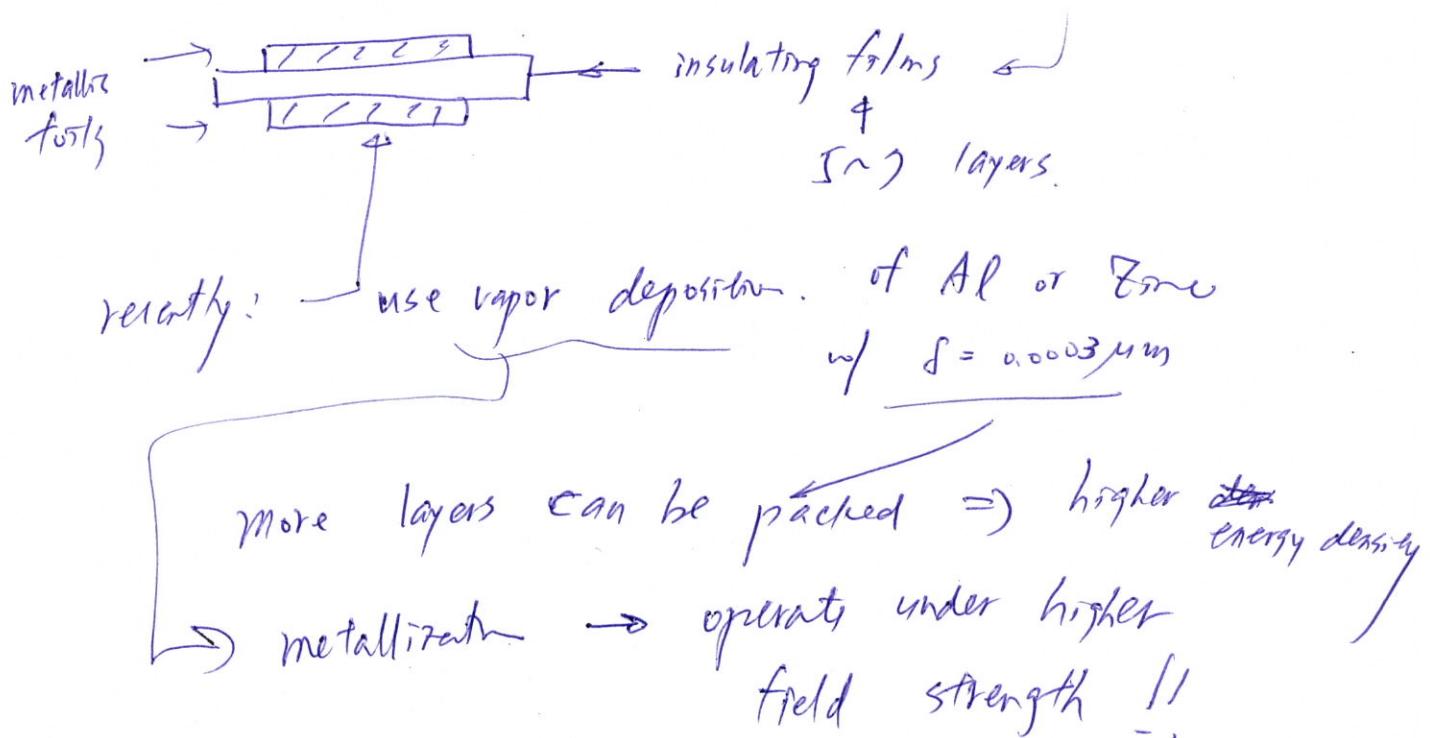
- If dielectric is hydrophilic (親水) & is immersed in water  $\rightarrow$  tree channels filled w/ water.
- When electric stress is removed, water is reabsorbed in the solid dielectric. The channel becomes dry & hollow.
- The electrical conductivity of water ~~is~~ trees compared to dry trees is high  
 $\Rightarrow$  rapid growth.  
underground cable !!

## ? Methods of improving solid insulator performance.

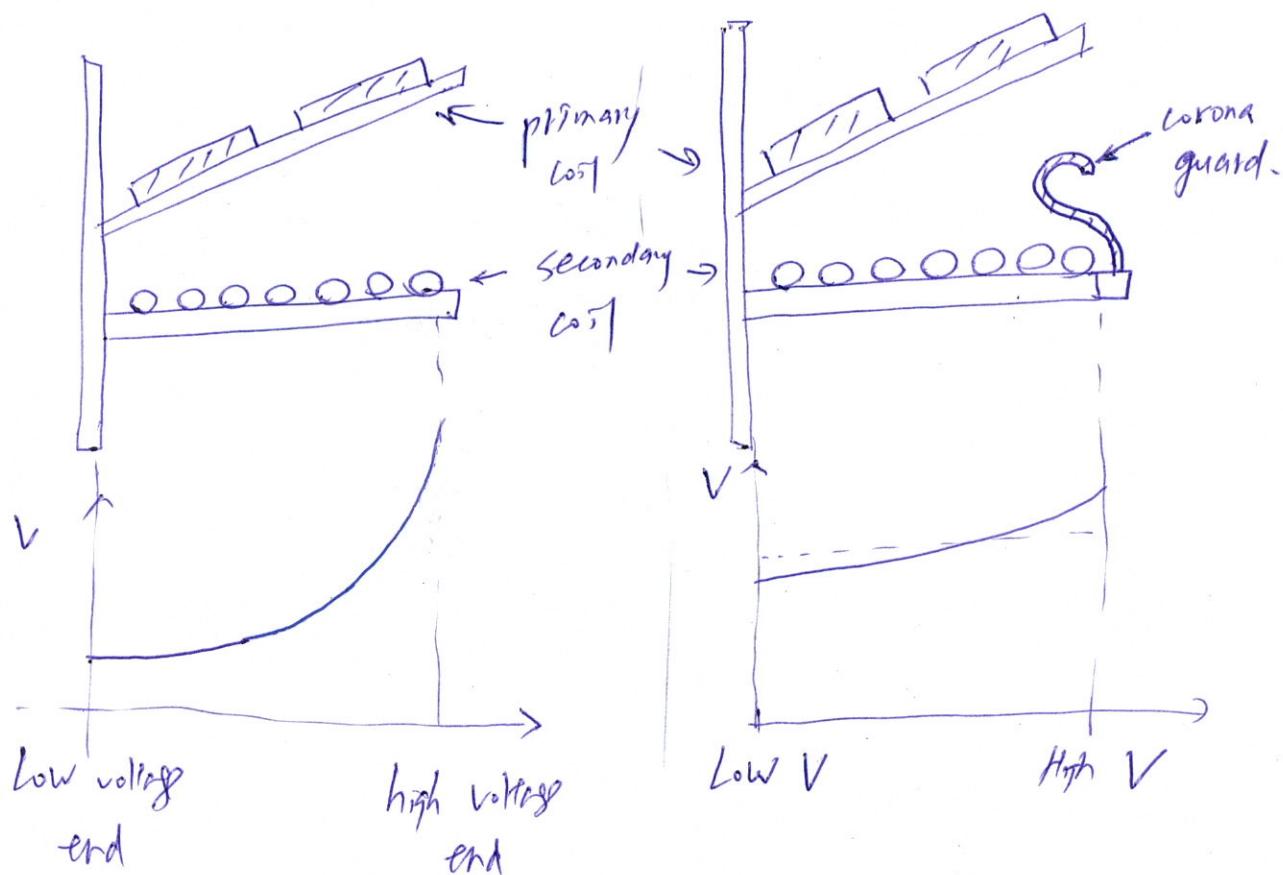
- layers of insulating films instead of single layer w/ the same thickness
- improving the contact area @ the interface between electrodes & dielectric - metallization & oil impregnation
- controlling a nonuniform field - corona guards / equipotential rings
- modifying insulator shapes & surface profiles.  
 $\rightarrow$  reduce the interaction of charge carriers at the surface.

## Six: - Insulation in energy storage capacitors

p9

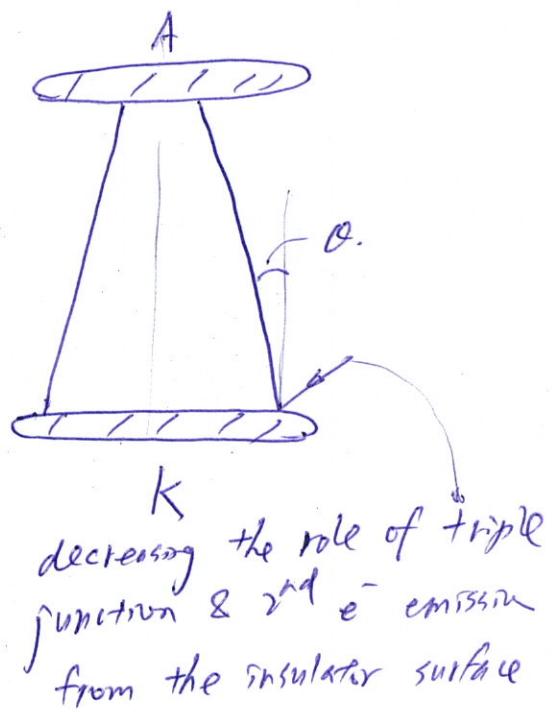
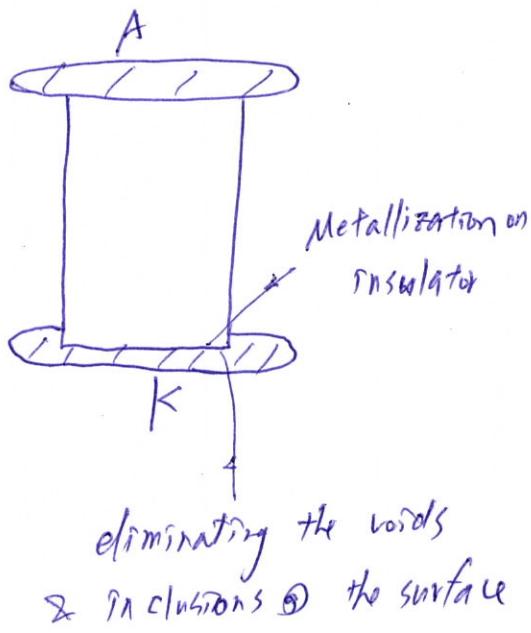
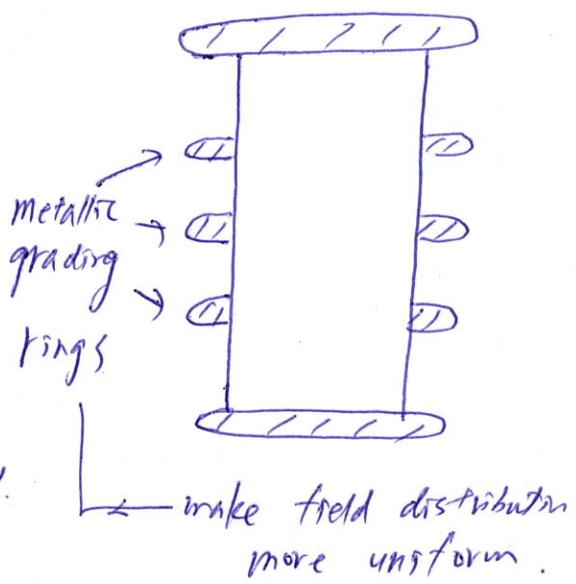
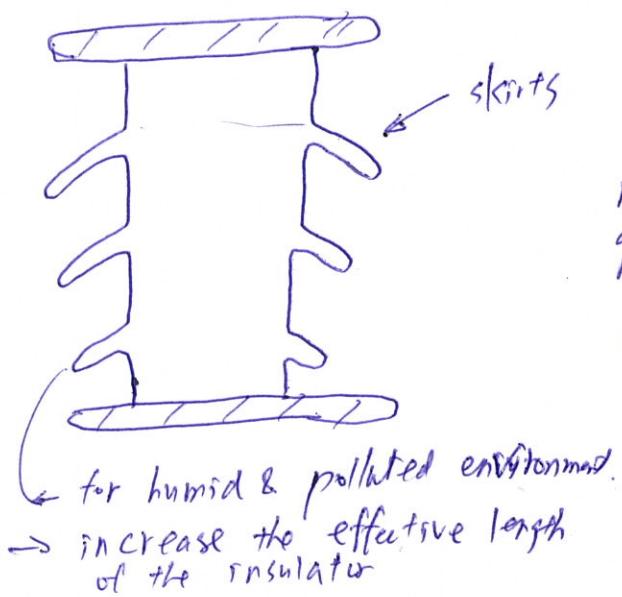


## - Surge voltage distribution in a Tesla Transformer

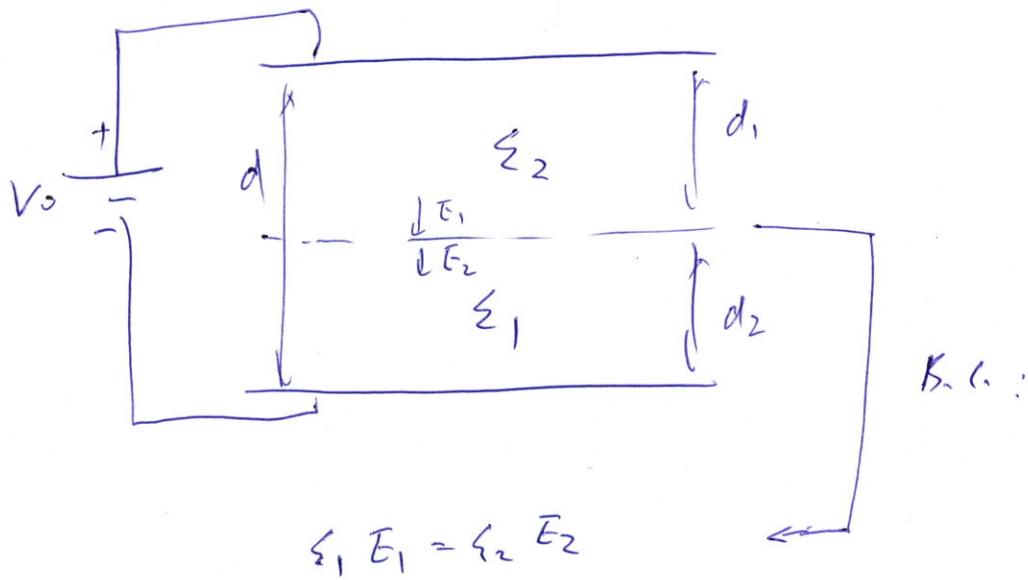


# Surface flashover in standoff insulators

pro



### 3 Composite dielectrics:



$$E_1 = \frac{V_1}{d_1}, \quad E_2 = \frac{V_2}{d_2}$$

$$\left[ \begin{array}{l} \epsilon_1 \frac{V_1}{d_1} = \epsilon_2 \frac{V_2}{d_2} \\ \Rightarrow V_1 = \frac{\epsilon_2}{\epsilon_1} \frac{d_1}{d_2} V_2 \end{array} \right] \quad V_0 = V_1 + V_2$$

$$V_0 = \frac{\epsilon_2}{\epsilon_1} \frac{d_1}{d_2} V_2 + V_2 = \frac{\epsilon_2 d_1 + \epsilon_1 d_2}{\epsilon_1 d_2} V_2$$

$$V_2 = V_0 - \frac{\epsilon_1 d_2}{\epsilon_2 d_1 + \epsilon_1 d_2} \quad E_0 = \frac{V_0}{d}$$

$$\left\{ \begin{array}{l} E_2 = \frac{\epsilon_1}{\epsilon_2 d_1 + \epsilon_1 d_2} V_0 = \frac{1}{d_2 + \frac{\epsilon_1}{\epsilon_2} d_1} V_0 \\ E_1 = \frac{\epsilon_2}{\epsilon_1} E_2 = \frac{\epsilon_2}{\epsilon_2 d_1 + \epsilon_1 d_2} V_0 = \frac{1}{d_1 + \frac{\epsilon_2}{\epsilon_1} d_2} V_0 \end{array} \right.$$

$$\text{if } \frac{\epsilon_2}{\epsilon_1} > 1 \quad d_1 + \frac{\epsilon_1}{\epsilon_2} d_2 < d_1 + d_2 = d$$

$$\Rightarrow \underline{E_1 > E_0}$$

## 3. Liquids

p11

- "All-liquid" pulsed-power system is feasible.

Ex: Oil-filled Marx - oil/water-filled PTL  
- oil or water spark gap

Marx: high dielectric strength

PTL: - - - +  
high dielectric constant +  
low conductivity

Spark gap: - - - +  
high thermal conductivity +  
minimum decomposition products +  
self-healing properties.

- Properties:
1. good thermal properties.
  2. low viscosity.
  3. low flammability
  4. good chemical & thermal stability
  5. ~~good~~ works in low temperature
  6. environmental considerations
  7. low cost.

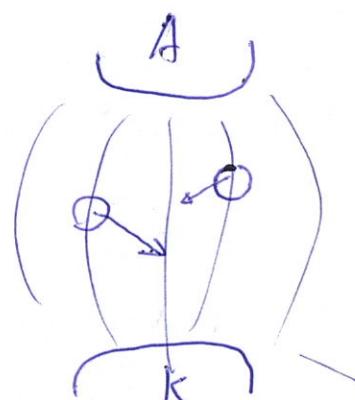
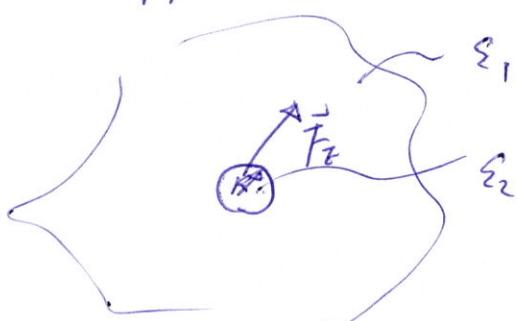
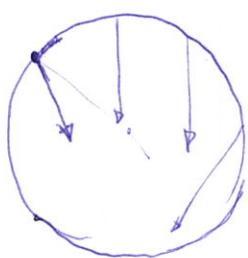
prc

\* Breakdown in liquid:

- particle alignment.
- electrons breakdown.
- streamers in bubbles.

\* particle alignment - solid impurities always exists in a liquid

- convection currents are set up in a liquid dielectric due to particle movements even at low applied voltage.



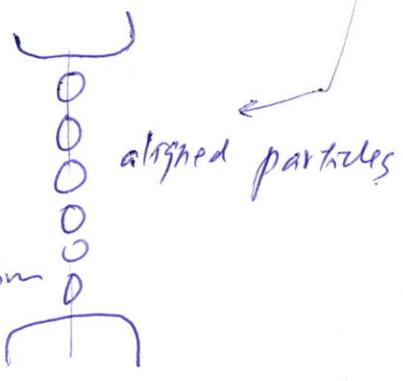
$$\vec{F}_E = \frac{\epsilon_2 - \epsilon_1}{\epsilon_1 + 2\epsilon_2} \cdot R^3 (\vec{E} \cdot \nabla \vec{E})$$

- The ~~attractive~~ force tends to concentrate the solid impurities to the region of the center of the electrodes where the field is fairly uniform.



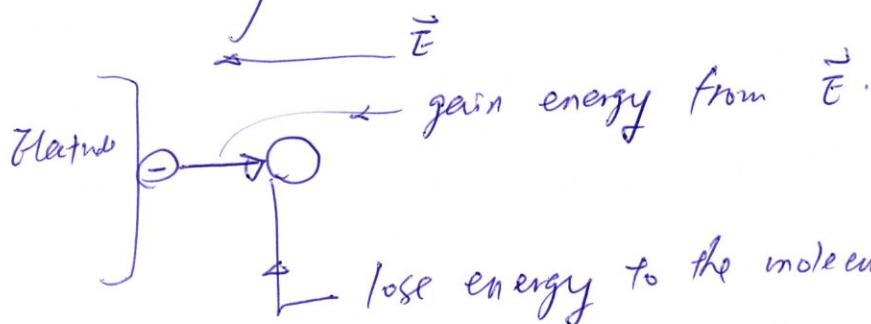
- $\vec{F}_D$  - diffusion force.

If  $\vec{F}_E > \vec{F}_D$ , the alignment of the particles takes place along the center of the electrode and breakdown in the liquid takes place along the aligned particles.



\* Electron. breakdown.

- very similar to breakdown in gas.



- elastic, vibration, excitation process

$\rightarrow$  At elevated temperatures & high field strength near an asperity of an electrode.

$\rightarrow$  energy loss  $\downarrow$ .

$\Rightarrow$  continuous acceleration

$\Rightarrow$  energy  $>$  ionization energy.

$\Rightarrow$  more  $e^-$  due to impact ionization of the molecule

$\Rightarrow$  avalanche of  $e^- \Rightarrow$  breakdown.

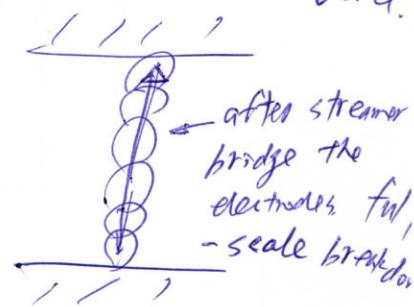
\* Streamers in bubbles - propagation of streamers in the low-density vapor or bubble

the process is very similar to that in gases

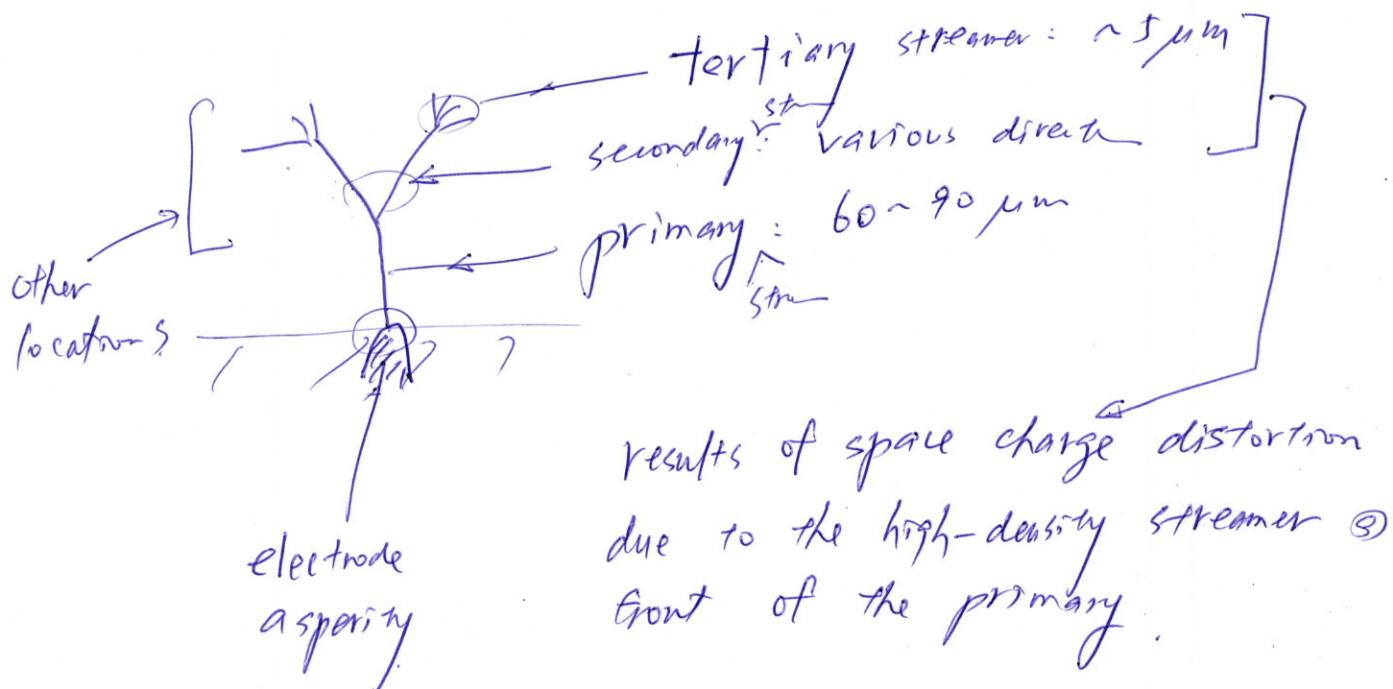
$\Rightarrow$  streamer mechanism of liquid breakdown is similar to the growth of electric trees in a solid due to discharge in a void.

low-density vapor

high field due to space charge  $\Rightarrow$  shockwave & thermal dissipation  
 $\Rightarrow$  more low-density vapor.  
 $\Rightarrow$  more ionization



## Structure.



- Effect of hydrostatic pressure:

- breakdown voltage  $\nabla$  w/  $P \uparrow$

~~streamer~~  
streamer grow at higher field  $\vartheta P \uparrow$

Ex: transformer oil,  $V_{break} \times 3 \approx 4 \vartheta 4 \text{ MPa}$

Mechanisms of bubble formation.

( $\sim 40 \text{ atm}$ )

(1) foreign particles

(2) asperities on electrode causing field emission.

(3) chemical interaction w/ molecules causing their dissociation.

(4) release of the already existing gas dissolved in the liquid.

- Krasnick's hypothesis:

- a vapor bubble grew continuously & when a critical size was reached.  
→ breakdown ~~takes~~ place.

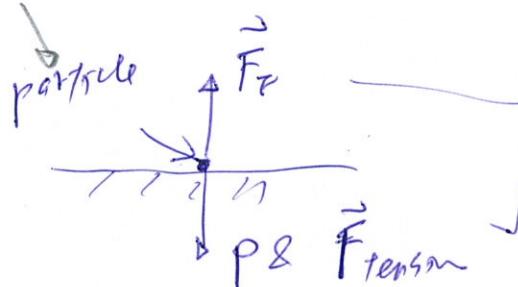
~~when~~ when  $V$  is gone → collapse faster than air bubble

⇒  $p$  inside the bubble is "Zero"

- w/ impurity particle → bubble grows preferentially on the particles

→ near the electrode surface.

seed of bubble



balance ⇒ causes a zero pressure

-  $V_b \uparrow$  as  $r_b \uparrow$

$r_b$  of particle

$\gamma_s \uparrow$  surface tension

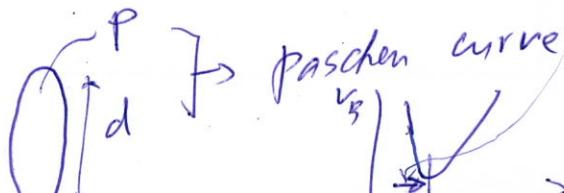
$P \uparrow$  hydrostatic pressure

- Kao's hypothesis:

- bubble once created starts elongating in the direction of the field. keeping its volume const.

$$P \uparrow \Rightarrow r \downarrow$$

$$\Rightarrow V_F \uparrow$$



Breakdown  $d$

~~DB + D + N~~

\* Sharbaugh & Watson hypothesis



$\Rightarrow$  asperity of  $K \Rightarrow$  field emission  $\uparrow$

$\Rightarrow$  high current

$\because \lambda$  is short

$\therefore$  energy deposited in small region.

$\Rightarrow$  low-density vapor locally

$\Rightarrow$  breakdown in the bubble

For a pulse w/ few  $\mu s \Rightarrow$  enough energy from  
field emission to vaporize a small mass of liquid.  
ahead of an asperity into a bubble

$P \uparrow \Rightarrow$  boiling point  $T_b \uparrow$

$\Rightarrow$  more field is required to form the  
bubble.

( $\epsilon_r = 80$ )

\* Water:

① high energy density. in energy storage

② low impedance in PFL

③ self-healing post breakdown

④ easy maintenance.

⑤ low cost

⑥ ease of disposal

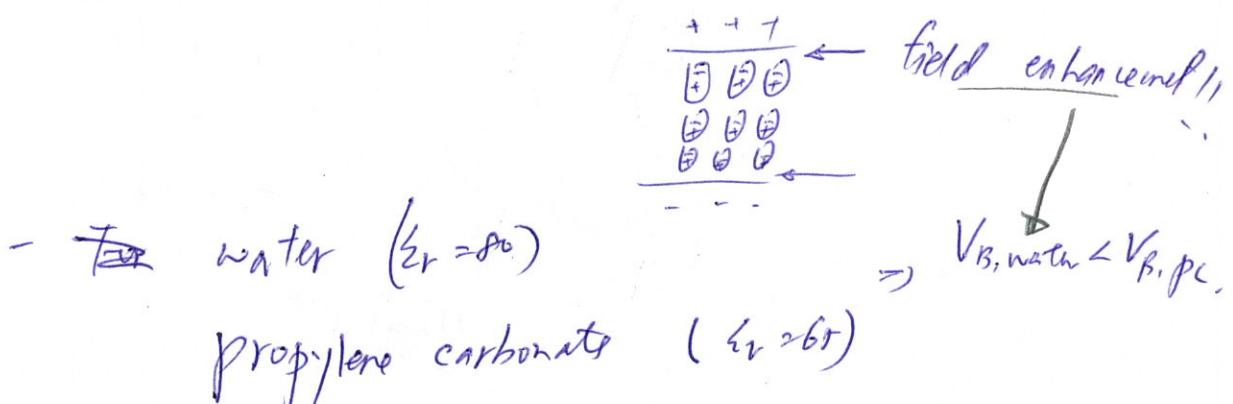
- for pulse w/ short duration ( $1\text{-}3\text{ ns}$ )  
 submega volt . , the E field strength  
 is  $\approx \times 2$  for longer p duration ( $10\text{ ns}^{\text{ns}}$ ),

$3 \times 10^7 \text{ V/m}$  for  $\mu\text{s}$  electric stress

- dependance of breakdown voltage on Polarity ()

- E field intensification.

- enhanced field intensification at the aperitres  
 due to collector orientation of the bipolar  
 water molecules ③ liquid-electrode interface



- ~~water~~ water ( $\epsilon_r = 80$ )

propylene carbonate ( $\epsilon_r = 65$ )

- \* Methods of improving liq. dielectric performance.

- New composition:

In PFL: (vegetable oil): castor oil ( $\epsilon_r = 4.7$ )  
 v.s. mineral oil ( $\epsilon_r = 2.4$ )

sealing is  $\leftarrow$  hygroscopic - (absorb),  
 important.

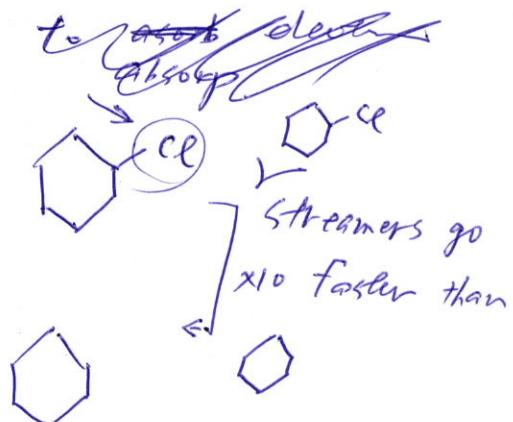
Synthetic oil e.g. PAO (poly-alpha-olefin),  
 a silicone oil → good for closing SW.  
 1) resistance to oxidation.  
 2) lower viscosity, ok @ low temp  
 3) good lubrication, ok w/ hydraulic pump  
 forced flow @ high P & velocity  
 removes the gases evolved by molecular  
 dissociation & erosion from electrodes

- Electron Scavengers - ~~to absorb electrons~~

w: chloro cyclohexane.

v.s

cyclohexane



or addy  $\text{CCl}_4$ , more streamer !! (?)

$\therefore$  detrappling of  $e^-$  @ high field

- Liquid mixture.

gas:  $\text{SF}_6 + \text{N}_2$

solid: paper + polypropylene.

liquid: In PFL: water ( $\epsilon_r = 80$ )

+

ethylene glycol ( $\epsilon_r = 60$ )

$\Rightarrow$  increasing intrinsic time const.

## \* Impregnation

when putting insulating films & metallic foils in liquid dielectric:

① ② high temperature  $\Rightarrow$  removal of air

③ ④ vacuum trapped ⑤  
electrode-liquid interface

## - Purification

- freed of foreign particles & ions  
 $\Rightarrow$  filter  $\Rightarrow$  deionizer.

- low temperature  $\rightarrow$  R.F.  
 $\hookrightarrow$  chiller unit.

3

## Vacuum

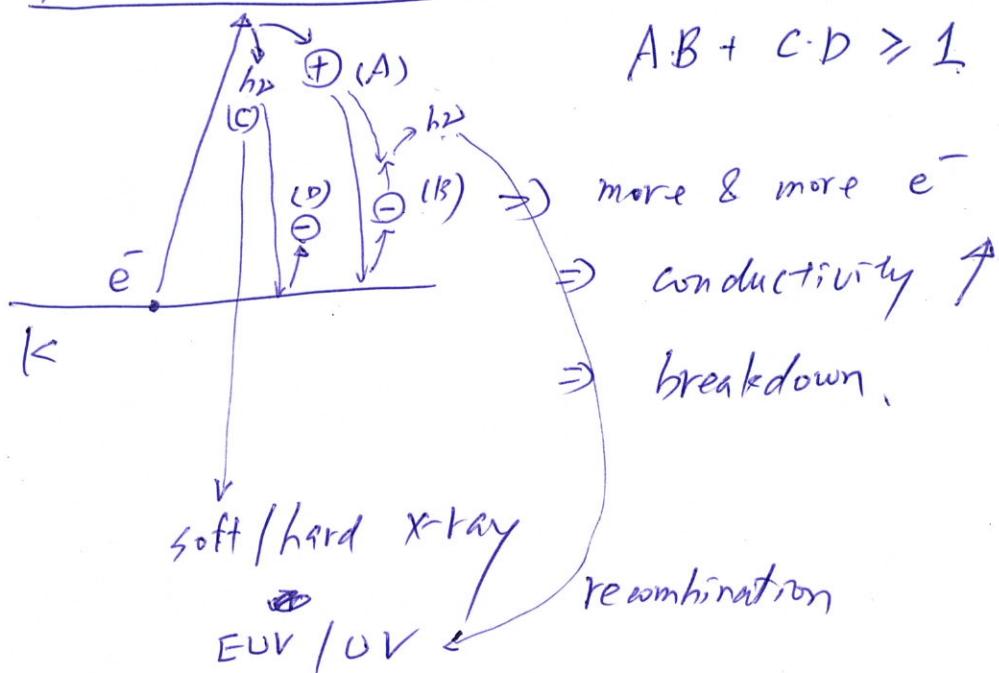
- No medium  $\rightarrow$  NO breakdown, however
- breakdown does take place  $\because$  charge ~~particles~~  
carriers being injected  
 $\Rightarrow$  desorbed gas, metal vapors from the electrode
- "Surface flashover" across the solid insulator;  
the insulator surface is an electrically weaker

- Ex: ① spark gap switches medium than vacuum
- ② diodes for particle beams, X-rays, microwaves
- ③ transmission lines for feeding pulsed power into the load.

### 3) Vacuum breakdown mechanisms.

- for  $pd < 10^{-3}$  Torr cm  $\rightarrow e^-$  cross the gap w/o colliding.
- however:
- \* ABCD mechanism

A



- \* high ③ large impulse field intensity:
  - 1) high gas evolution from electrolyte
  - 2) metal vapor formation
  - 3) unfavorable μ-injection geometry
- \* field emission - insolated breakdown

Fowler-Nordheim (F-N) field emission formula

$$j_c = C_1 E_p^2 e^{-C_2/E_p} \frac{A}{cm^2}$$

$$\frac{1.58 \times 10^{-6}}{6.83 \times 10^2 \cdot \varphi^{3/2} \mu ly} \quad y = 3.79 \times 10^5 \cdot \frac{\sqrt{E}}{\varphi}$$

wave func.  $\rightarrow \Psi t^2 ly$

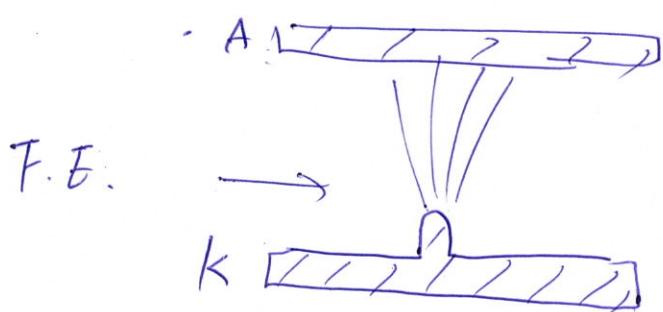
120

① for  $E_p = 10^6 - 10^8 \text{ V/cm}$

$$j_c = 10^8 - 10^{10} \text{ A/cm}^2$$

$\rightarrow$  leads to ABCD breakdown  
or other

- ②  $j_c \rightarrow$  joule heating of  $\varnothing$  microprojection  
 $\rightarrow$  melting, vaporization, plasma forming  
 $\downarrow$   
 ionizat  $\rightarrow$  breakdown.
- ③ high-energy e beam on anode  
 $\rightarrow$  heating  $\rightarrow$  metal vapor



- ④ low work function for K  $\rightarrow$  high field emission

### \* Microparticle-initiated breakdown

- ①   
loosely adhering material  $\hookrightarrow$  being detached from electrode due to electrostatic force
- ② microprojections, made soft from joule heating by field emission
- ③ vaporizata of anode by field emisn
- ④ ——— Cathode

( $\rightarrow$  plasma flare - initiator Breitlow.) pg

## 3 Improving vacuum insulation performance

### - Conditioning:

~~conditioned breakdown~~

w/ successive breakdown events, the breakdown voltage steadily increases ~~until~~ and attains a steady value

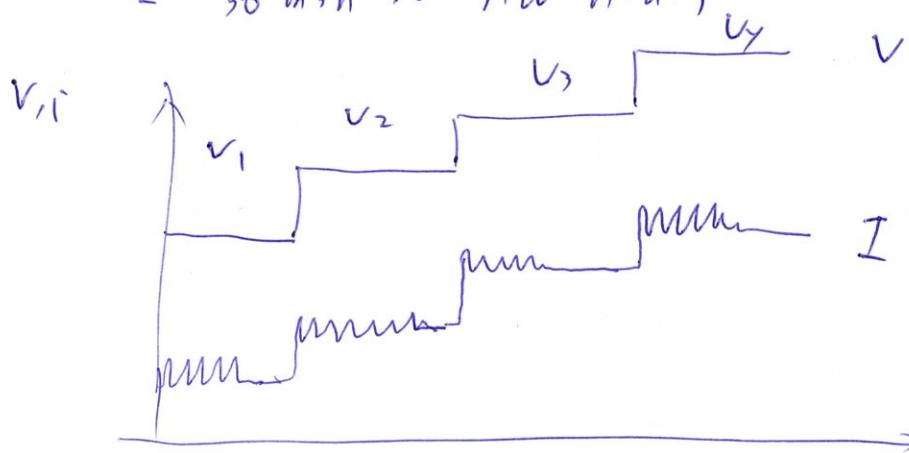
### ~~Current~~ conditioning:

~~current~~

-  $I \sim 100 \mu A$

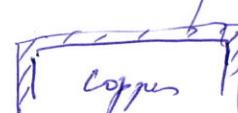
- A breakdown pulse removes a microprojection and the following pulse shifts to another microprojection site.

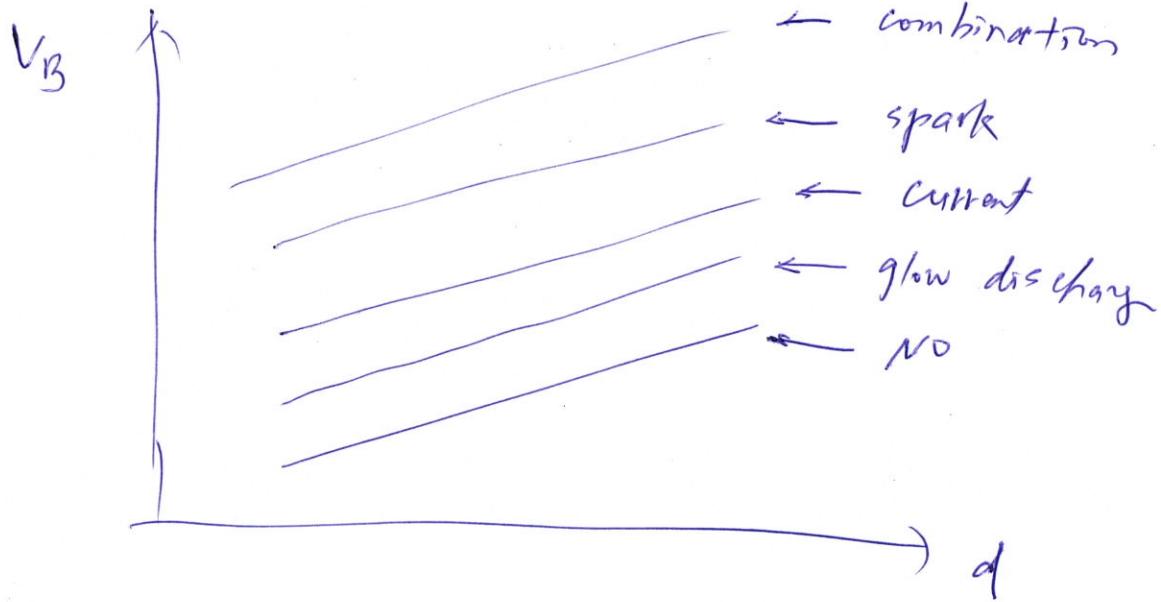
- 30 min ~ few hours



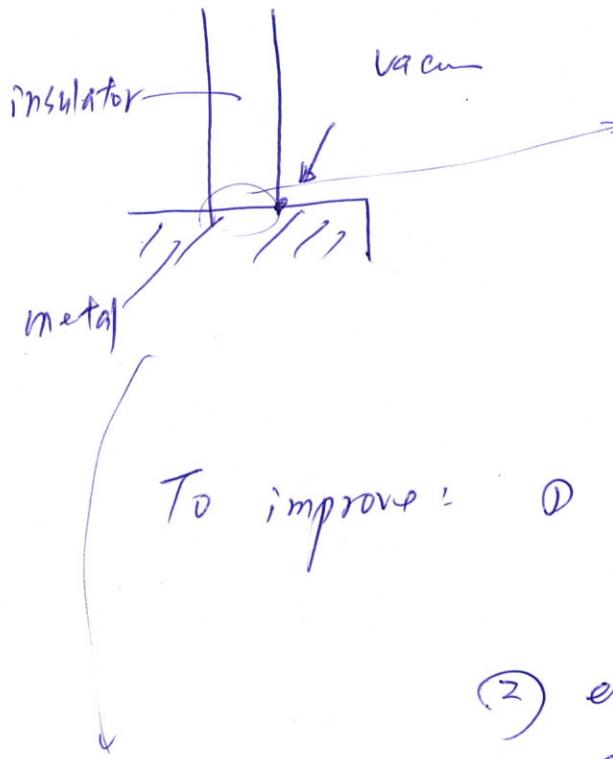
- AC / DC , start from 50% of expected  
 $V_b$ .  
for both electrode.

- \* spark conditioning
  - Impulse voltages w/ width of 100s NS is used,  
 $I \leq \text{few A}$ .
  - chemical cleaning
    - reducing impurities
    - Valence band e<sup>-</sup> energy  
is changed
  - residual stresses are changed → hardened.  
 $\uparrow$   
 work
- \* glow discharge cleaning.
  - H, He, Ar, N<sub>2</sub>, SF<sub>6</sub>, dry air
  - sputter-cleaning
  - a continuous flow of gas allowed the removal  
of impurities
  - 30-60 mins using  $\downarrow$ , then use Ar to remove  
O<sub>2</sub>
- \* Outgassing & annealing
  - heat to  $T = 250 \sim 1500^\circ\text{C}$  for several hours  
for outgassing.
- \* surface treatment & coating
  - cobalt-molybdenum 钴钼
  - cobalt-tungsten 钴钨
  - ion implantation → work hardening of the surface

$\uparrow$   
 'mon coating'  




### 3 Triple-Point Junction Modifications

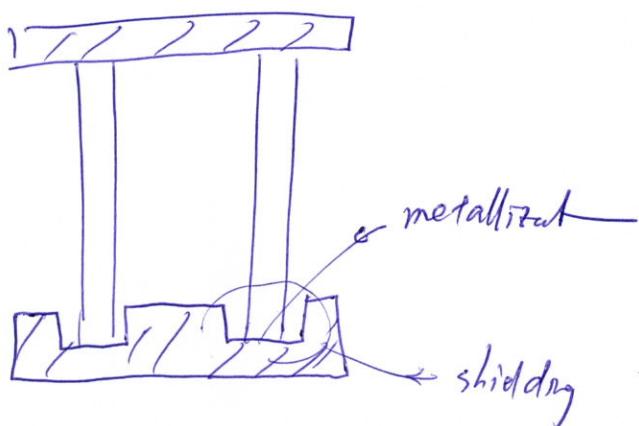


If imperfect  
 $\Rightarrow$  a void or a gap results  
 $\Rightarrow$  field enhancement  
 $\Rightarrow$  enhanced field emission

To improve:

- ① metallizing the insulator surface
- ② contact  $\Rightarrow$  a firm contact.

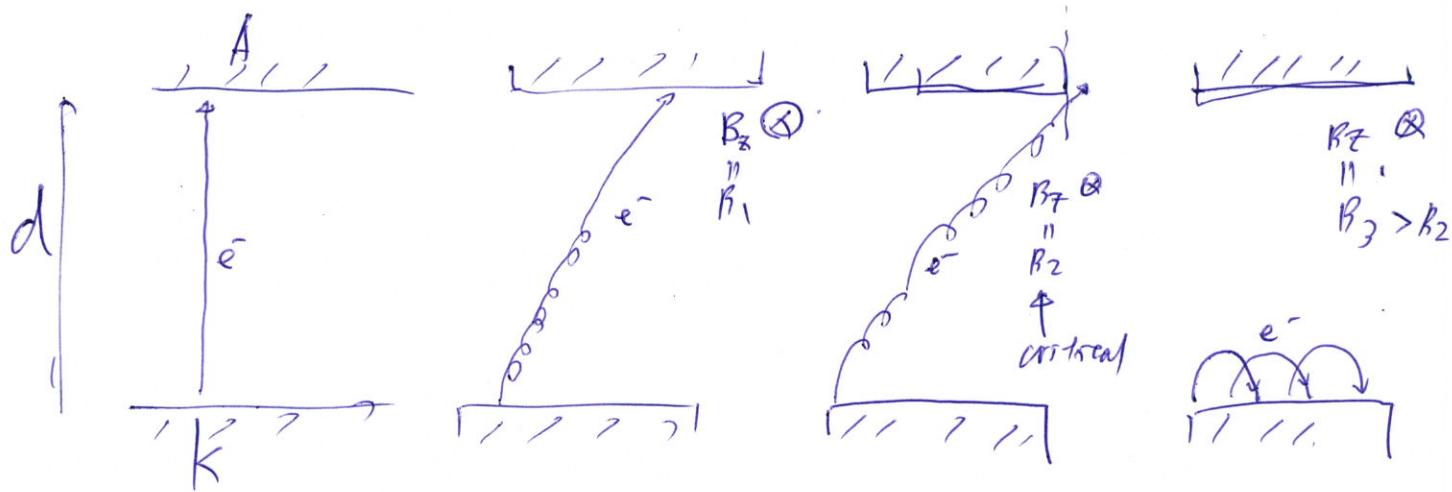
② elimination of the void and the shielding of the emitted area by  $K_{II}$



Anode doesn't help

## 3. Vacuum magnetic insulation

by



- the crossed B field can be externally applied.

but also self-generated

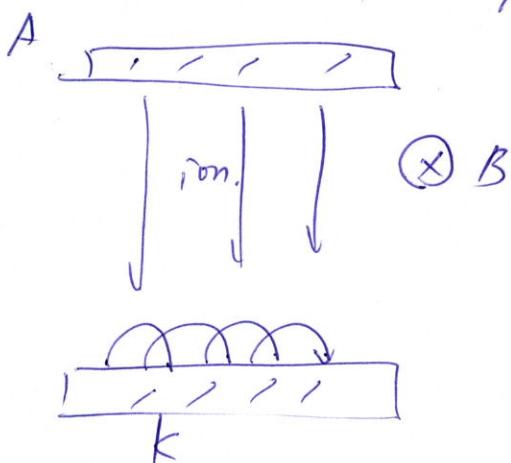
⇒ magnetic insulation transmission line (MITL)

----- insulated line oscillator (MILO)

high power  
μ wave source.

- For diode

$$m_i > m_e$$

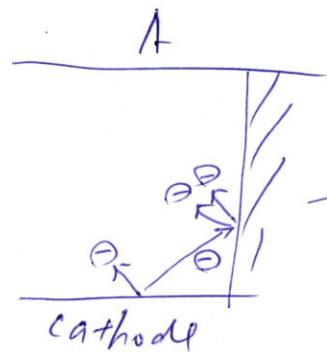


### 3 Surface flashover across solid in Vacuum

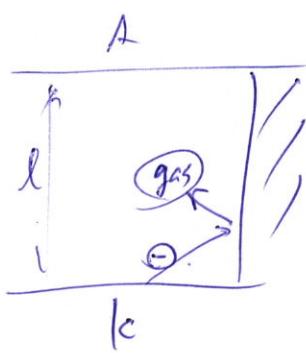
137

- $V_B \nrightarrow$  rapidly @ low  $p$  : lack of ionizing collisions partners

→ surface flashover



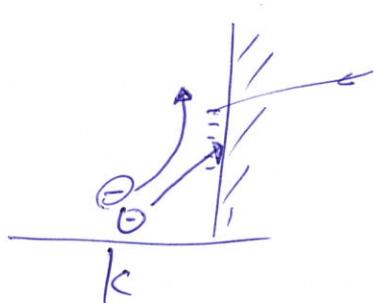
→ The dielectric surface is the source of electrons to feed the developing avalanche by a process known as 2<sup>nd</sup> e<sup>-</sup> emission.



→ electron-stimulated desorption.  
e<sup>-</sup> impacting the surface liberates gas trapped or adsorbed by the surface.

→ 2<sup>nd</sup> e<sup>-</sup> emission from dielectric surface

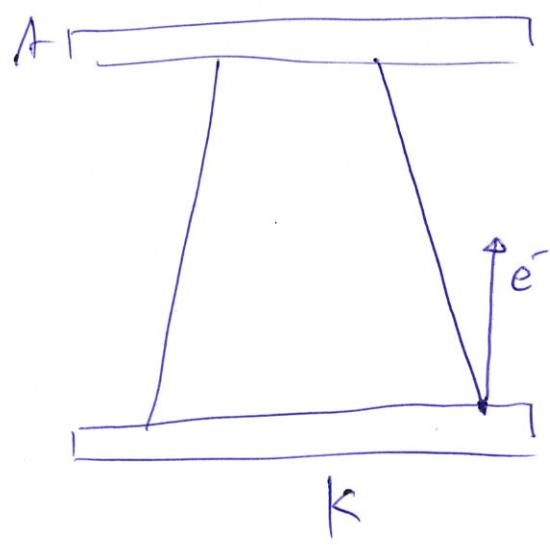
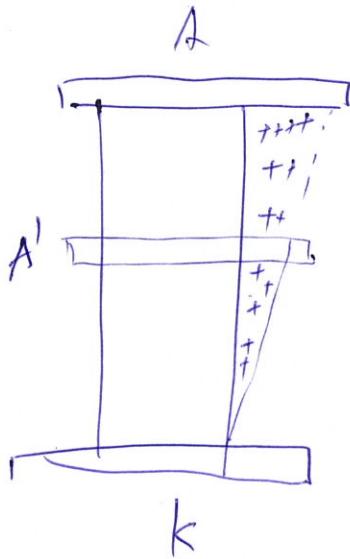
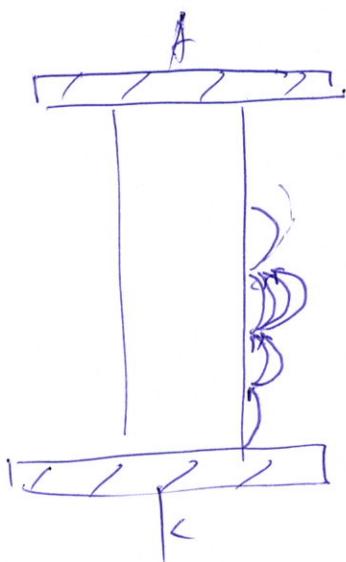
$$E_{lc} > E_0 \rightarrow \text{to liberate } e^-$$



If  $E_{lc} < E_0$ , charge builds up causing the following e<sup>-</sup> away from the surface using more energy

$$\Rightarrow E_{lc} \geq E_0 \rightarrow \text{generating more } e^-$$

$$V_B \propto \sqrt{l}$$



← to improve  $V_B'$   
or higher value of  
 $E_0$  → less e-  
generate