

Introduction to Nuclear Fusion as An Energy Source



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Lecture 8

2025 spring semester

Tuesday 9:00-12:00

Materials:

<https://capst.ncku.edu.tw/PGS/index.php/teaching/>

Online courses:

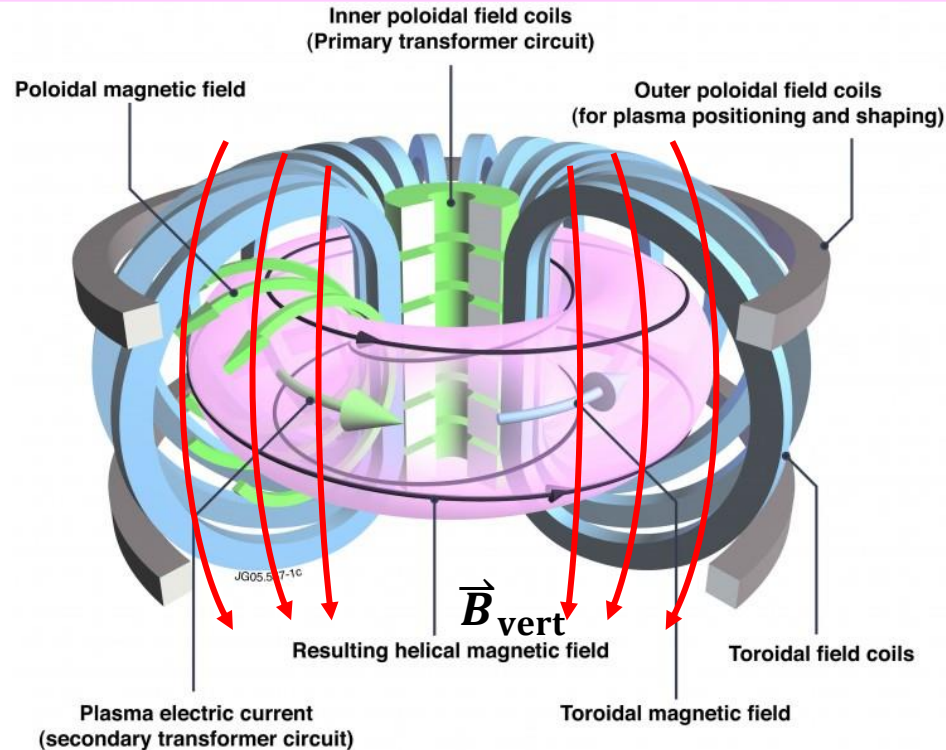
<https://nckucc.webex.com/nckucc/j.php?MTID=mf1a33a5dab5eb71de9da4380ae888592>

Course Outline



- **Magnetic confinement fusion (MCF)**
 - Gyro motion, MHD
 - 1D equilibrium (z pinch, theta pinch)
 - Drift: ExB drift, grad B drift, and curvature B drift
 - Tokamak, Stellarator (toroidal field, poloidal field)
 - Magnetic flux surface
 - 2D axisymmetric equilibrium of a torus plasma: Grad-Shafranov equation.
 - Stability (Kink instability, sausage instability, Safety factor Q)
 - Central-solenoid (CS) start-up (discharge) and current drive
 - CS-free current drive: electron cyclotron current drive, bootstrap current.
 - Auxiliary Heating: ECRH, Ohmic heating, Neutral beam injection.

Coils in a tokamak



- Toroidal field coils (in poloidal direction) – generate toroidal field for confinement.
- Poloidal field coils – generate vertical field for plasma positioning and shaping.
- Central solenoid – for breakdown and generating plasma current (in toroidal direction) and thus generating poloidal field for confinement.

Plasma condition can be obtained by solving Grad-Shafranov equation



$$\Delta^* \psi = -\mu_0 R^2 \frac{dp}{d\psi} - \frac{1}{2} \frac{dF^2}{d\psi} \quad \text{where } \Delta^* \psi = R^2 \nabla \cdot \left(\frac{\nabla \psi}{R^2} \right)$$

- The usual strategy to solve the Grad-Shafranov equation:
 1. Specify two free functions, the plasma pressure $p = p(\psi)$ and the toroidal field function $F = F(\psi)$.
 2. Solve the equation with specified boundary conditions to determine the flux function $\psi(R, z)$.

3. Calculation the magnetic field using the following equations:

$$B_R = -\frac{1}{R} \frac{\partial \psi}{\partial z} \quad B_\phi = \frac{F(\psi)}{R} \quad B_z = \frac{1}{R} \frac{\partial \psi}{\partial R}$$

4. The pressure profile can then be obtained from $p = p(\psi(R, z))$.

Application of solving Grad-Shafranov equation for designing a tokamak



- Given I_{plasma} , $p(\psi)$, $I(\psi)$, I_{coils} , free boundary of plasma, perfect conductor as the chamber.
- Given I_{plasma} , $p(\psi)$, $I(\psi)$, I_{coils} , free boundary of plasma, insulator chamber.
- Given I_{plasma} , $p(\psi)$, $I(\psi)$, I_{coils} , free boundary of plasma, chamber with eddy current.
- Given I_{plasma} , $p(\psi)$, $I(\psi)$, fixed boundary of plasma. Then, use I_{coils} , free boundary of plasma and match the plasma shape calculated in the fixed boundary condition.

$$\Delta^* \psi = -\mu_0 R^2 \frac{dp}{d\psi} - \frac{1}{2} \frac{dF^2}{d\psi} \quad \text{where } \Delta^* \psi = R^2 \nabla \cdot \left(\frac{\nabla \psi}{R^2} \right)$$

$$I_P = -2\pi F(\psi)$$

$$\mu_0 \vec{J} = \left(\frac{\nabla F}{R} \right) \times \hat{\phi} + \left(-\frac{1}{R} \Delta^* \psi \right) \hat{\phi} \quad \vec{B} = \left(\frac{\nabla \psi}{R} \right) \times \hat{\phi} + \frac{F(\psi)}{R} \hat{\phi}$$

Application of solving Grad-Shafranov equation for reconstructing a tokamak equilibrium state



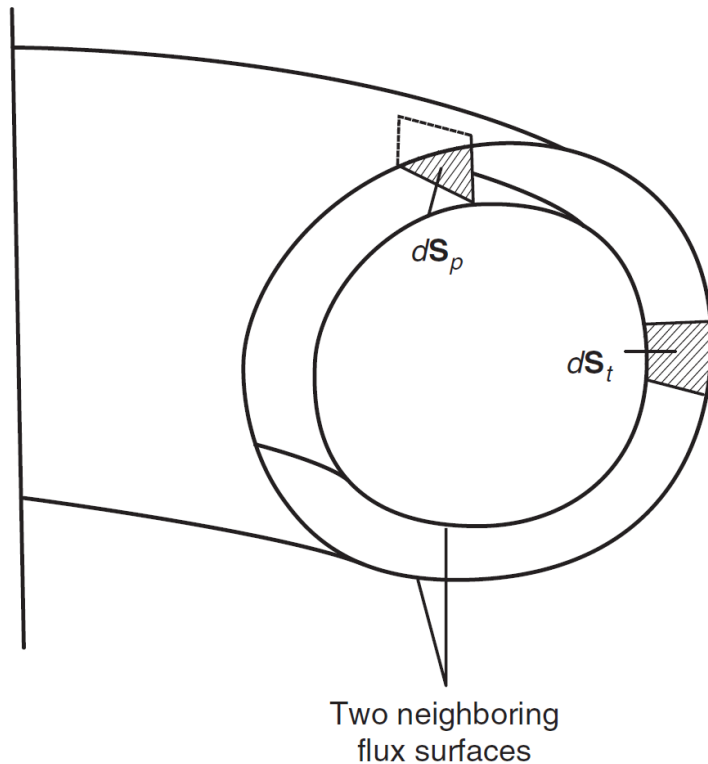
- **Measure**
 - boundary conditions, including ψ , B , etc., on the wall (using flux loop and B-dot probe).
 - Pressure.
 - Plasma current (using Rogowski coil).
- Reconstruct $\psi(r,z)$, j , $p(\psi)$, $I(\psi)$, etc.

$$\Delta^* \psi = -\mu_0 R^2 \frac{dp}{d\psi} - \frac{1}{2} \frac{dF^2}{d\psi} \quad \text{where } \Delta^* \psi = R^2 \nabla \cdot \left(\frac{\nabla \psi}{R^2} \right)$$

$$I_P = -2\pi F(\psi)$$

$$\mu_0 \vec{j} = \left(\frac{\nabla F}{R} \right) \times \hat{\phi} + \left(-\frac{1}{R} \Delta^* \psi \right) \hat{\phi} \quad \vec{B} = \left(\frac{\nabla \psi}{R} \right) \times \hat{\phi} + \frac{F(\psi)}{R} \hat{\phi}$$

Fluxes and currents



- **Poloidal flux:** $\psi_p = \int \vec{B} \cdot d\vec{S}_p$
 $\psi_p = \psi_p(p)$
- **Toroidal flux:** $\psi_t = \int \vec{B} \cdot d\vec{S}_t$
- **Poloidal current:** $I_p = \int \vec{j} \cdot d\vec{S}_p$
- **Toroidal current:** $I_t = \int \vec{j} \cdot d\vec{S}_t$

Normalized plasma pressure, β



$$\beta = \frac{\text{plasma pressure}}{\text{magnetic pressure}} = \frac{2\mu_0 \langle p \rangle}{B^2}$$

- Plasma pressure: $\langle p \rangle = \frac{1}{V_p} \int p d\vec{r}$

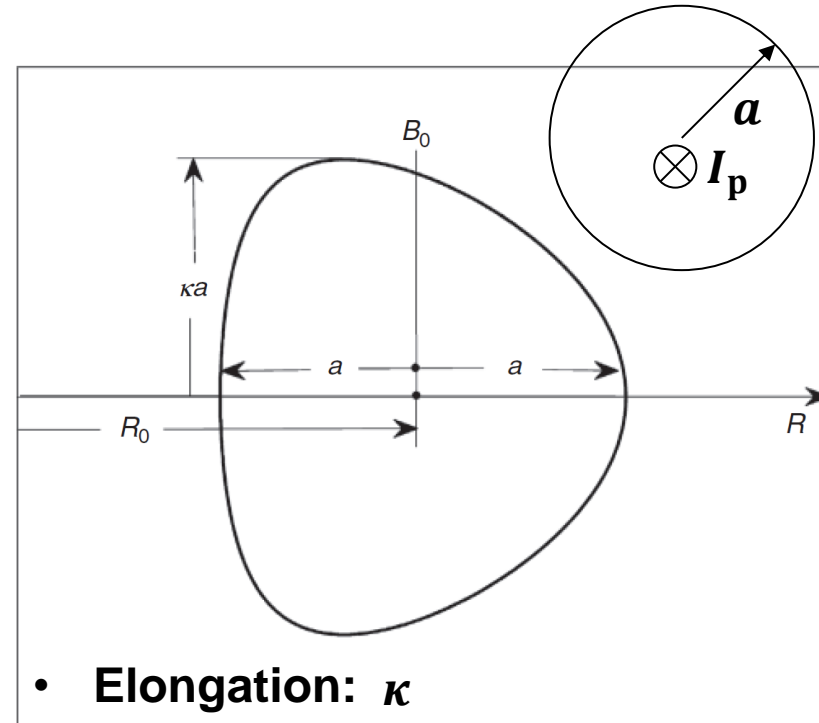
- Magnetic pressure: $P_B = \frac{B^2}{2\mu_0}$

$$B^2 = B_t^2 + B_p^2 = B_0^2 + \left(\frac{\mu_0 I_p}{2\pi a} \right)^2 \frac{2}{1 + \kappa^2}$$

$$B_t^2 = B_0^2 \quad B_0 = B @ R = R_0$$

$$B_p^2 = \left(\frac{\mu_0 I_p}{2\pi a} \right)^2 = \left(\frac{\mu_0 I_p}{C_p} \right)^2$$

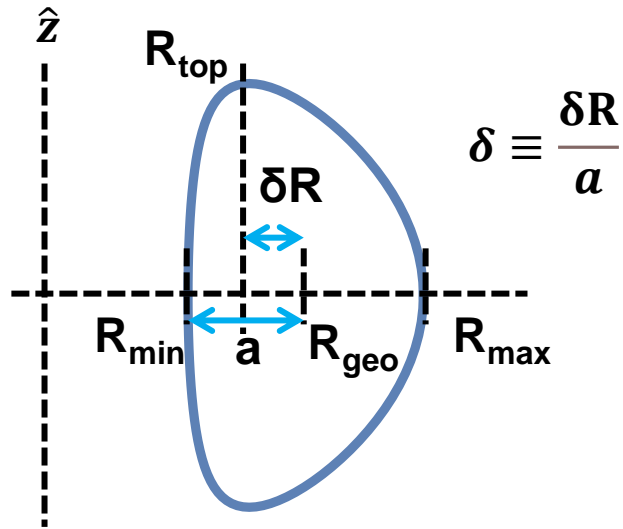
$$C_p \approx 2\pi a \sqrt{\frac{1 + \kappa^2}{2}}$$



$$\beta_t = \frac{2\mu_0 \langle p \rangle}{B_0^2} \quad \beta_p = \frac{4\pi^2 a^2 (1 + \kappa^2) p}{\mu_0 I_p^2}$$

$$\frac{1}{\beta} = \frac{1}{\beta_t} + \frac{1}{\beta_p}$$

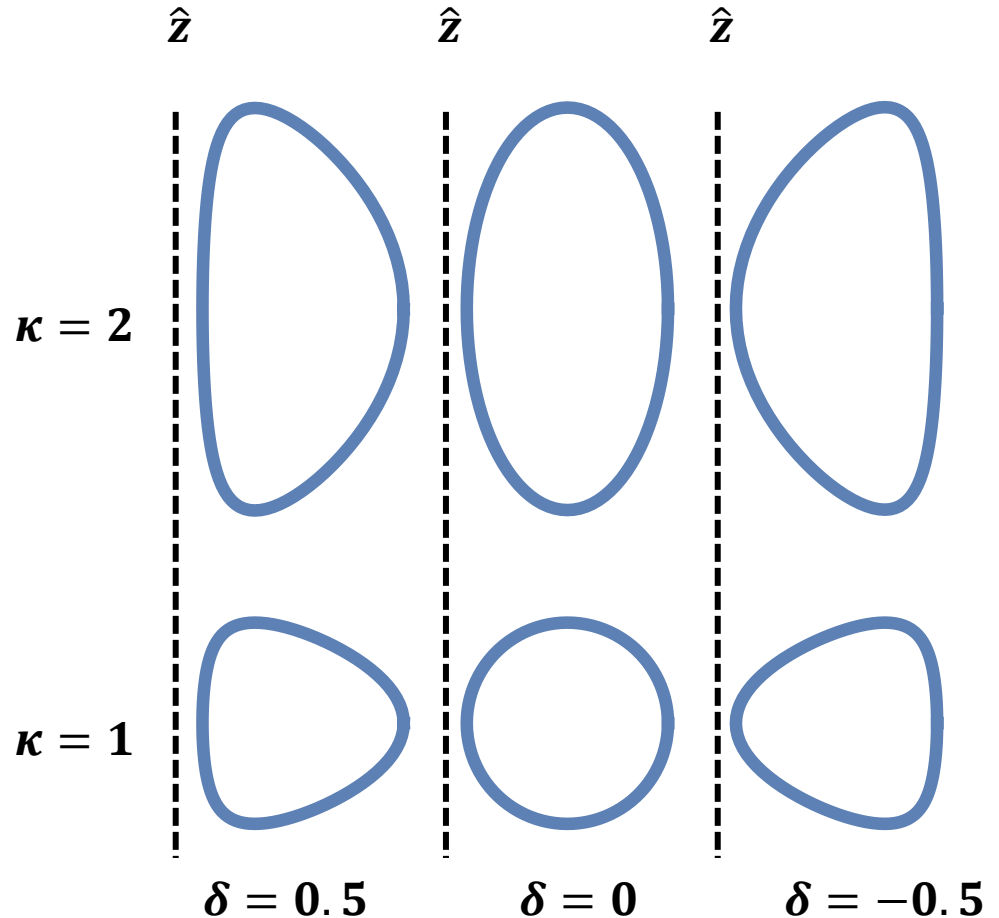
Different poloidal shapes



$$r = R + a \cos(\theta + \delta \sin(\theta))$$

$$z = a \kappa \sin(\theta)$$

- Aspect ratio: $\frac{R}{a}$
- Elongation: κ
- Triangularity: δ

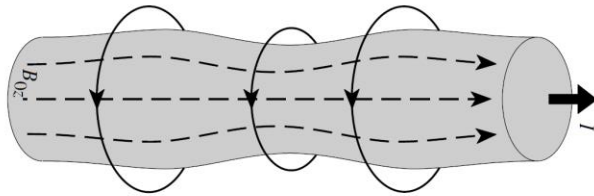


Safety factor

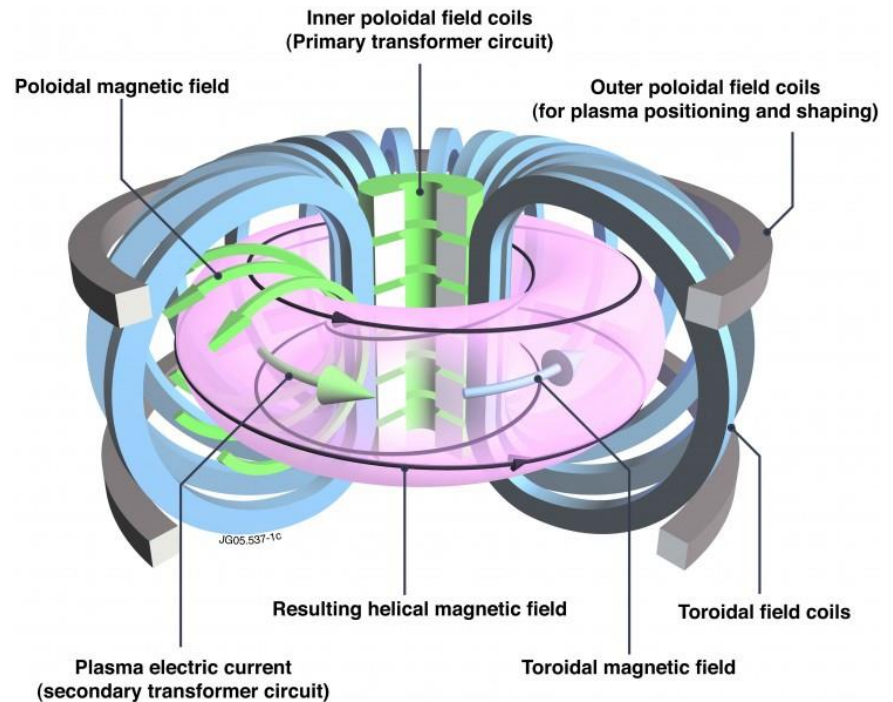


- Kink Safety Factor:

$$q^*(r) = \frac{aB_0}{R_0 B_p} = \frac{2\pi a^2 \kappa B_0}{\mu_0 R_0 I_0}$$



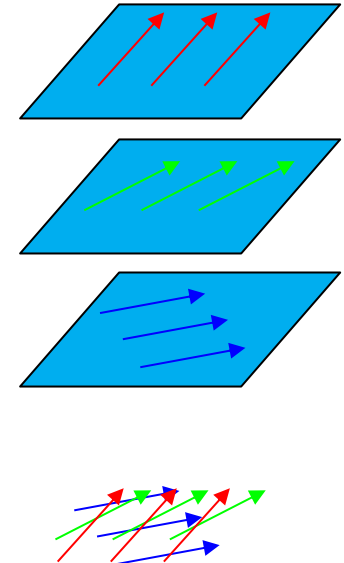
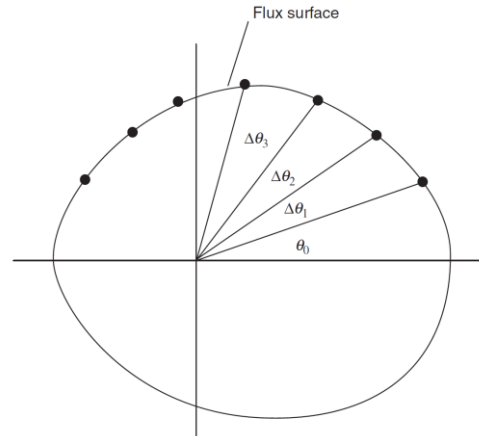
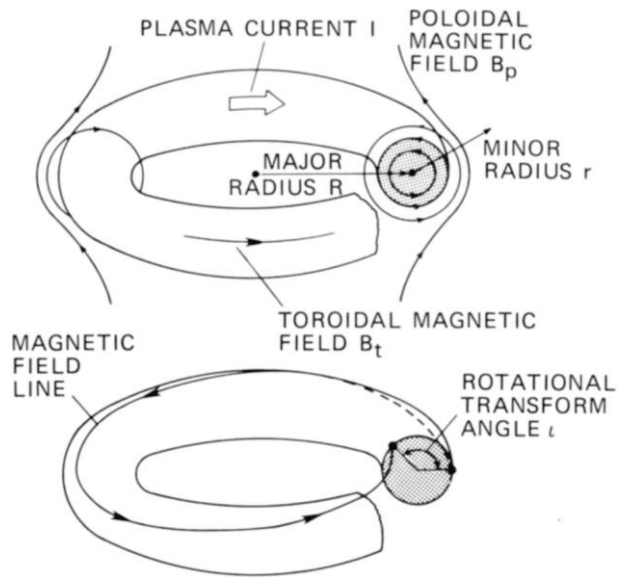
$$q(r) = \frac{rB_z(r)}{R_0 B_\theta(r)}$$



Safety factor



- **Shear:**



- **Rotational transform:**
$$\iota \equiv \lim_{N \rightarrow \infty} \frac{1}{N} \sum \Delta \theta_n$$

- **MHD safety factor:**
$$q(V) \equiv \frac{2\pi}{\iota(V)} = \frac{d\psi_t/dV}{d\psi_p/dV}$$

$$\psi_t = \psi_t(V) \quad \psi_p = \psi_p(V)$$

- **Shear:**
$$s(V) \equiv 2 \frac{V}{q} \frac{dq}{dV}$$

$$\iota(V) \equiv 2\pi \left(\frac{d\psi_p/dV}{d\psi_t/dV} \right)$$

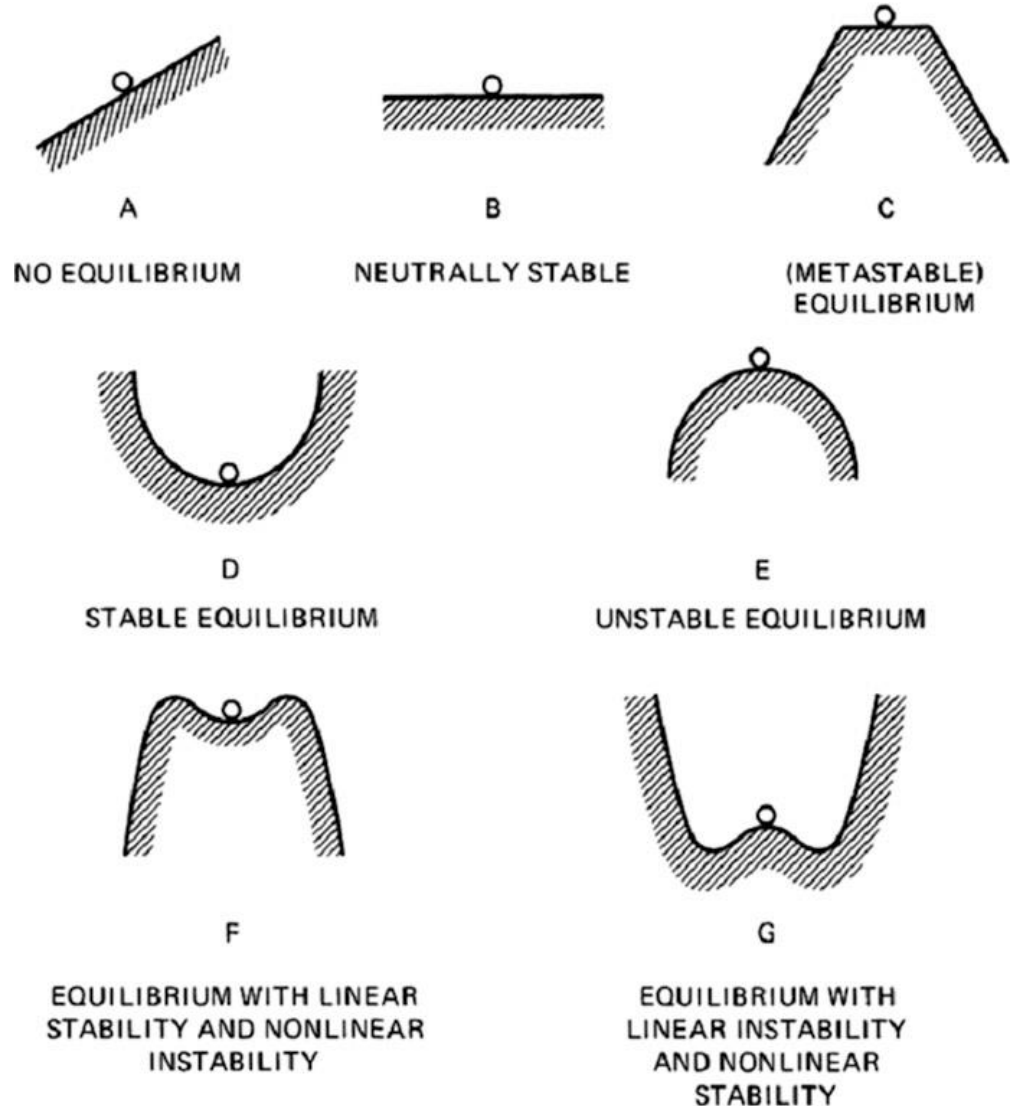
Magnetic well



$$\widehat{W} = 2 \frac{V}{\langle B^2 \rangle} \frac{d}{dV} \left\langle \frac{B^2}{2} \right\rangle$$

$$= 2 \frac{V}{\langle B^2 \rangle} \frac{d}{dV} \left\langle \mu_o p + \frac{B^2}{2} \right\rangle$$

- A magnetic well is a quantity that measures plasma stability against short perpendicular wavelength modes driven by the plasma pressure gradient.



Variational formulation for checking stabilization

- **Equilibrium state:** $\vec{j}_o \times \vec{B}_o = \nabla p_o$
 - **Momentum eq:** $\rho_m \left[\frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \nabla) \vec{v} \right] = \vec{j} \times \vec{B} - \nabla \cdot \vec{P}$
- $$\rho_m = \rho_o + \tilde{\rho}_1 \quad p = p_o + \tilde{p}_1 \quad \vec{v} = \vec{v}_o + \vec{\tilde{v}}_1 = \vec{\tilde{v}}_1 \equiv \frac{\partial \vec{\xi}}{\partial t}$$
- $$\vec{j} = \vec{j}_o + \vec{j}_1 \quad \vec{B} = \vec{B}_o + \vec{\tilde{B}}_1 \equiv \vec{B}_o + \vec{Q}$$

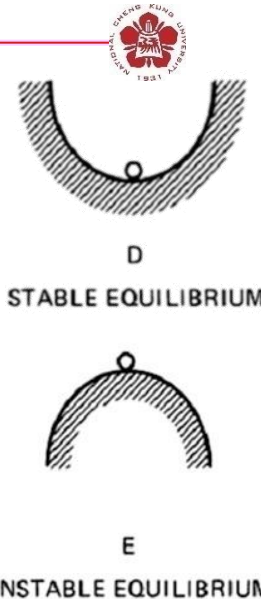
$$\rho_m \frac{\partial^2 \vec{\xi}}{\partial t^2} = \vec{F}(\vec{\xi}) \quad \vec{F}(\vec{\xi}) = \vec{j}_o \times \vec{Q} + \vec{j}_1 \times \vec{B}_o - \nabla \tilde{p}_1$$

$$\vec{F}(\vec{\xi}) = \frac{1}{\mu_o} (\nabla \times \vec{B}_o) \times \vec{Q} + \frac{1}{\mu_o} (\nabla \times \vec{Q}) \times \vec{B}_o + \nabla (\vec{\xi} \cdot \nabla p + \gamma p \nabla \cdot \vec{\xi})$$

- **The change in potential energy associated with the perturbation:**

$$\delta W = -\frac{1}{2} \int \vec{\xi}^* \cdot \vec{F}(\vec{\xi}) d\vec{r} \quad \bullet \text{ Stable requirement: } \delta W \geq 0$$

$$\delta W_F = \frac{1}{2} \int d\vec{r} \left[\frac{|\vec{Q}_\perp|^2}{\mu_o} + \frac{B^2}{\mu_o} |\nabla \cdot \vec{\xi}_\perp + 2 \vec{\xi}_\perp \cdot \vec{\kappa}|^2 + \gamma p |\nabla \cdot \vec{\xi}|^2 \right. \\ \left. - 2(\vec{\xi}_\perp \cdot \nabla p)(\vec{\kappa} \cdot \vec{\xi}_\perp^*) - J_\parallel (\vec{\xi}_\perp^* \times \vec{b}) \cdot \vec{Q}_\perp \right]$$



Variational formulation for checking stabilization

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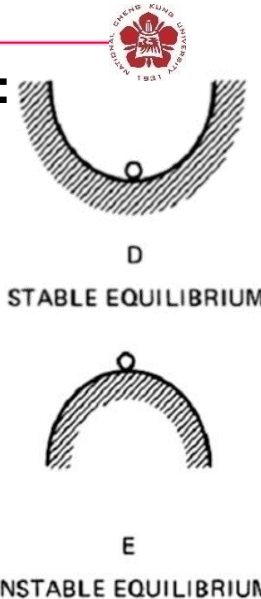
- Stabilization terms:

$$\frac{|\vec{Q}_\perp|^2}{\mu_o}: \text{ For bending magnetic field lines, (shear Alfvén wave).}$$

$$\frac{B^2}{\mu_o} (|\nabla \cdot \vec{\xi}_\perp + 2 \vec{\xi}_\perp \cdot \vec{\kappa}|)^2: \text{ For compressing the magnetic field, (compressional Alfvén wave).}$$

$$\gamma p |\nabla \cdot \vec{\xi}|^2: \text{ For compressing the plasma, (sound wave).}$$

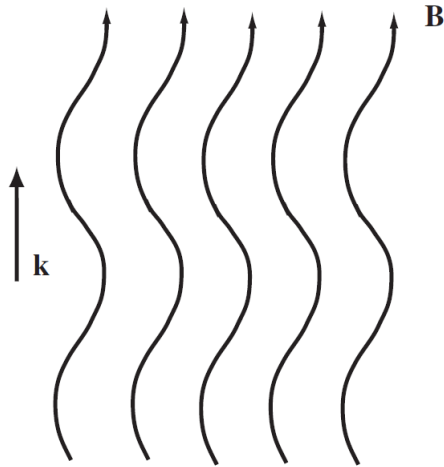
- Destabilization terms: $-2(\vec{\xi}_\perp \cdot \nabla p)(\vec{\kappa} \cdot \vec{\xi}_\perp^*) - J_\parallel (\vec{\xi}_\perp^* \times \vec{b}) \cdot \vec{Q}_\perp$



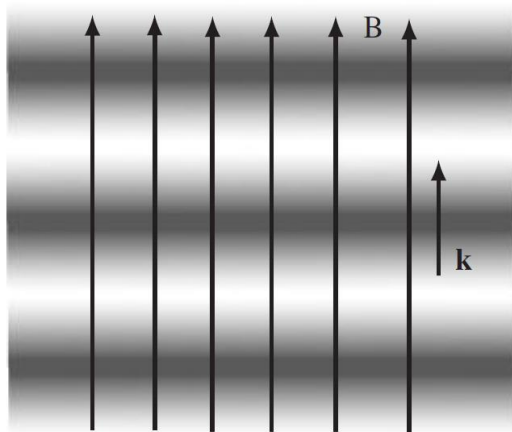
Alfvén waves



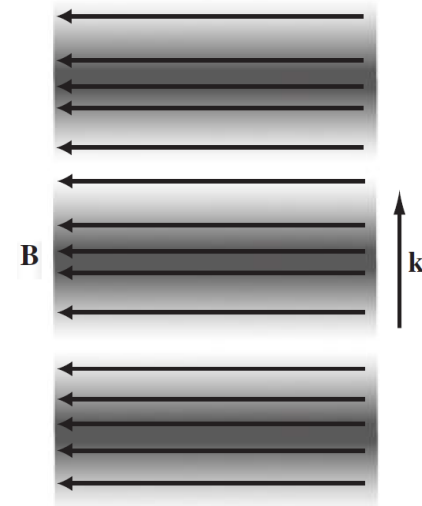
- **Shear Alfvén wave:**



- **Longitudinal sound wave
(the slow magnetosonic wave)**



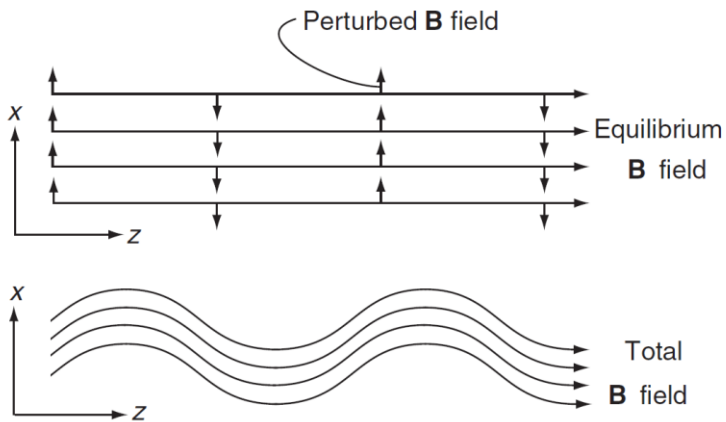
- **The fast magnetosonic wave
(Compressional Alfvén wave):**



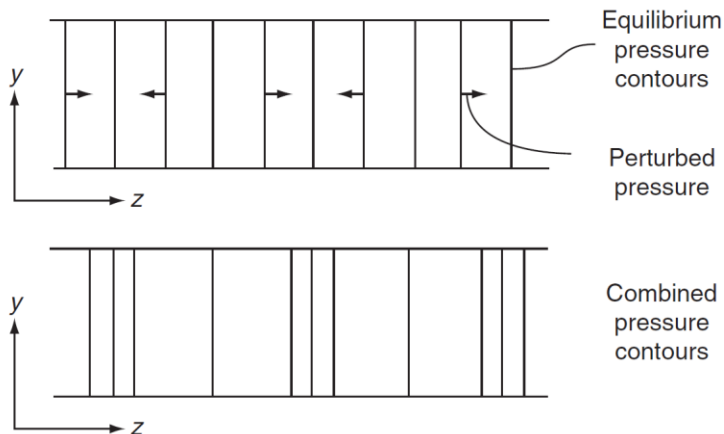
Alfvén waves



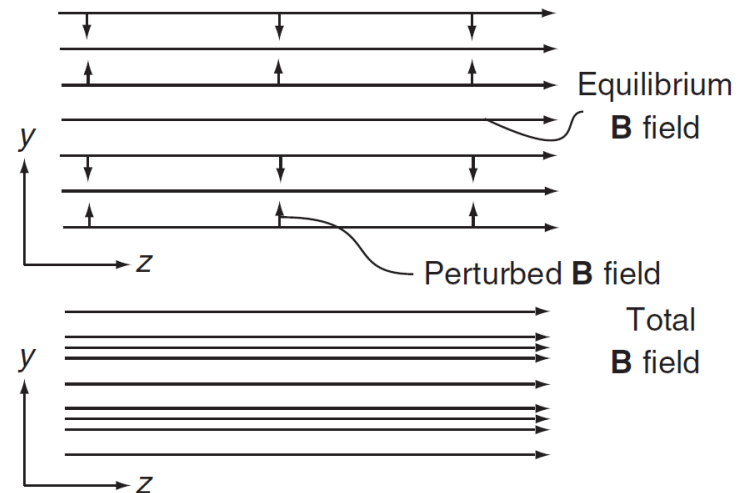
- Shear Alfvén wave:**



- The slow magnetosonic wave (Shear + Compressional Alfvén wave):**



- The fast magnetosonic wave (Compressional Alfvén wave):**



Classification of MHD instabilities



- **Locations:**
 - **Internal/Fixed boundary modes:** mode structure does not require any motion of the plasma-vacuum interface away from its equilibrium position.
 - **External/Free-boundary modes:** the plasma-vacuum interface moves from its equilibrium position during an unstable MHD perturbation.
- **Dominant destabilizing term**
 - **Pressure-driven modes:** the dominant destabilizing term is the one proportional to ∇p .
 - **Current-driven modes:** the dominant destabilizing term is the one proportional to J_{\parallel} .

$$\delta W_F = \frac{1}{2} \int d\vec{r} \left[\frac{|\vec{Q}_{\perp}|^2}{\mu_0} + \frac{B^2}{\mu_0} |\nabla \cdot \vec{\xi}_{\perp} + 2 \vec{\xi}_{\perp} \cdot \vec{\kappa}|^2 + \gamma p |\nabla \cdot \vec{\xi}|^2 \right. \\ \left. - 2(\vec{\xi}_{\perp} \cdot \nabla p)(\vec{\kappa} \cdot \vec{\xi}_{\perp}^*) - J_{\parallel}(\vec{\xi}_{\perp}^* \times \vec{b}) \cdot \vec{Q}_{\perp} \right]$$

Classification of MHD instabilities

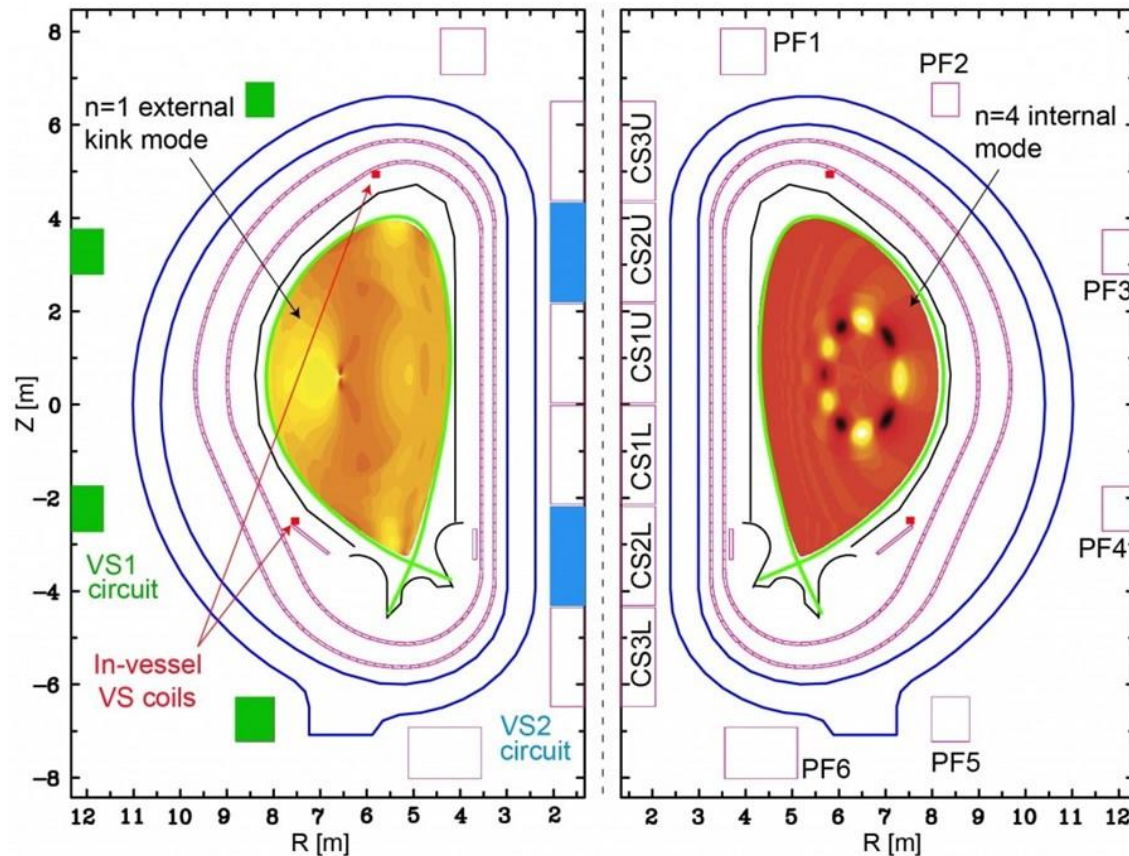


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 - **External/Free-boundary modes:** the plasma-vacuum interface moves from its equilibrium position during an unstable MHD perturbation.
- **Dominant destabilizing term**
 - **Current-driven modes, e.g., kink instability, sausage instability.**
 - **Pressure-driven modes, e.g., interchange mode, ballooning mode.**

External mode vs internal mode



- Predicted behaviors of the plasma in ITER

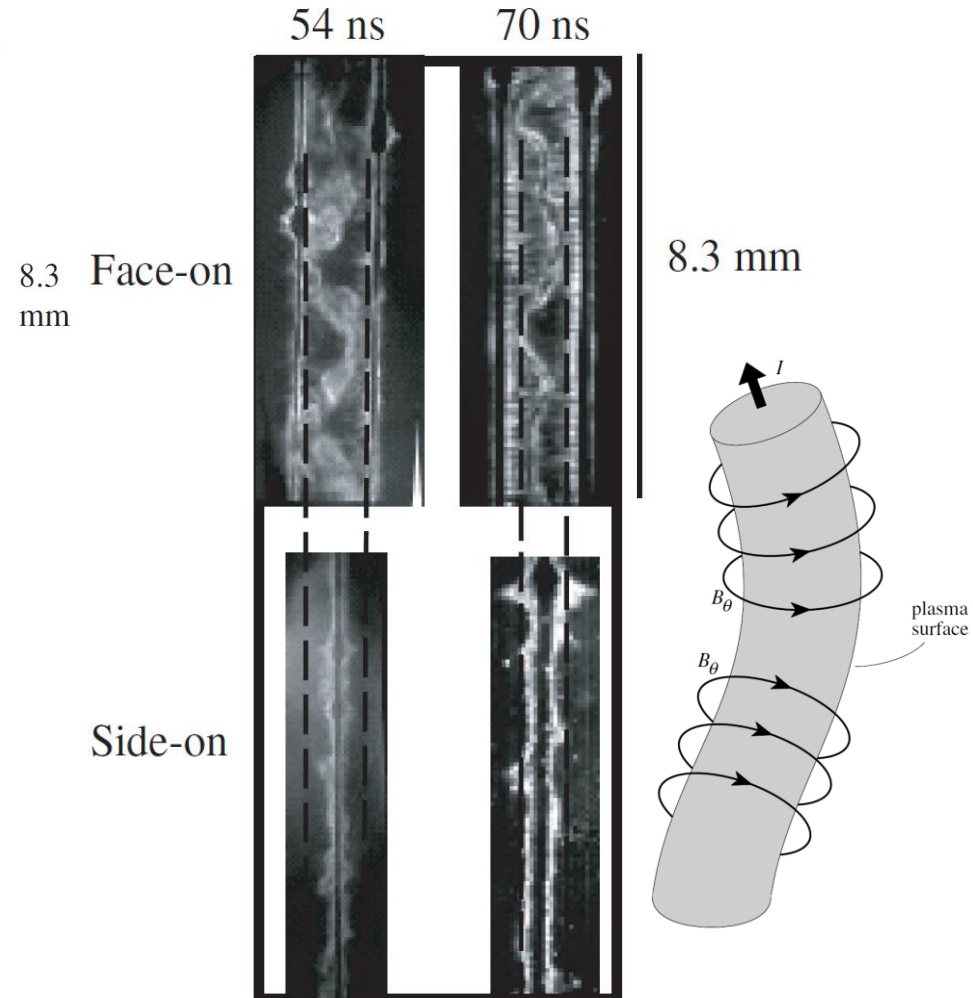
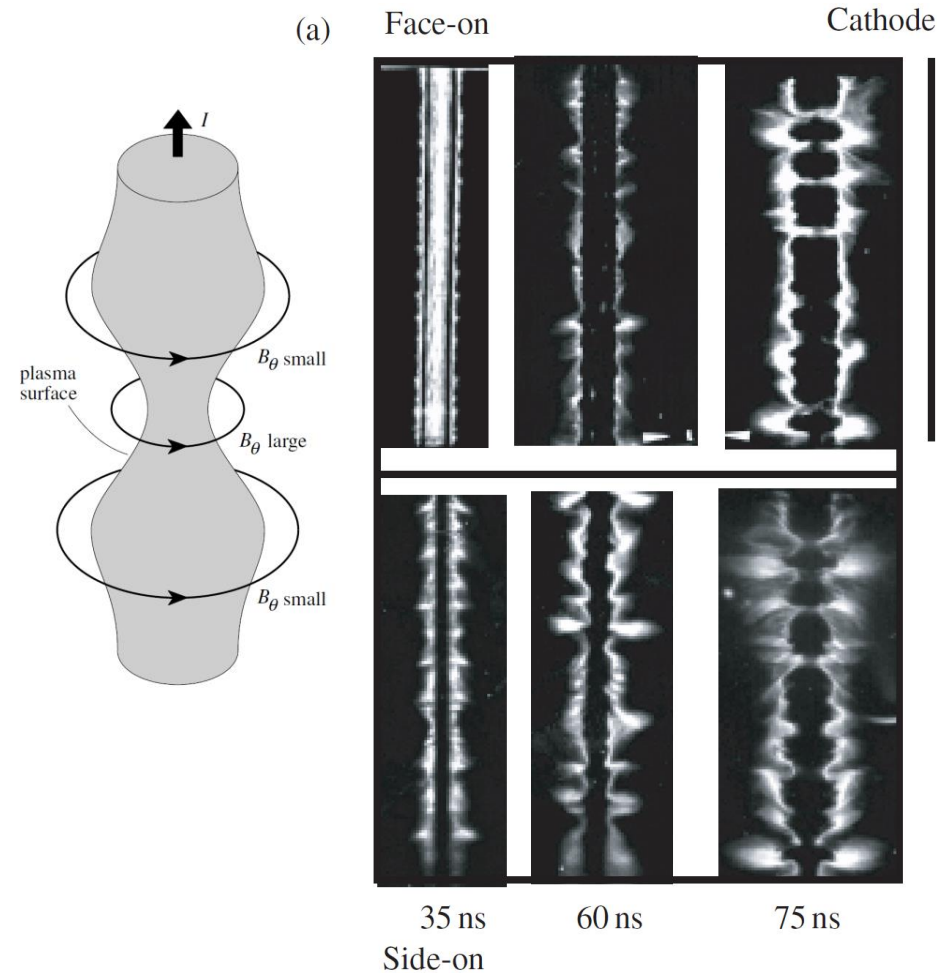


Current-driven instability

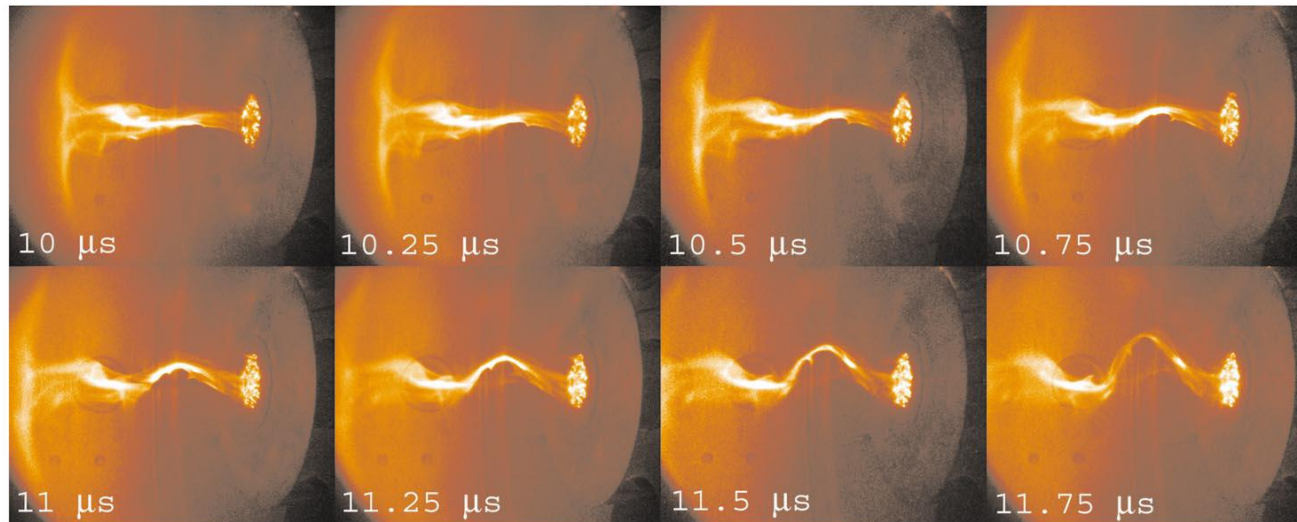
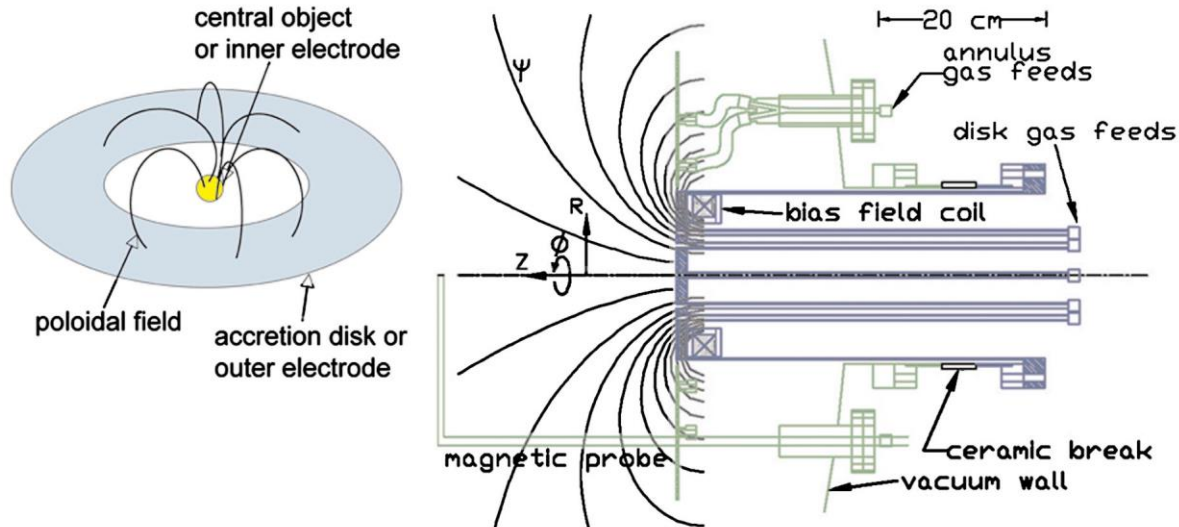


- Sausage instability ($m=0$)**

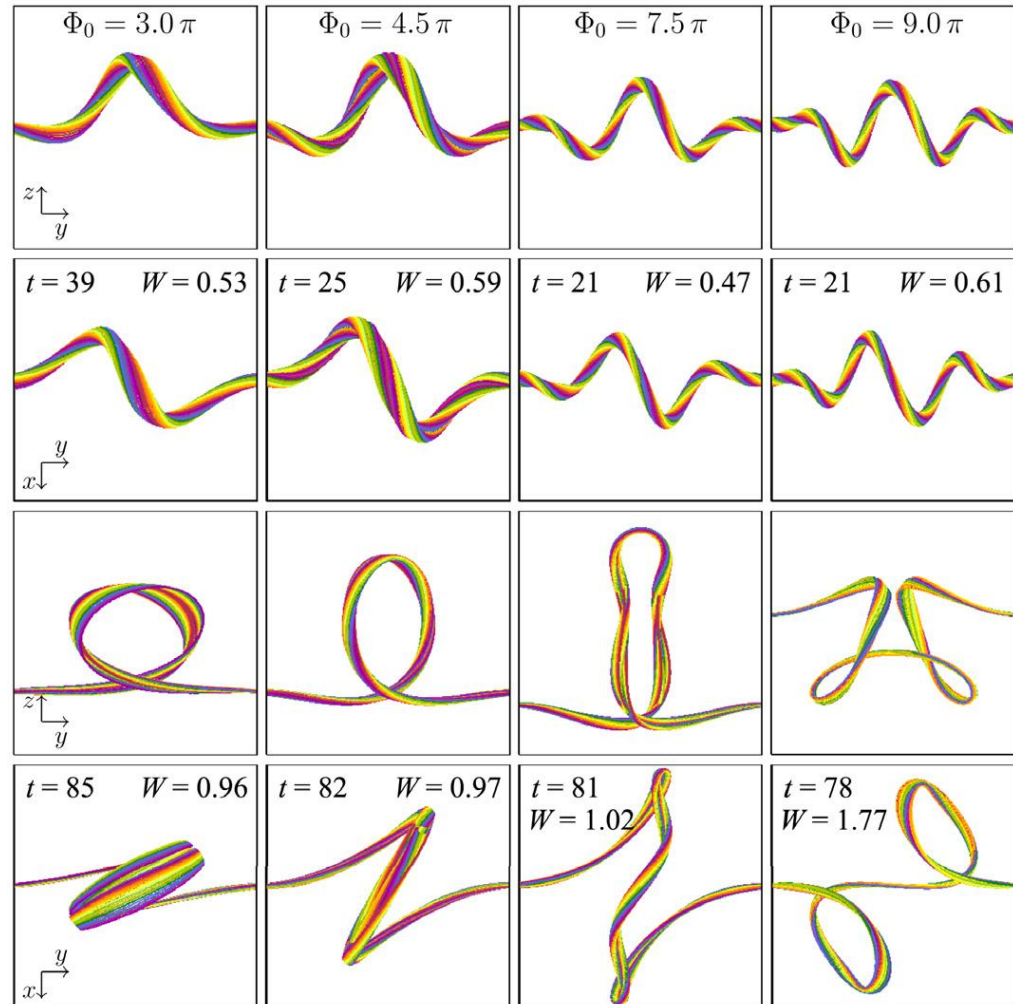
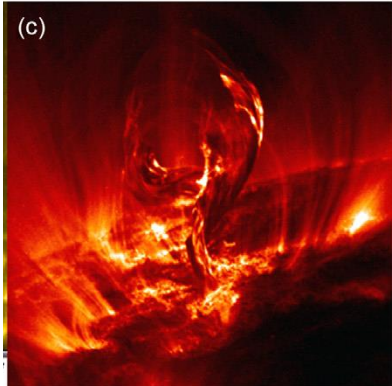
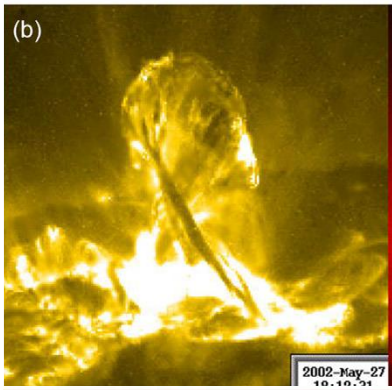
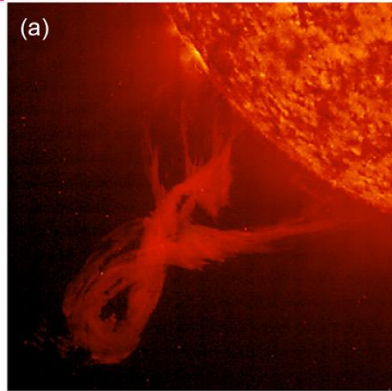
- Kink instability ($m=1$)**



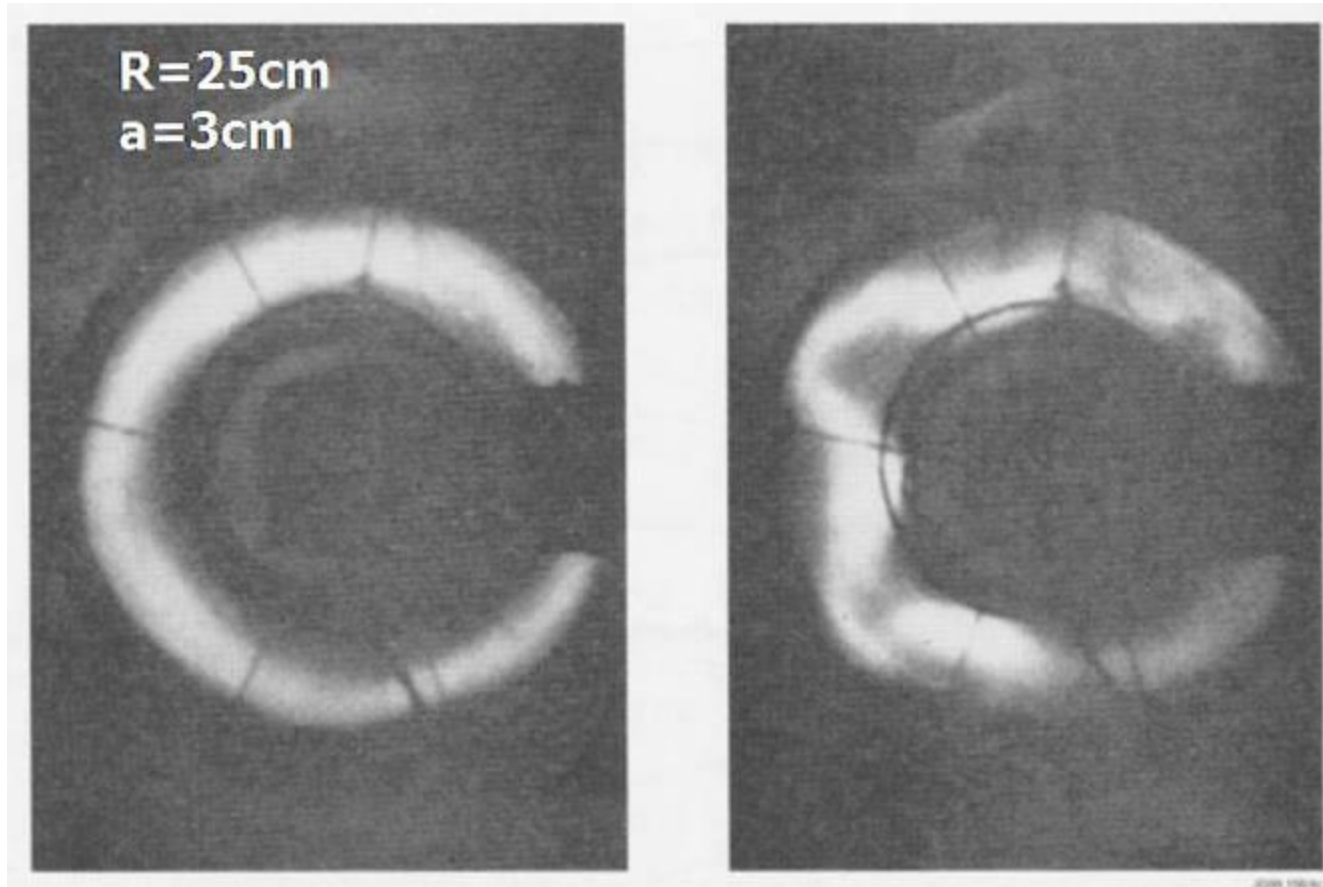
Kink instabilities in the lab



Kink instabilities in space



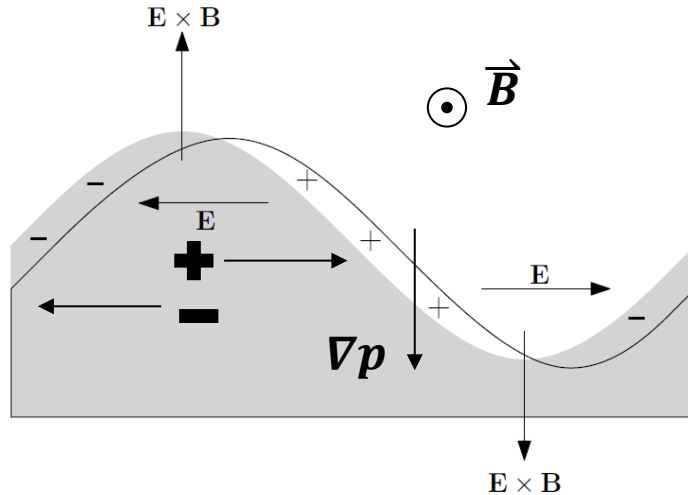
Kink instability in Tokamak



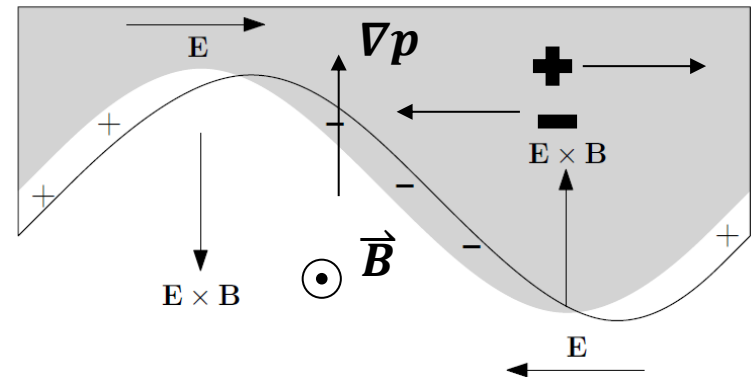
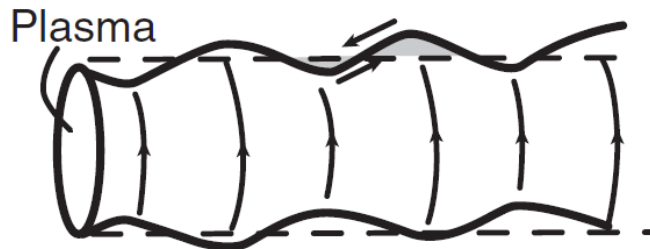
Pressure driven instability – interchange perturbations



- Unstable: bad curvature $\vec{R}_c \cdot \nabla p < 0$
- stable: good curvature $\vec{R}_c \cdot \nabla p > 0$

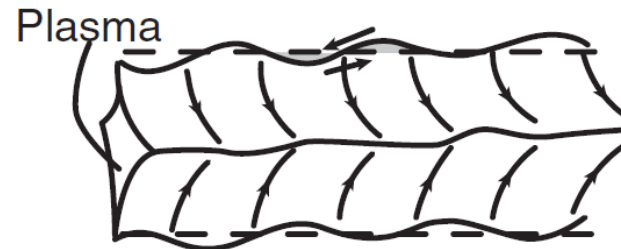


Unstable
plasma–vacuum
interface



\vec{R}_c Curvature
 $\vec{R}_c \times \vec{B}$ Curvature drift

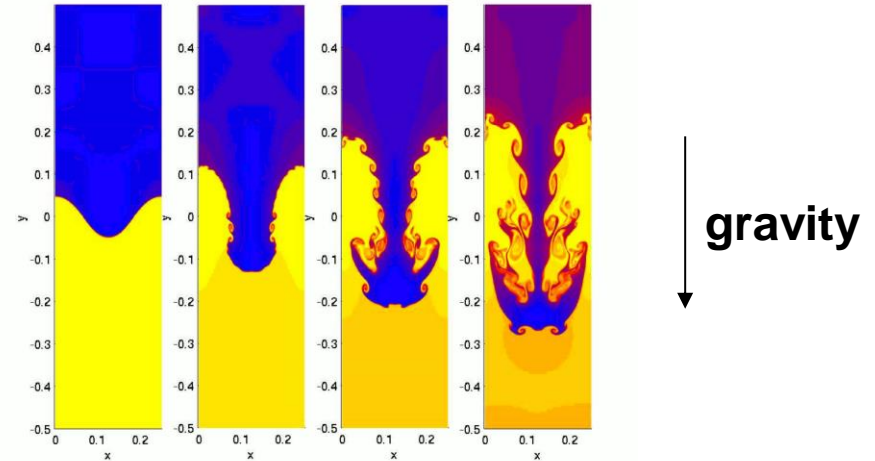
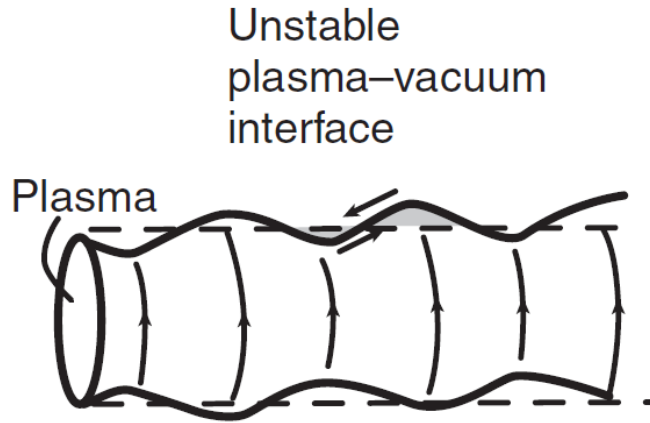
Stable
plasma–vacuum
interface



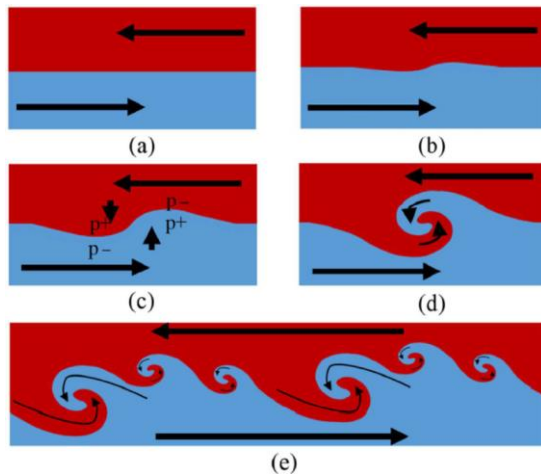
Rayleigh-Taylor instability



- Rayleigh-Taylor instability

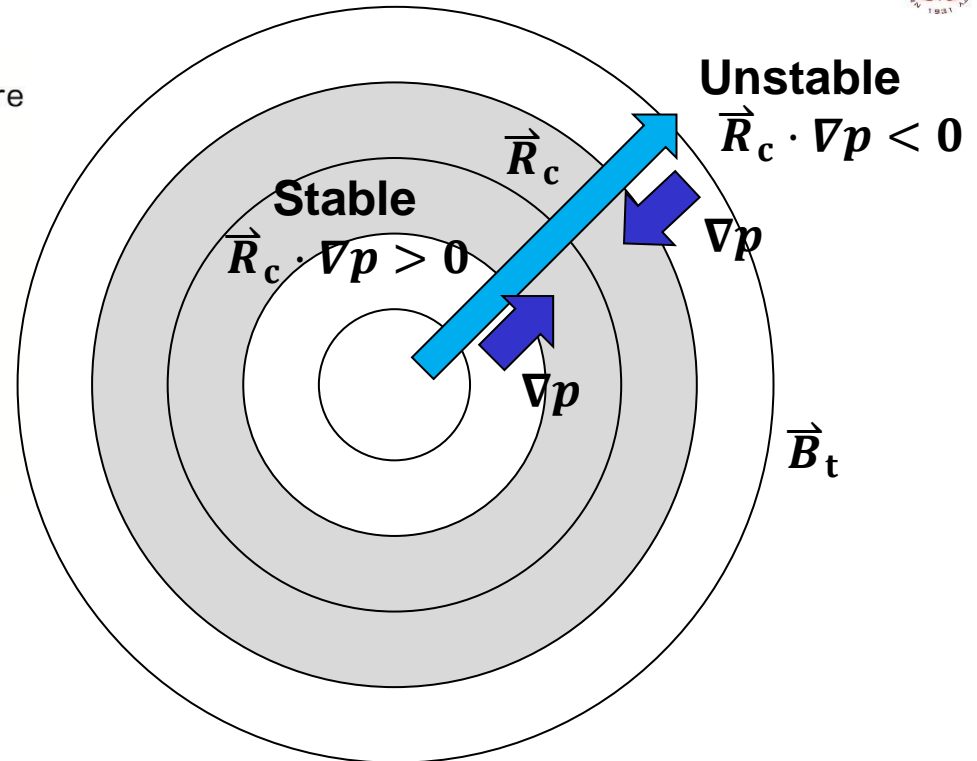
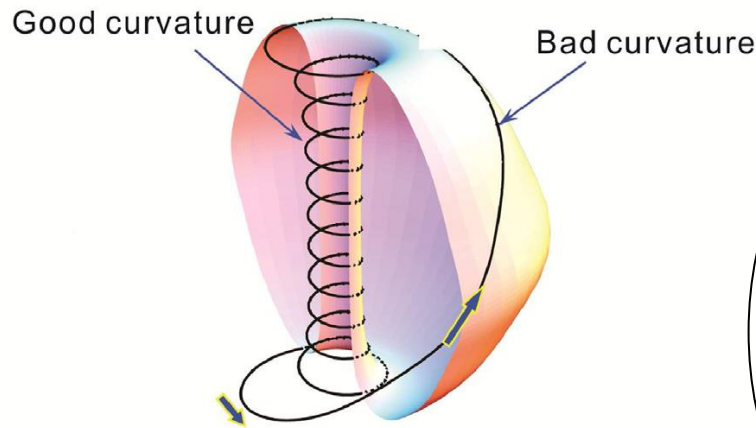


- Kelvin-Helmholtz instability



https://en.wikipedia.org/wiki/Rayleigh%E2%80%93Taylor_instability
https://en.wikipedia.org/wiki/Kelvin%E2%80%93Helmholtz_instability
 Xie Lei et al, Energy Report **7**, 2262 (2021)

Pressure driven instability – interchange perturbations



- Suydam criterion for cylindrical plasmas:

$$\mu_0 \frac{2r^2}{B_\theta^2} \frac{1}{s^2} \vec{R}_c \cdot \nabla p > -\frac{1}{4} \quad \text{Shear: } s = \frac{r}{q} \frac{dq}{dr}$$

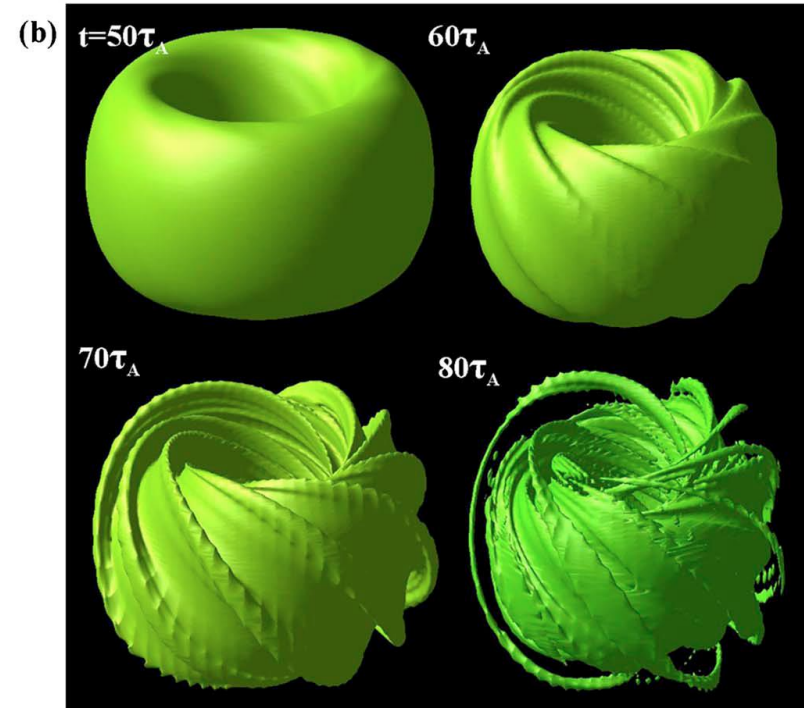
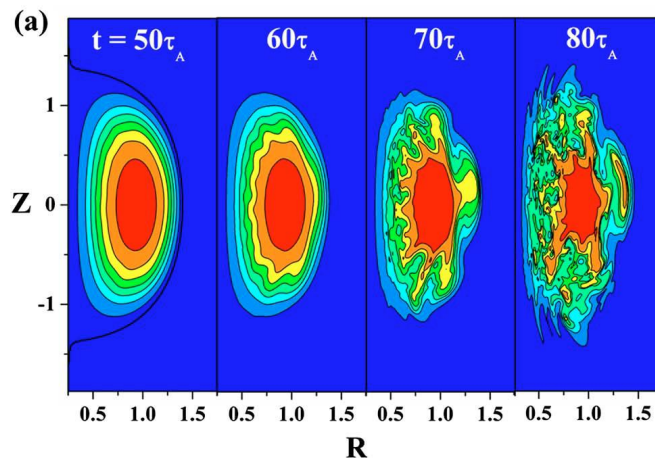
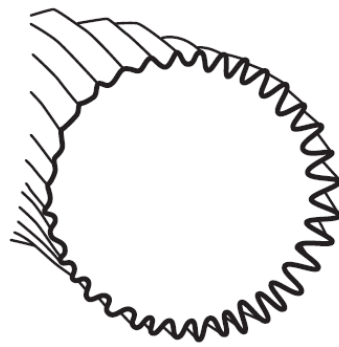
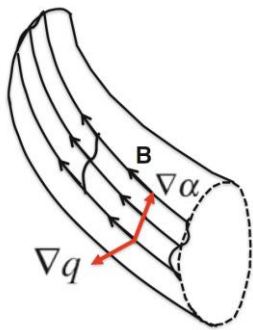
- Mercier criterion for tokamak:

$$D = -\mu_0 \frac{2r}{B^2} \frac{1}{s^2} \frac{dp}{dr} (1 - q^2) < \frac{1}{4}$$

Ballooning mode – show wavelength mode



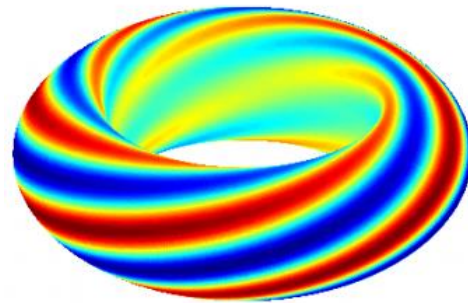
$$\delta W_F = \frac{1}{2} \int d\vec{r} \left[\frac{|\vec{Q}_\perp|^2}{\mu_o} + \frac{B^2}{\mu_o} |\nabla \cdot \vec{\xi}_\perp + 2 \vec{\xi}_\perp \cdot \vec{\kappa}|^2 + \gamma p |\nabla \cdot \vec{\xi}|^2 \right. \\ \left. - 2(\vec{\xi}_\perp \cdot \nabla p)(\vec{\kappa} \cdot \vec{\xi}_\perp^*) - J_\parallel (\vec{\xi}_\perp^* \times \vec{b}) \cdot \vec{Q}_\perp \right]$$



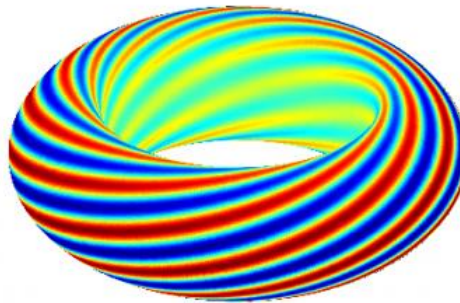
Ballooning mode – show wavelength mode



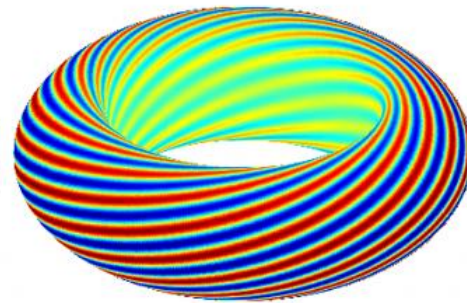
Tokamak Ballooning Mode Visualization (Artificial)



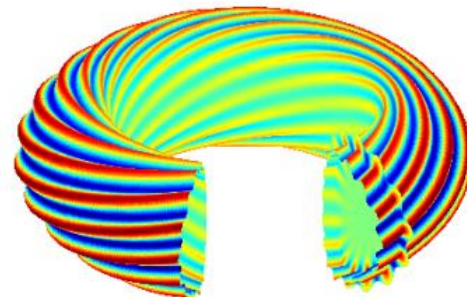
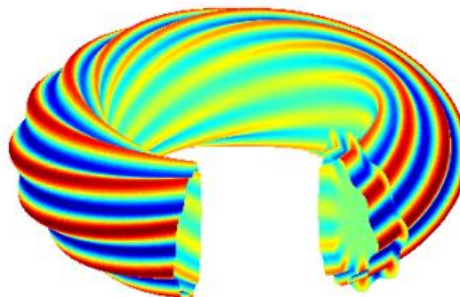
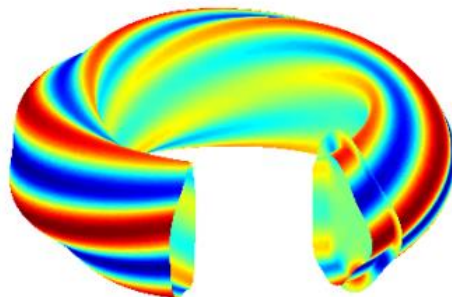
(m=5, n=4)



(m=10, n=8)



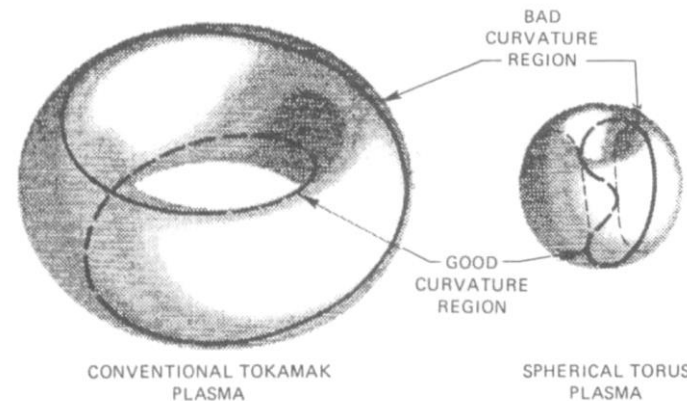
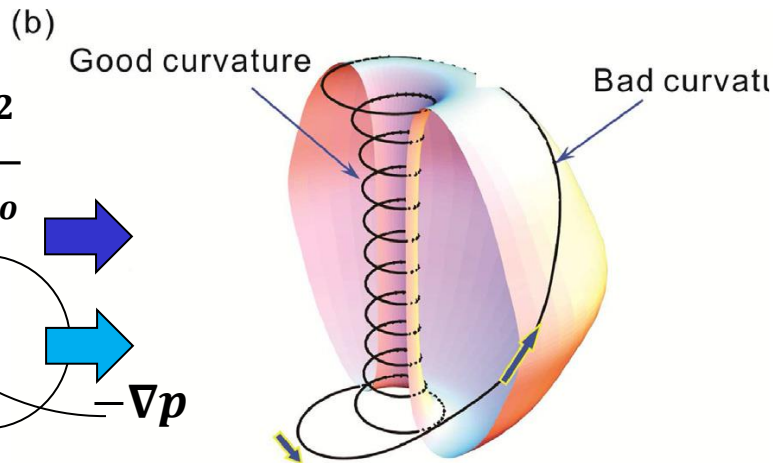
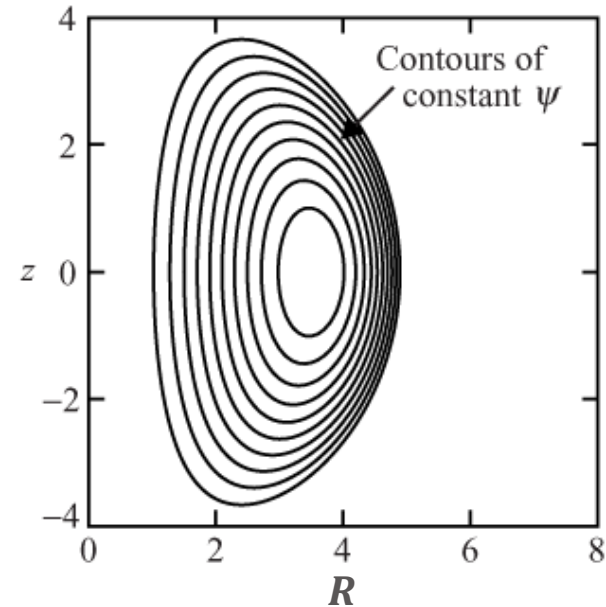
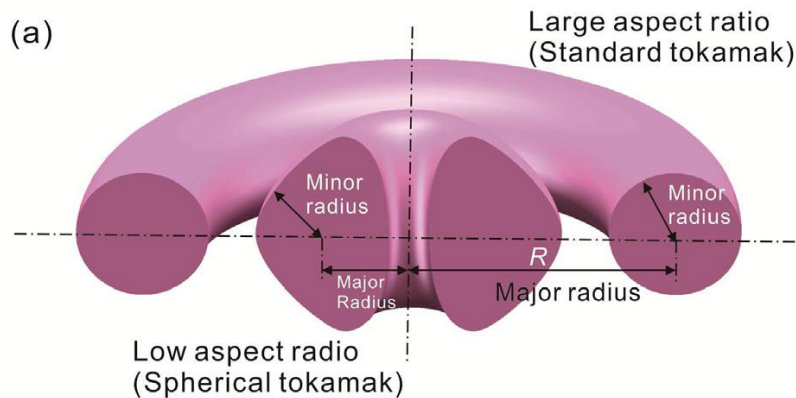
(m=15, n=12)



The Spherical tokamak



- Aspect ratio $R_0/a \sim 1.6$



Zhe Gao, Matter and Radia. Extrem., **1**, 153 (2016)

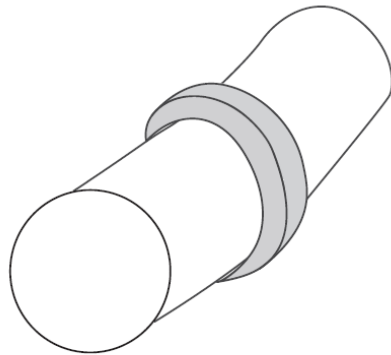
Y-k. M. Peng and D. J. Strickler, Nucl. Fusion **26**, 769 (1986)

The Spherical tokamak

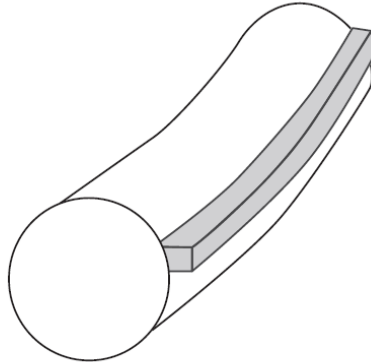


- Aspect ratio $R_0/a \sim 1.6$
- Advantages:
 - Higher β_t limit.
 - A compact design almost spherical in appearance.
- Challenges:
 - Minimum space is given in the center of the torus to accommodate the toroidal field coils.
 - With a very compact design the technology associated with the construction and maintenance of the device may be more difficult than for a “normal” tokamak.
 - Large currents will have to be driven noninductively, a costly and physically difficult requirement.

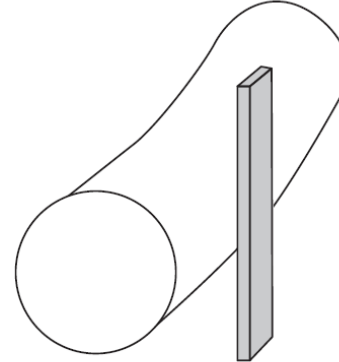
Limiter protects the vacuum chamber from plasma bombardment and defines the edge of the plasma



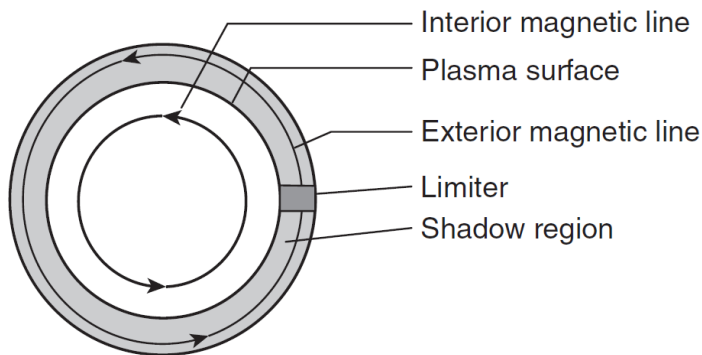
Poloidal limiter



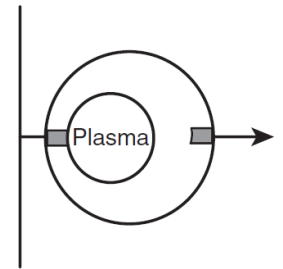
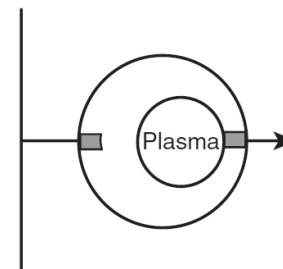
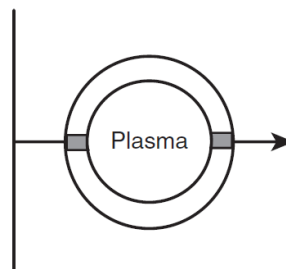
Toroidal limiter



Rail limiter



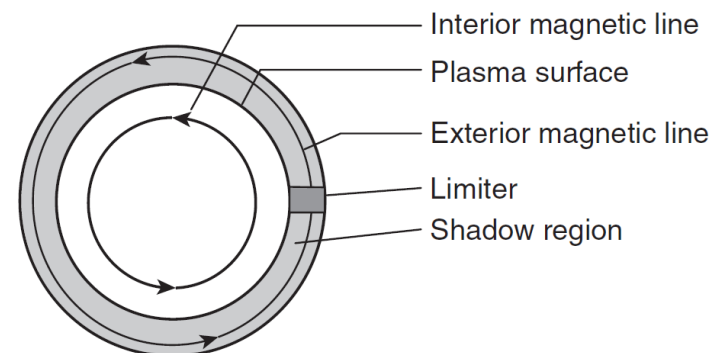
- **Vertical field is correct.**
- **Vertical field is too small.**
- **Vertical field is too large.**



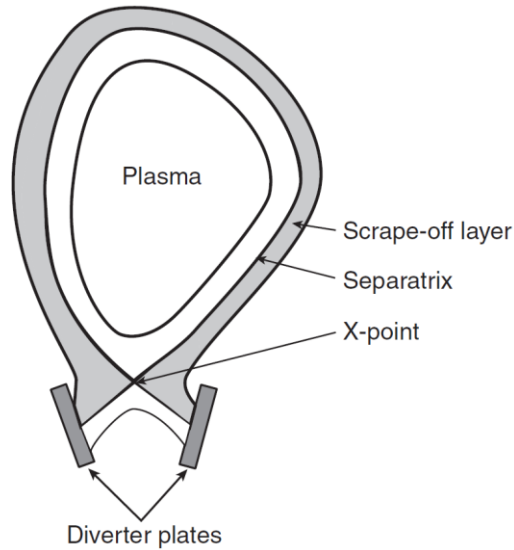
Limiter protects the vacuum chamber from plasma bombardment and defines the edge of the plasma



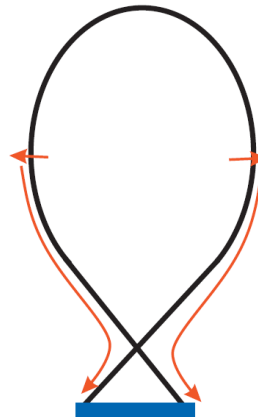
- A mechanical limiter is a robust piece of material, often made of tungsten, molybdenum, or graphite placed inside the vacuum chamber.
- Some of the particles of the limiter surface may escape. Neutral particles can penetrate some distance into the plasma before being ionized.
- The high-z impurities can lead to significant additional energy loss in the plasma through radiation.
- In ignition experiments and fusion reactors, the bombardment is more intense and extends over longer periods of time. In addition, if the impurity level is too high, it may not be possible to achieve a high enough temperature to ignite.



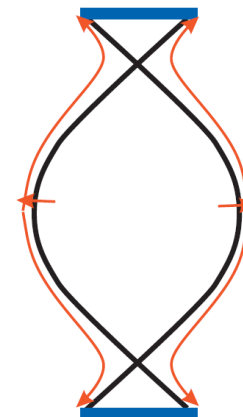
The magnetic divertor – guide a narrower layer of magnetic lines away from the edge of the plasma



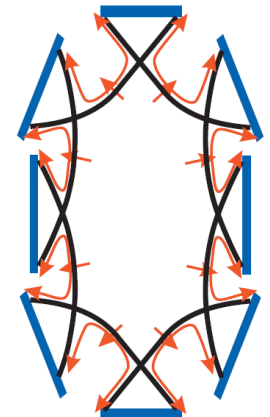
- **Single-null poloidal-field divertors for tokamak**



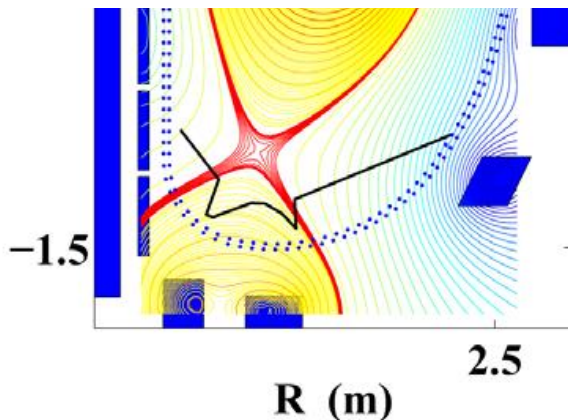
- **Double-null poloidal-field divertors for tokamak**



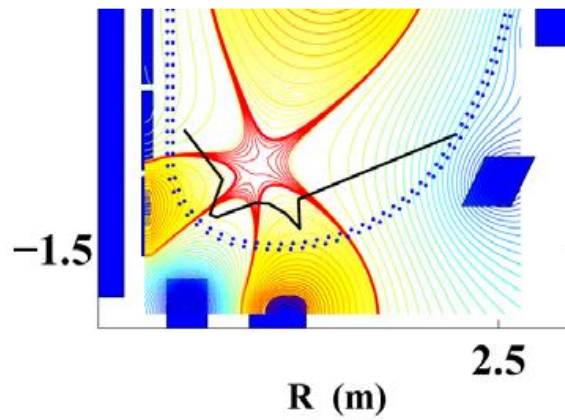
- **Island divertor for stellerators**



- **Standard**



- **Snowflake**



Y. Feng, Nucl. Fusion, **46**, 807 (2006)
 L Xue *et al*, Plasma Phys. Control. Fusion **58**, 055005 (2016)

Pros and cons of a divertor



- **Advantages:**
 - The collector plate is remote from the plasma. There is space available to spread out the magnetic lines.
 - A lower intensity of particles and energy bombard the collector plate leading to a longer replacement time.
 - It is more difficult for impurities to migrate into the plasma.
 - There are longer distance distances to travel and if a neutral particle becomes ionized before or during the time it crosses the divertor layer on its way toward the plasma, its parallel motion then carries it back to the collector plate.
 - The larger divertor chamber provides more access to pump out impurities.
 - The plasma edge is not in direct contact with a solid material such as a limiter.
- **Disadvantages:** larger and more complex system and more expensive.

Course Outline

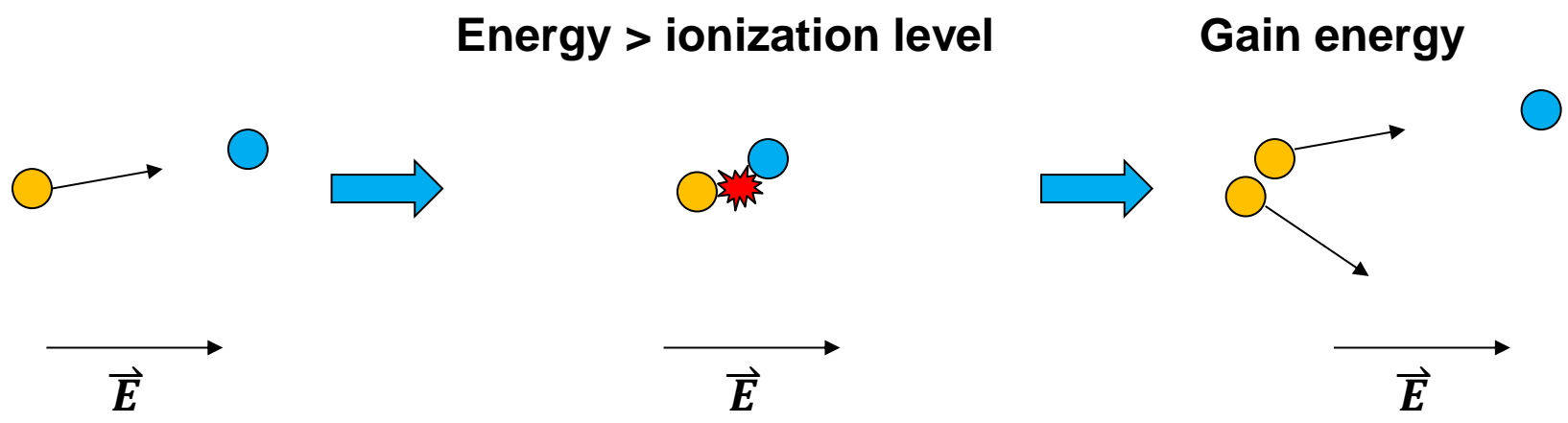


- **Magnetic confinement fusion (MCF)**
 - Gyro motion, MHD
 - 1D equilibrium (z pinch, theta pinch)
 - Drift: ExB drift, grad B drift, and curvature B drift
 - Tokamak, Stellarator (toroidal field, poloidal field)
 - Magnetic flux surface
 - 2D axisymmetric equilibrium of a torus plasma: Grad-Shafranov equation.
 - Stability (Kink instability, sausage instability, Safety factor Q)
 - Central-solenoid (CS) start-up (discharge) and current drive
 - CS-free current drive: electron cyclotron current drive, bootstrap current.
 - Auxiliary Heating: ECRH, Ohmic heating, Neutral beam injection.

Collisions play an important role in ionization process



- At the microscopic level, breakdown requires the presence of sufficiently energy charge particles that have acquired enough energy from the applied electric field between two energy-dissipating collisions to ionize the material and to create more charge particles.



In most cases, electrons dominate the breakdown process since its mobility is much larger than that of ions



$$E_k = \frac{1}{2}mv^2$$

$$v = \sqrt{\frac{2E_k}{m}}$$

$$E_k \sim kT$$

Collision time: $t = \frac{s}{\sqrt{\frac{2E_k}{m}}} \sim \frac{n^{-1/3}}{\sqrt{T}} \sqrt{m}$

$$n = \frac{\#}{V} \sim \frac{\#//}{s^3}$$

$$s \sim n^{-1/3}$$

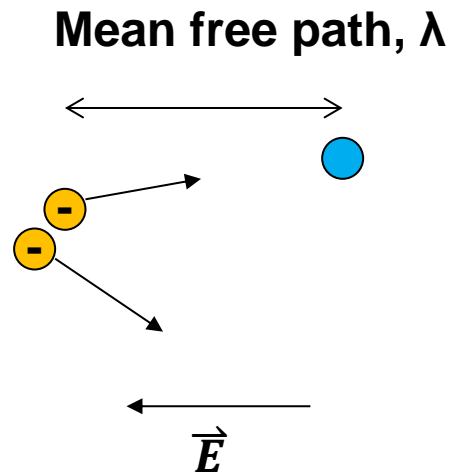
$$\frac{m_i}{m_e} \sim 2000 \times \text{Atomic mass}$$

$$\frac{t_i}{t_e} \sim 45 \times \sqrt{A}$$

Mean free path is important in ionization process



- For an electron to acquire enough energy between collisions, its mean free path in the material must be sufficiently long.

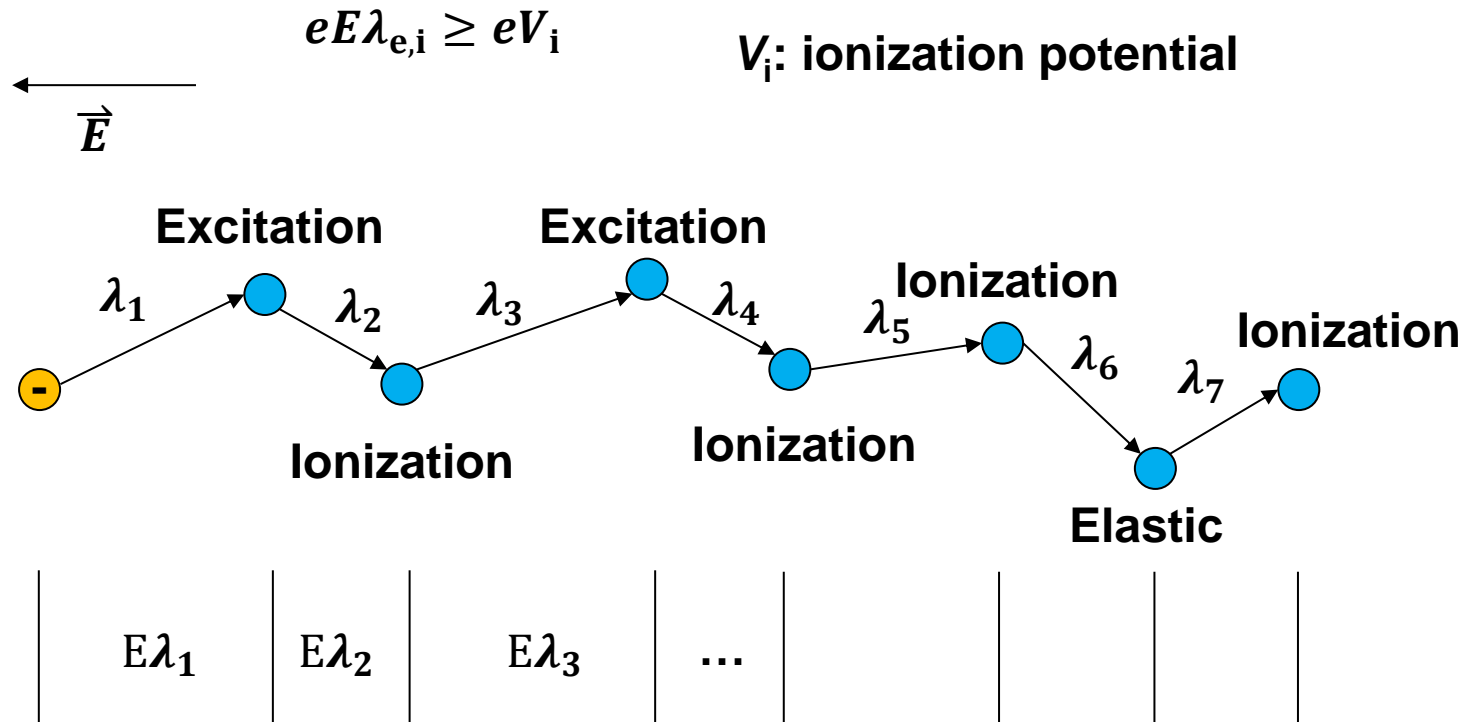


$$E_k = e \times E \times \lambda = eV$$

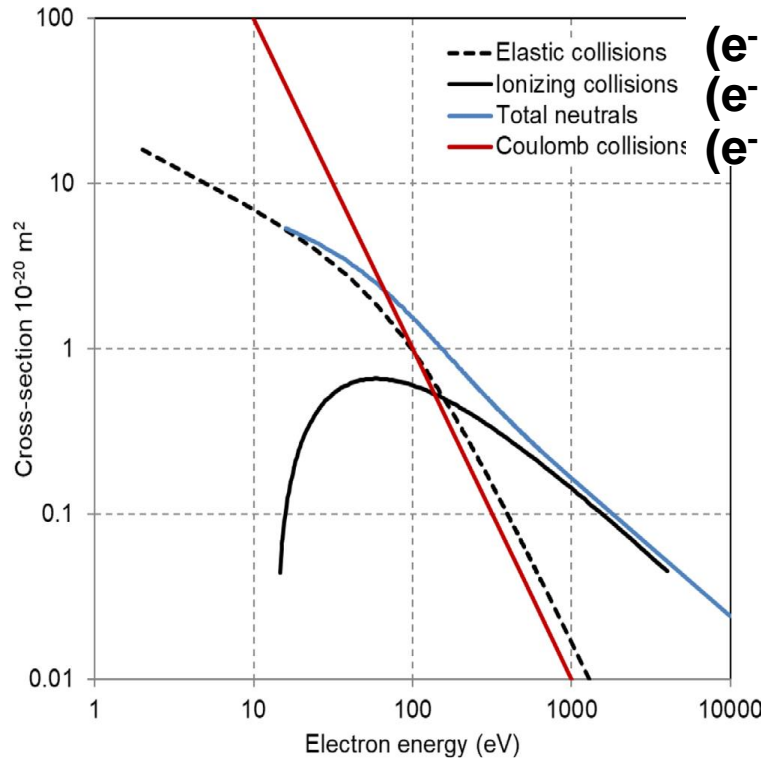
Electron impact ionization is the most important process in a breakdown of gases



- Electron impact ionization: $A + e^- \rightarrow A^+ + e^- + e^-$
 - The most important process in the breakdown of gases but is not sufficient alone to result in the breakdown.



Collision cross-sections of elastic, ionizing collisions between e^- and H_2 and coulomb collisions



(e^- vs H_2)
 $(e^- + H_2 \rightarrow 2e^- + H^+ + H)$
 (e^- vs H^+)

$$\sigma_{\text{elastic}, m^2} = \frac{1.75 \times 10^{-16}}{(W_{e, \text{eV}}^{1.5} + 750) \sqrt{W_{e, \text{eV}}}}$$

$$\sigma_{\text{ionizing}, m^2} \sim 3 \times 10^{-20} \left(\ln \epsilon - 0.69 + \frac{0.66}{\epsilon} \right) \epsilon^{-1}$$

$$\epsilon = \frac{W_e}{E_{\text{ion}}} \quad E_{\text{ion}} \sim 15 \text{ eV for } H_2$$

$$\sigma_{\text{coulomb}} = \frac{e^4}{4\pi\epsilon_0^2 m_e^2 v_e^2} \ln \Lambda$$

$$= \frac{e^4}{16\pi\epsilon_0^2 W_e^2} \ln \Lambda \sim 10^{-16} W_e^{-2}$$

for $\ln \Lambda \sim 13 - 15$

$$\nu = n v_E \sigma$$

$$\lambda = \frac{1}{n \sigma}$$

Townsend avalanche process for Tokamak breakdown



- The first Townsend coefficient α : the number of ionizing collisions made on the average by an electron as it travels 1 m along the electric field:

$$\alpha \sim \frac{1}{\lambda_i} = \frac{\nu_{ei}}{\bar{v}_e} = \frac{n_0 \langle \sigma v_e \rangle_{ne}}{\bar{v}_e} = \frac{p}{T} \frac{\langle \sigma v \rangle_{ne}}{\bar{v}_e} \equiv Ap \quad A \equiv \frac{1}{T} \frac{\langle \sigma v \rangle_{ne}}{\bar{v}_e}$$

- Number of primary electrons with energy higher than the ionization potential:

$$dn_e = -n_e \frac{dx_i}{\lambda_i} \Rightarrow \frac{n_e(x_i)}{n_{e0}} = \exp\left(-\frac{x_i}{\lambda_i}\right)$$

$$\alpha \equiv \frac{\text{\# / ionization collisions}}{\text{per electron}} \times (\text{\# / electron with } E > \text{ionization potential})$$

$$= \frac{1}{\lambda_i} \frac{n_e(x_i)}{n_{e0}} = \frac{1}{\lambda_i} \exp\left(-\frac{x_i}{\lambda_i}\right)$$

$$\alpha = Ap \exp(-Ap x_i)$$

$$A = 3.83 \text{ m}^{-1} \text{Pa}^{-1} = 1060 \text{ m}^{-1} \text{Torr}^{-1}$$

$$B = 96.6 \text{ Vm}^{-1} \text{Pa}^{-1} = 35000 \text{ m}^{-1} \text{Torr}^{-1}$$

$$\alpha = Ap \exp\left(-\frac{AV^*}{E/p}\right) \equiv Ap \exp\left(-\frac{B}{E/p}\right) \quad x_i \approx \frac{V^*}{E} \text{ where } V^* > V_i$$

- The parameters A and B must be experimentally determined.

Paschen's curve for minimum breakdown voltage



$$\alpha \sim \frac{1}{\lambda_i} = Ap \quad \alpha = Ap \exp\left(-\frac{B}{E/p}\right)$$

$$A = 3.83 \text{ m}^{-1}\text{Pa}^{-1} = 1060 \text{ m}^{-1}\text{Torr}^{-1}$$

$$B = 96.6 \text{ Vm}^{-1}\text{Pa}^{-1} = 35000 \text{ m}^{-1}\text{Torr}^{-1}$$

- For $p=1 \text{ mPa}$, $\lambda_i \sim 262 \text{ m}$, for ITER, $2\pi r_o \sim 38 \text{ m}$ $\frac{\lambda_i}{2\pi r_o} \sim 7$

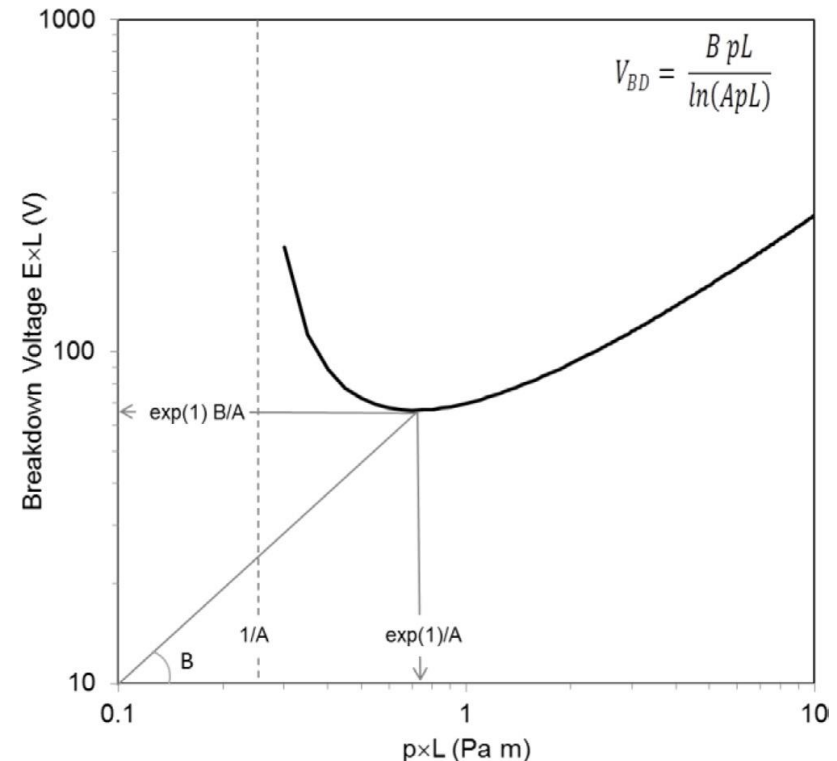
- For breakdown to happen:

$$\alpha L > 1 \quad \alpha L = ApL \exp\left(-\frac{BpL}{V_{BD}}\right) > 1$$

$$\exp\left(-\frac{BpL}{V_{BD}}\right) > \frac{1}{ApL}$$

$$-\frac{BpL}{V_{BD}} > -\ln(ApL)$$

$$V_{BD} > \frac{BpL}{\ln(ApL)} \quad E_{BD} > \frac{Bp}{\ln(ApL)}$$



Perpendicular stray-field (B_z) needs to be as small as possible



- For $p=1$ mPa, $\lambda_i \sim 262$ m, for ITER, $2\pi r_o \sim 38$ m $\frac{\lambda_i}{2\pi r_o} \sim 7$

$$\frac{B_z}{B_T} \sim 10^{-3} \quad \lambda_i \times \frac{B_z}{B_T} = 0.26 \text{ m}$$

- For ITER,

$$E \sim E_{\text{loop}} = 0.3 \text{ V/m}$$

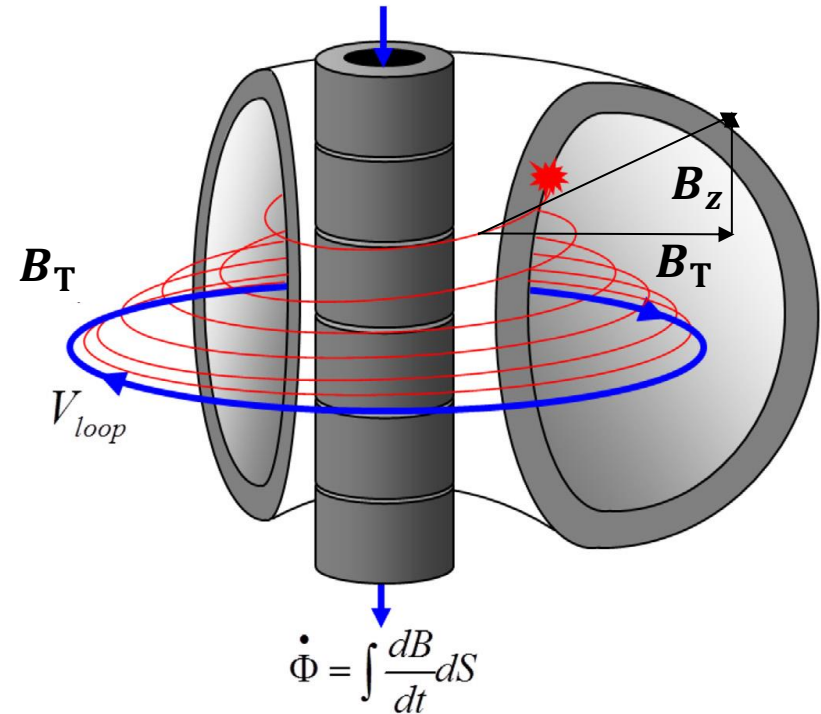
$$p = 1 \text{ mPa} \quad L_{\text{BD}} = 357 \text{ m}$$

- Required loop field:

$$E_{\text{BD}} > \frac{Bp}{\ln(ApL)}$$

$$E_{\text{BD}} > \frac{1.25 \times 10^4 P_{\text{Torr}}}{\ln(510 P L_c)}$$

$$L_c = 0.25 a_{\text{eff}} \left(\frac{B_z}{B_T} \right)$$



- W/ preionization: $E_T \frac{B_T}{B_z} \geq 100 \text{ V/m}$
- Purely Ohmic discharges: $E_T \frac{B_T}{B_z} \geq 100 \text{ V/m}$

Examples or required loop electric fields

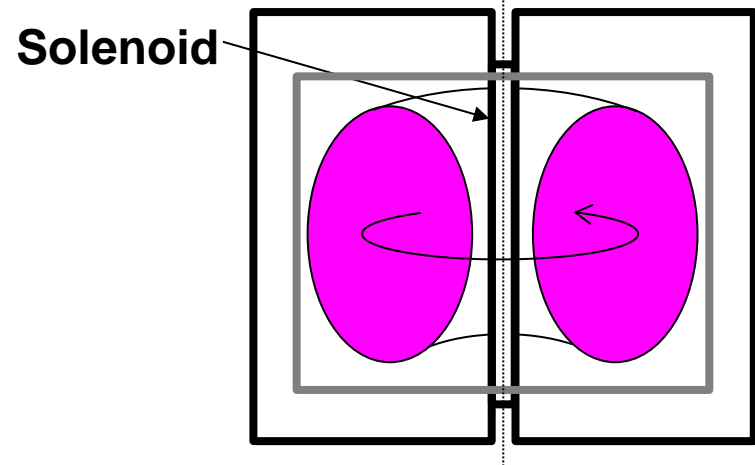
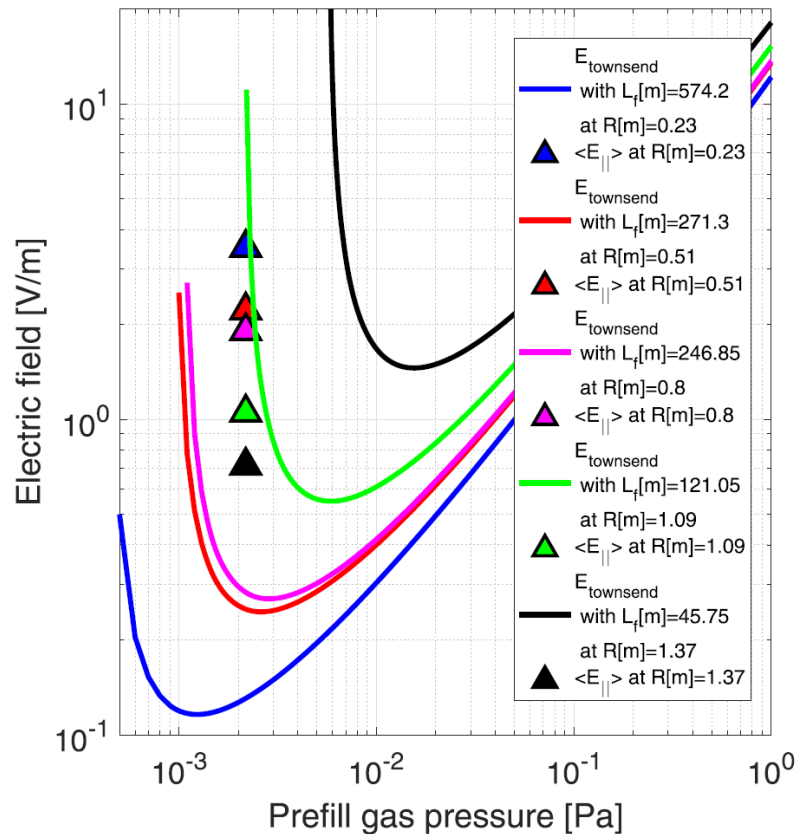


$$E_{BD} > \frac{1.25 \times 10^4 P_{Torr}}{\ln(510 P L_c)}$$

$$L_c = 0.25 a_{eff} \left(\frac{B_z}{B_T} \right)$$

- W/ preionization: $E_T \frac{B_T}{B_z} \geq 100 \text{ V/m}$

- Purely Ohmic discharges: $E_T \frac{B_T}{B_z} \geq 100 \text{ V/m}$



$$V_\phi = -\frac{\partial \phi}{\partial t} \equiv M \frac{\partial I_{CS}}{\partial t}$$

$$E_\phi = -\frac{1}{2\pi r} \frac{\partial \phi}{\partial t}$$

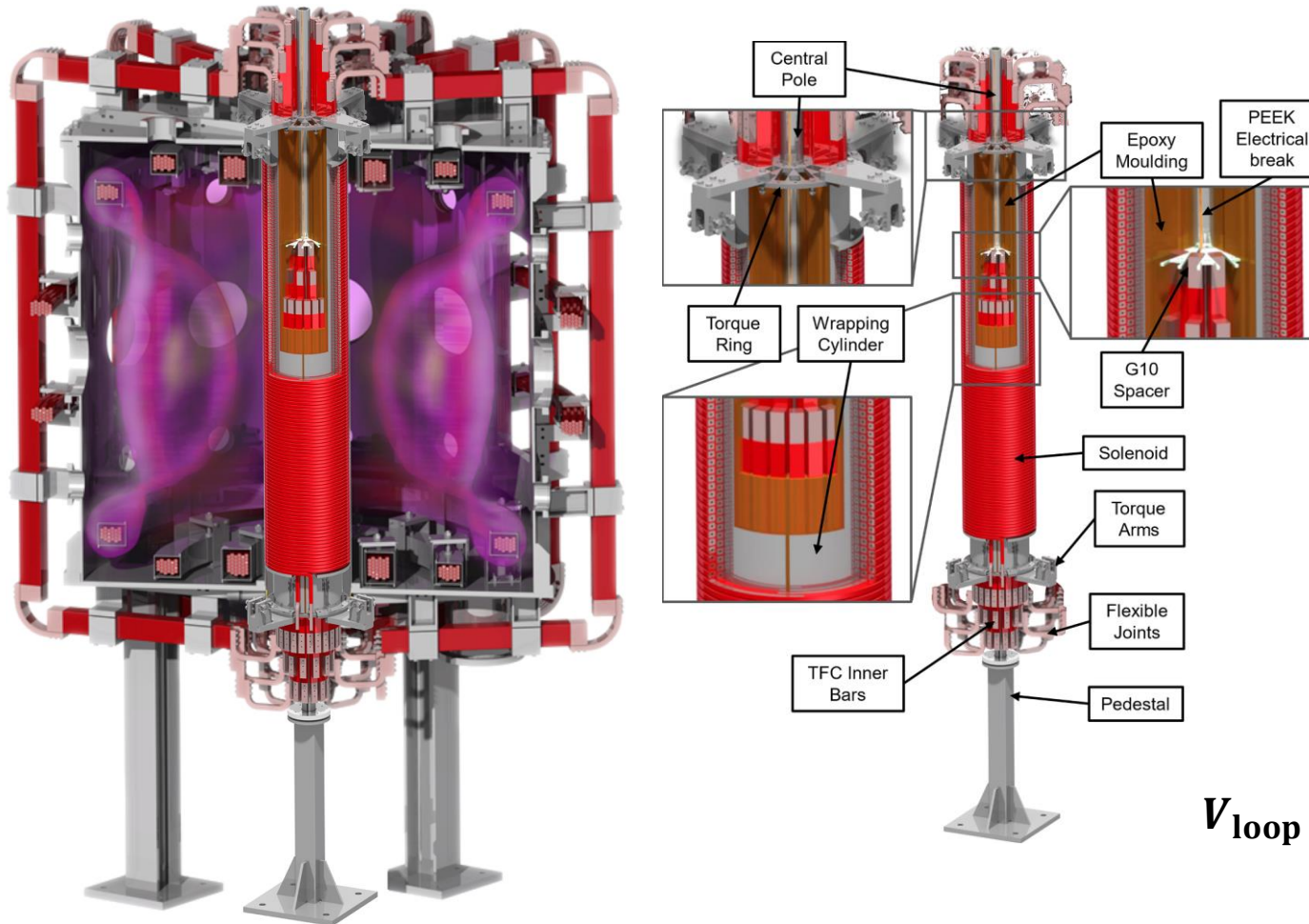
H.-T. Kim, etc., Nucl. Fusion **62**, 126012 (2022)

S. J. Doyle et al, Fusion Eng. Des. **171**, 112706 (2021)

Central solenoid can be used to provide the required loop voltage for breakdown

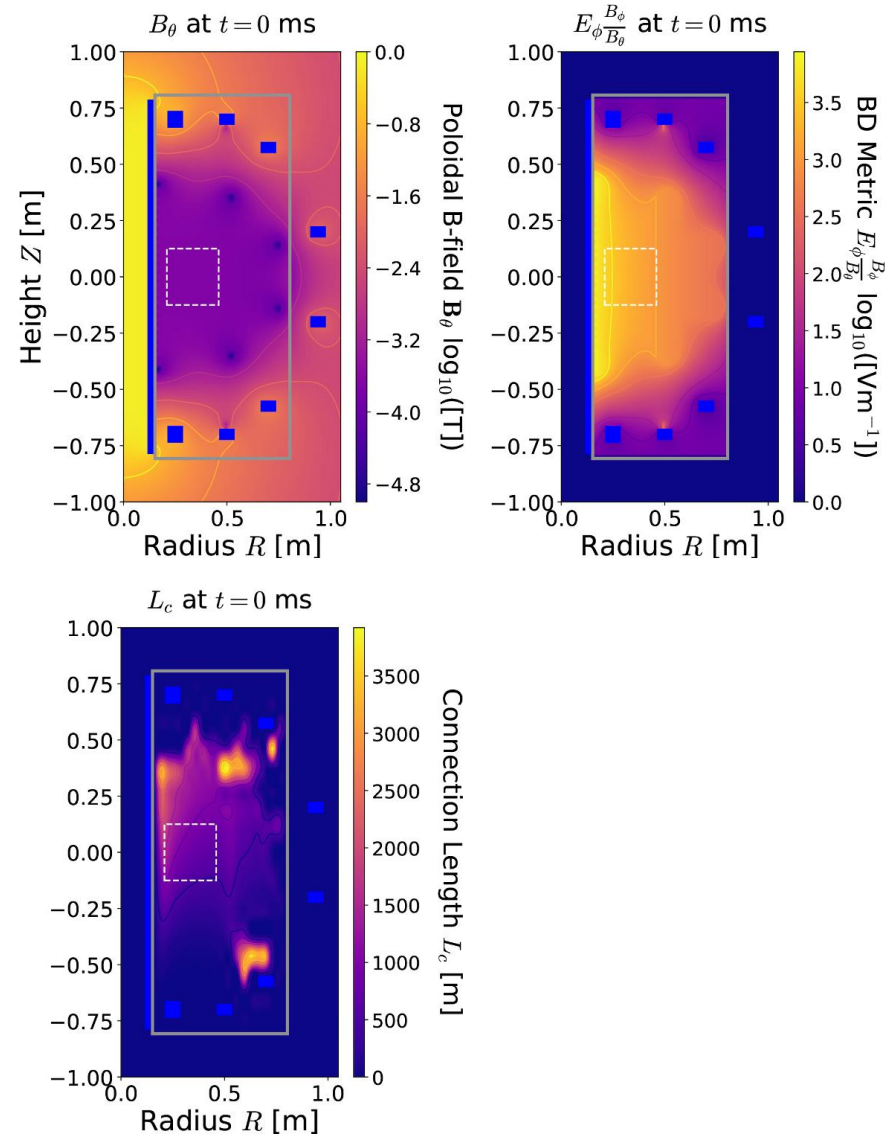


- **SMART:**

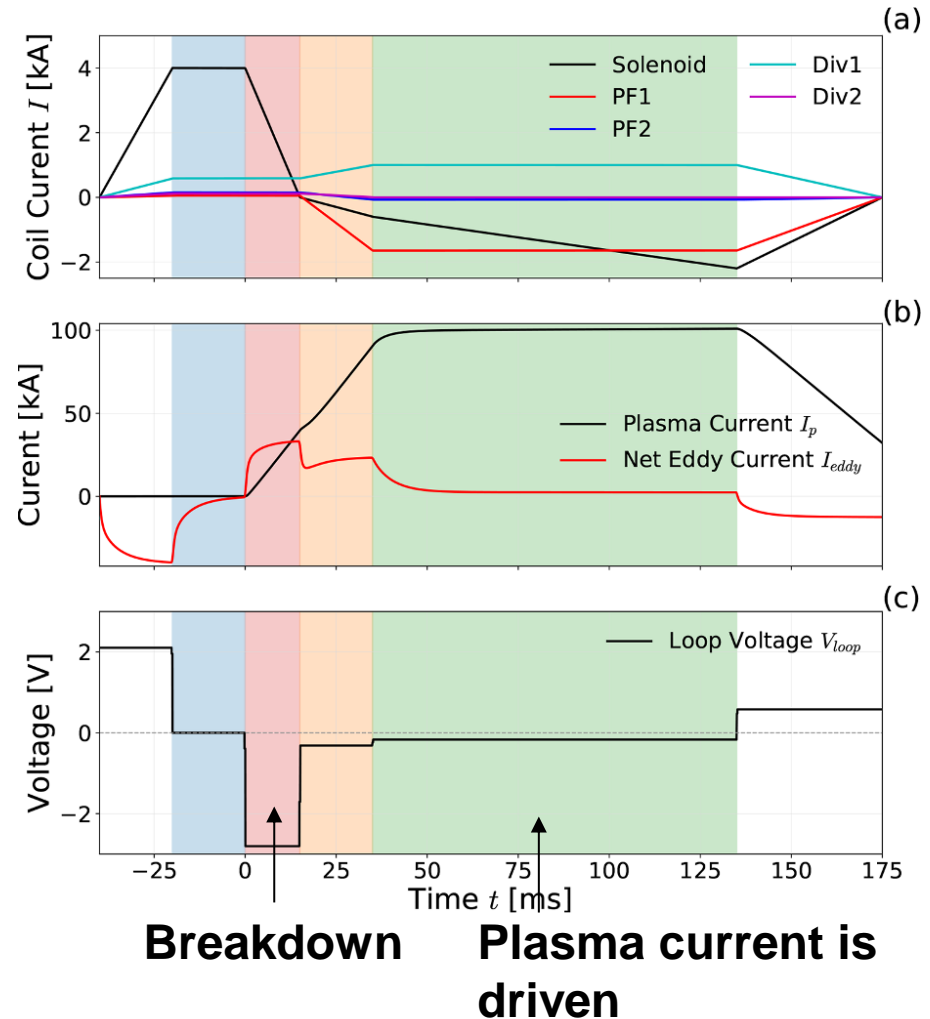


$$V_{\text{loop}} = \frac{A_{\text{sol}} \mu N_{\text{sol}}}{L_{\text{sol}}} \frac{dI_{\text{sol}}}{dt}$$

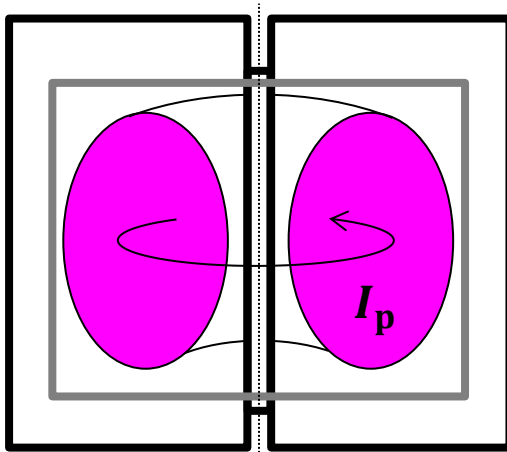
Poloidal coils are used to reduce the stray field during breakdown



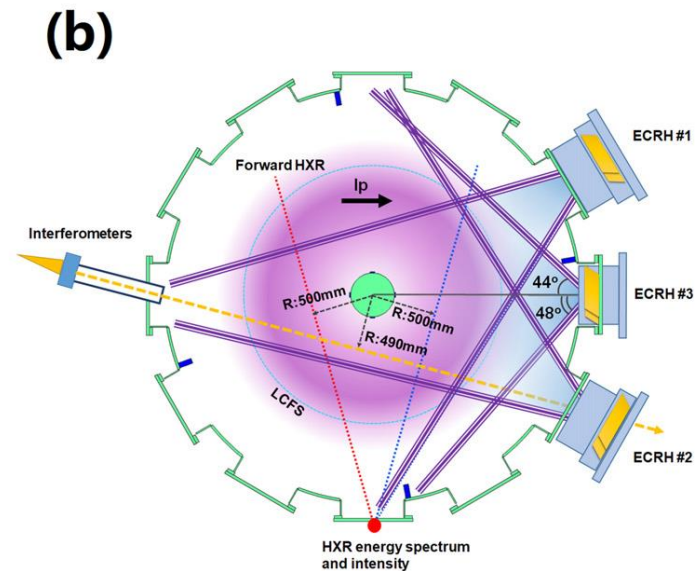
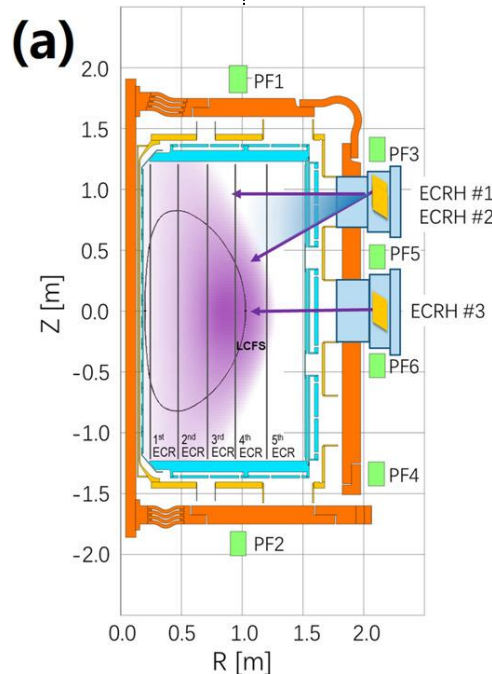
Currents of SMART



Momentum exchange may be needed to drive plasma current



$$\vec{j}_p = \Sigma q n \vec{v} = -en_e \vec{v}_e + en_i \vec{v}_i$$



Solenoid can be used to drive the plasma current

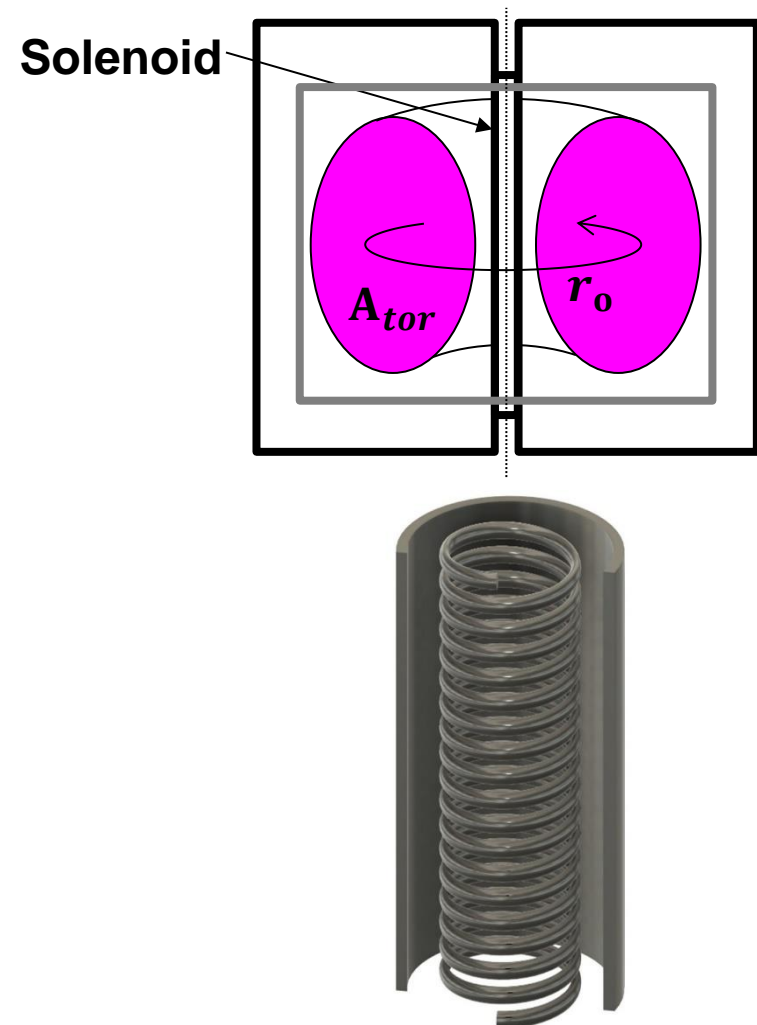


$$L_{\text{tor}} \frac{dI}{dt} + IR = V_{\text{loop}} = M \frac{dI_{\text{sol}}}{dt}$$

$$L_{\text{tor}} = \mu_0 r_0 \left[\ln \left(\frac{8r_0}{a} \right) - 1.5 \right]$$

$$R_{\text{spitzer}} = \eta_{\text{spitzer}} \frac{2\pi r_0}{A_{\text{tor}}}$$

$$\eta_{\text{spitzer}} = 5.2 \times 10^{-3} Z \ln \Lambda T_{e,(\text{eV})}^{-3/2}$$



Current is initially driven at the surface and then diffuses into the plasma



- Simplified Ohm's law: $\vec{E} + \vec{v} \times \vec{B} = \eta \vec{j}$
- Assuming a stationary plasma: $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = \nabla \times (\eta \vec{j})$
- Assuming a constant η :

$$-\frac{\partial}{\partial t} \nabla \times \vec{B} = \eta \nabla \times \nabla \times \vec{j} = \eta (\nabla (\nabla \cdot \vec{j}) - \nabla^2 \vec{j})$$

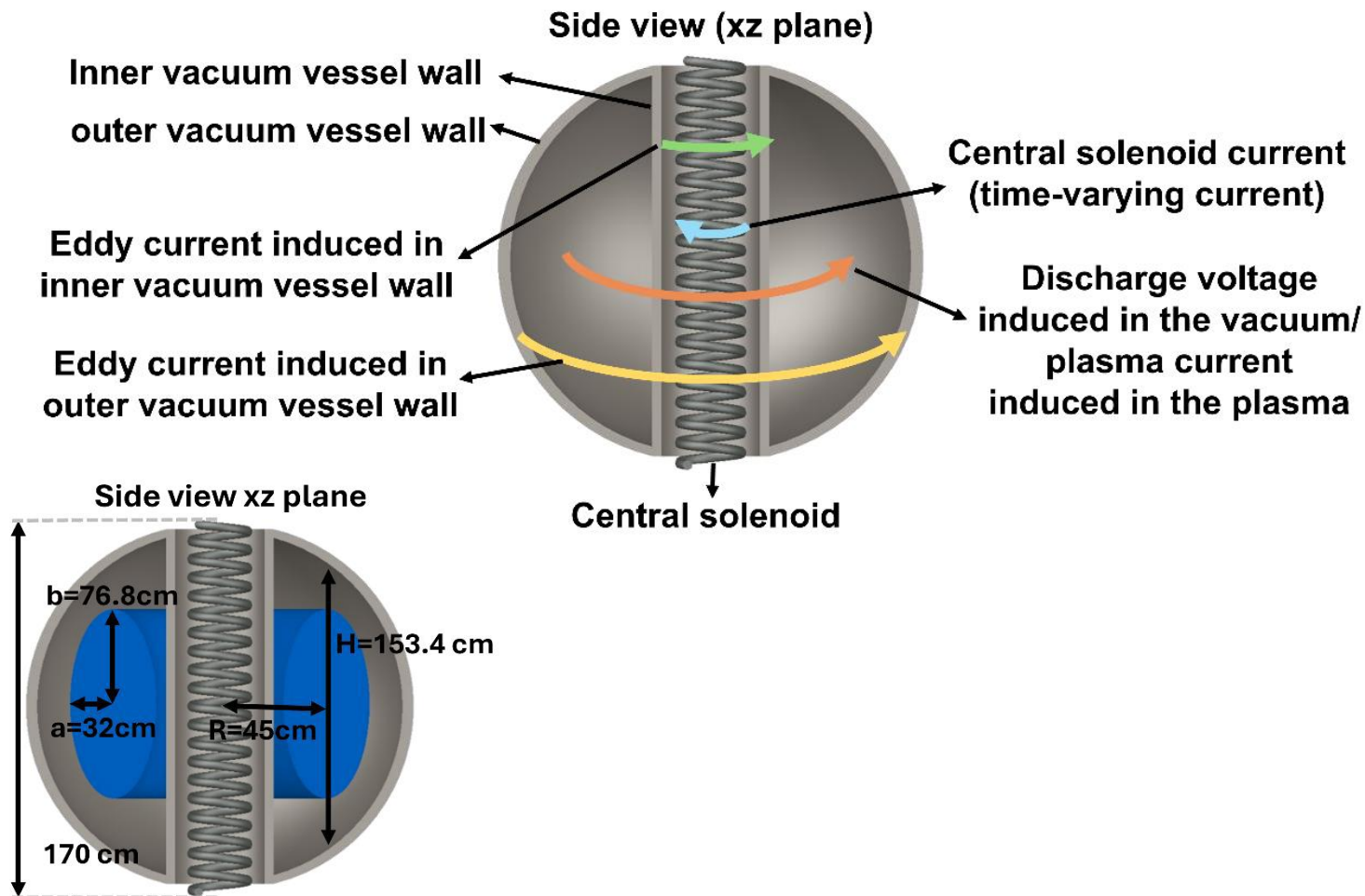
$$\frac{\partial \vec{j}}{\partial t} = \frac{\eta}{\mu_0} \nabla^2 \vec{j}$$

- Assuming non-constant η :

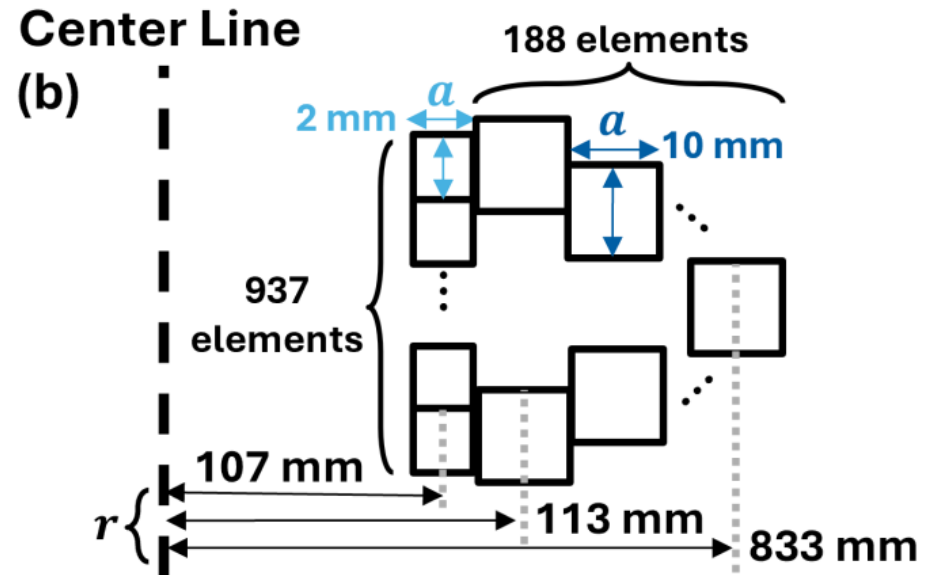
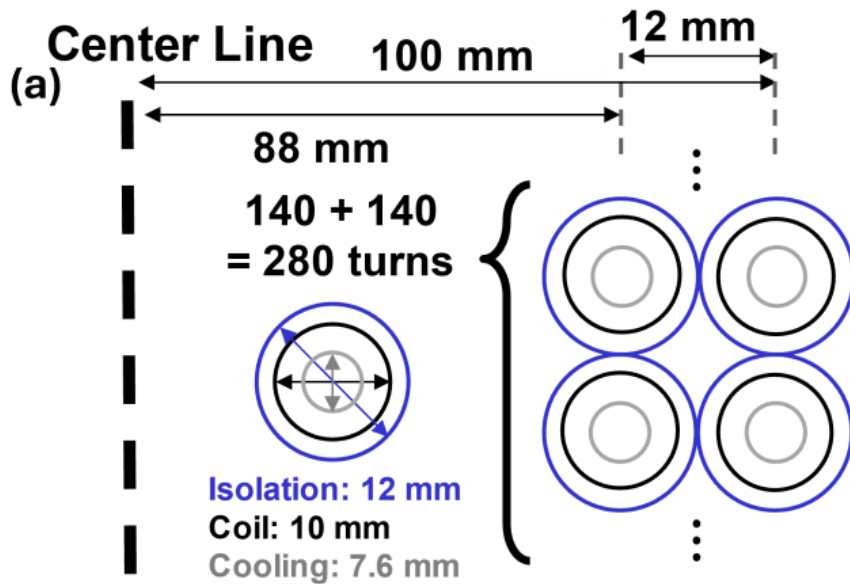
$$\frac{\partial \vec{j}}{\partial t} = \frac{1}{\mu_0} \nabla^2 (\eta \vec{j}) - \nabla [\nabla \cdot (\mu \vec{j})] \qquad \frac{\partial j_T}{\partial t} = \frac{1}{\mu_0} \nabla^2 (\eta j_T)$$

- Since $\eta \propto T^{-3/2}$, resistance drops with higher temperature. The typical limited temperature is ~ 3 keV.

Eddy current needed to be considered



Chamber is broken into ring elements carrying eddy currents



The eddy current in each chamber element is solved numerically

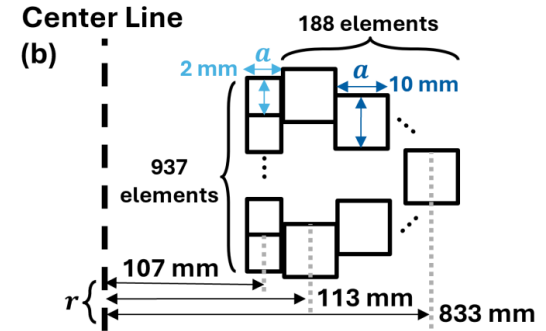


$$\vec{M} \frac{d\vec{I}}{dt} + \vec{R}_\Omega \vec{I} = \vec{V} \quad \vec{M} \frac{\vec{I}' - \vec{I}}{\Delta t} + \vec{R}_\Omega \vec{I} = \vec{V}$$

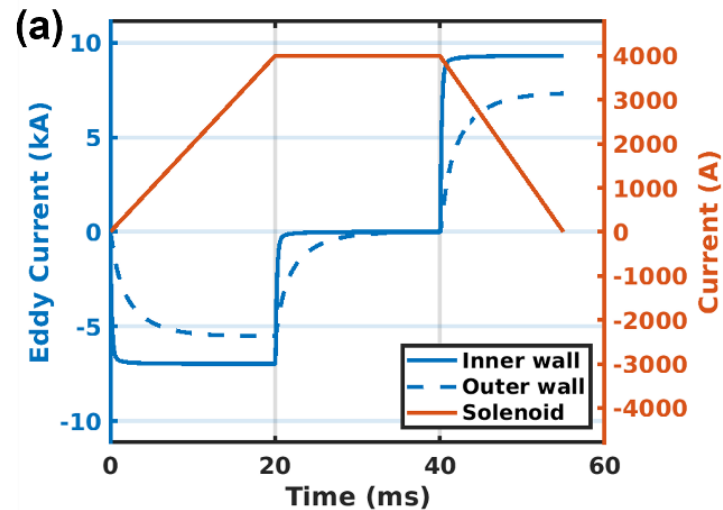
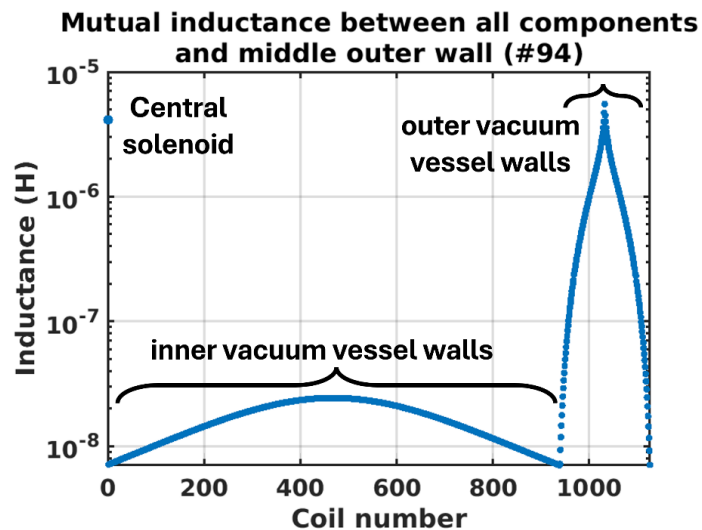
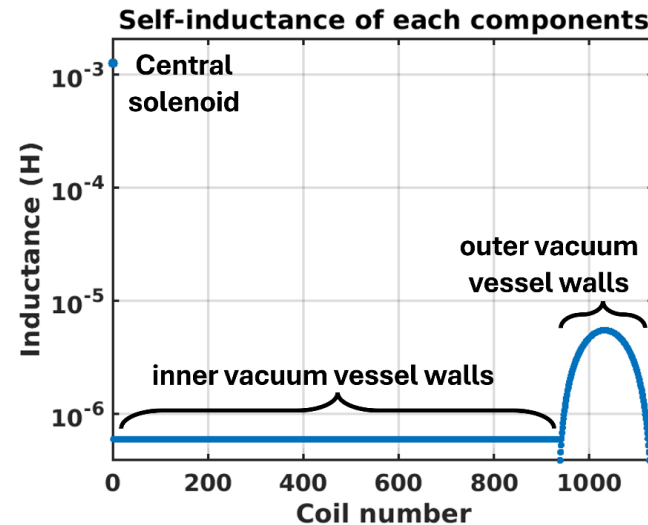
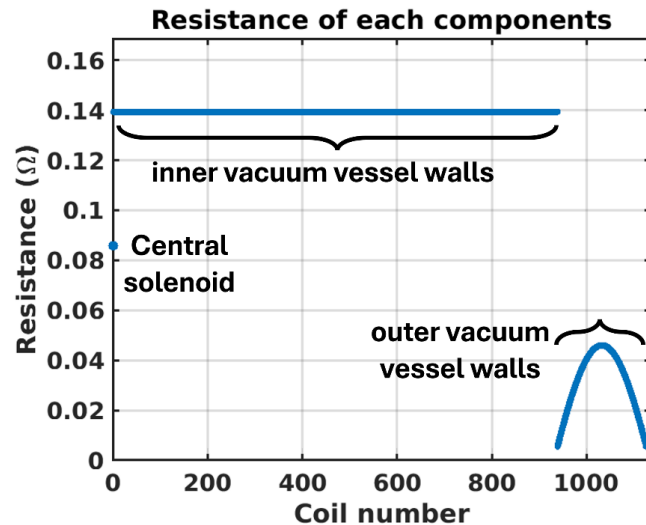
$$\vec{I}' = \left(\vec{1} - \Delta t \vec{M}^{-1} \vec{R}_\Omega \right) \vec{I} + \Delta t \vec{M}^{-1} \vec{V}$$

$$\vec{V} = \vec{M} \frac{d\vec{I}}{dt} + \vec{R}\vec{I}$$

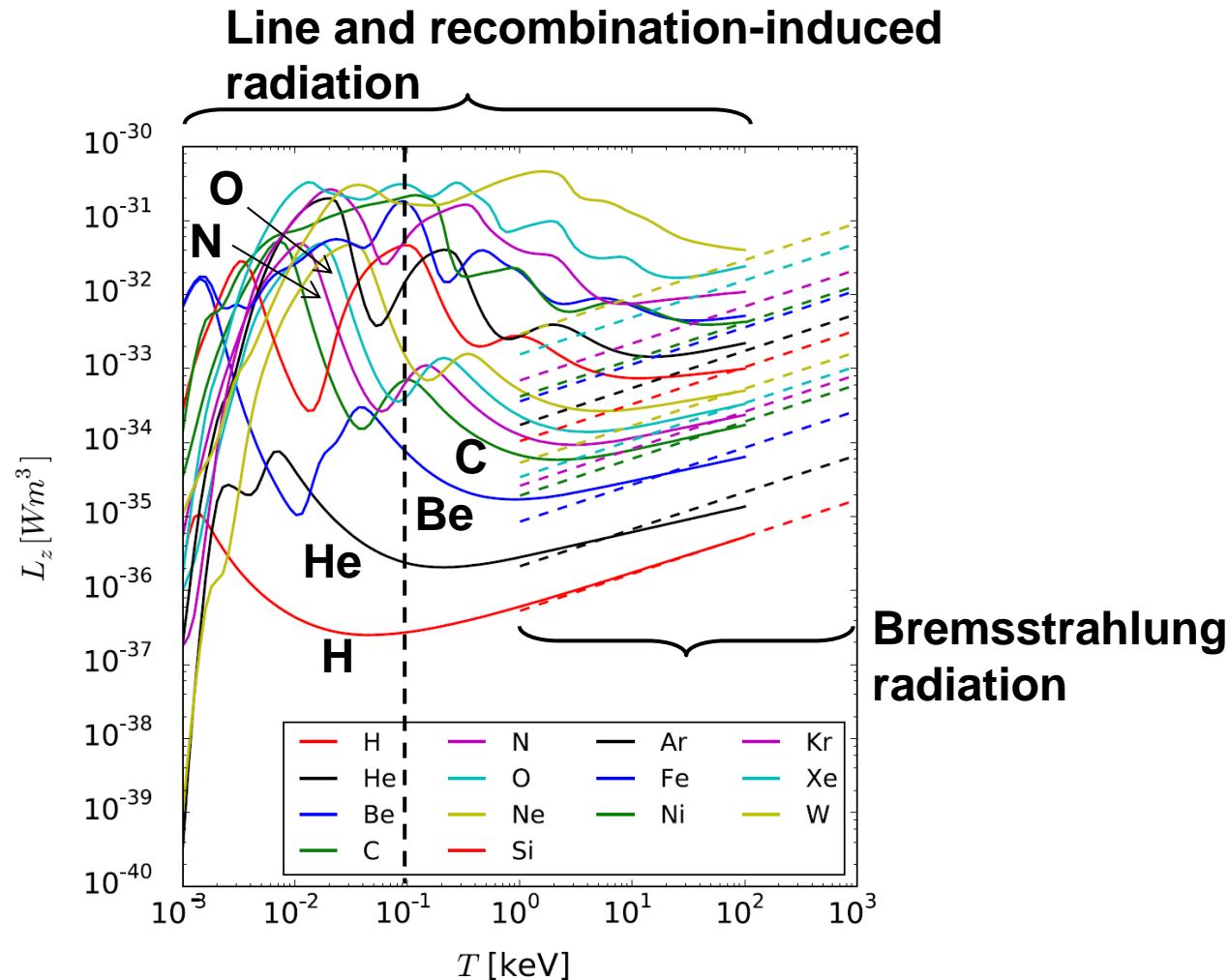
$$\Rightarrow \begin{bmatrix} V_{c1} \\ V_{c2} \\ \vdots \\ V_{v1} \\ V_{v2} \\ \vdots \\ V_p \end{bmatrix} = \begin{bmatrix} L_{c1} & M_{c1,c2} & M_{c1,c3} & \cdots & M_{c1,v1} & M_{c1,v2} & M_{c1,v3} & \cdots & M_{c1,p} \\ M_{c2,c1} & L_{c2} & M_{c2,c3} & \cdots & M_{c2,v1} & M_{c2,v2} & M_{c2,v3} & \cdots & M_{c2,p} \\ M_{c3,c1} & M_{c3,c2} & L_{c3} & \cdots & M_{c3,v1} & M_{c3,v2} & M_{c3,v3} & \cdots & M_{c3,p} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ M_{v1,c1} & M_{v1,c2} & M_{v1,c3} & \cdots & L_{v1} & M_{v1,v2} & M_{v1,v3} & \cdots & M_{v1,p} \\ M_{v2,c1} & M_{v2,c2} & M_{v2,c3} & \cdots & M_{v2,v1} & L_{v2} & M_{v2,v3} & \cdots & M_{v2,p} \\ M_{v3,c1} & M_{v3,c2} & M_{v3,c3} & \cdots & M_{v3,v1} & M_{v3,v2} & L_{v3} & \cdots & M_{v3,p} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ M_{p,c1} & M_{p,c2} & M_{p,c3} & \cdots & M_{p,v1} & M_{p,v2} & M_{p,v3} & \cdots & L_p \end{bmatrix} \begin{bmatrix} I'_{c1} \\ I'_{c2} \\ \vdots \\ I'_{v1} \\ I'_{v2} \\ \vdots \\ I'_p \end{bmatrix} + \begin{bmatrix} R_{c1} & 0 & \cdots & 0 & 0 & \cdots & 0 \\ 0 & R_{c2} & \cdots & 0 & 0 & \cdots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \cdots & R_{v1} & 0 & \cdots & 0 \\ 0 & 0 & \cdots & 0 & R_{v2} & \cdots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \cdots & 0 & 0 & \cdots & R_p \end{bmatrix} \begin{bmatrix} I_{c1} \\ I_{c2} \\ \vdots \\ I_{v1} \\ I_{v2} \\ \vdots \\ I_p \end{bmatrix} \quad (2)$$



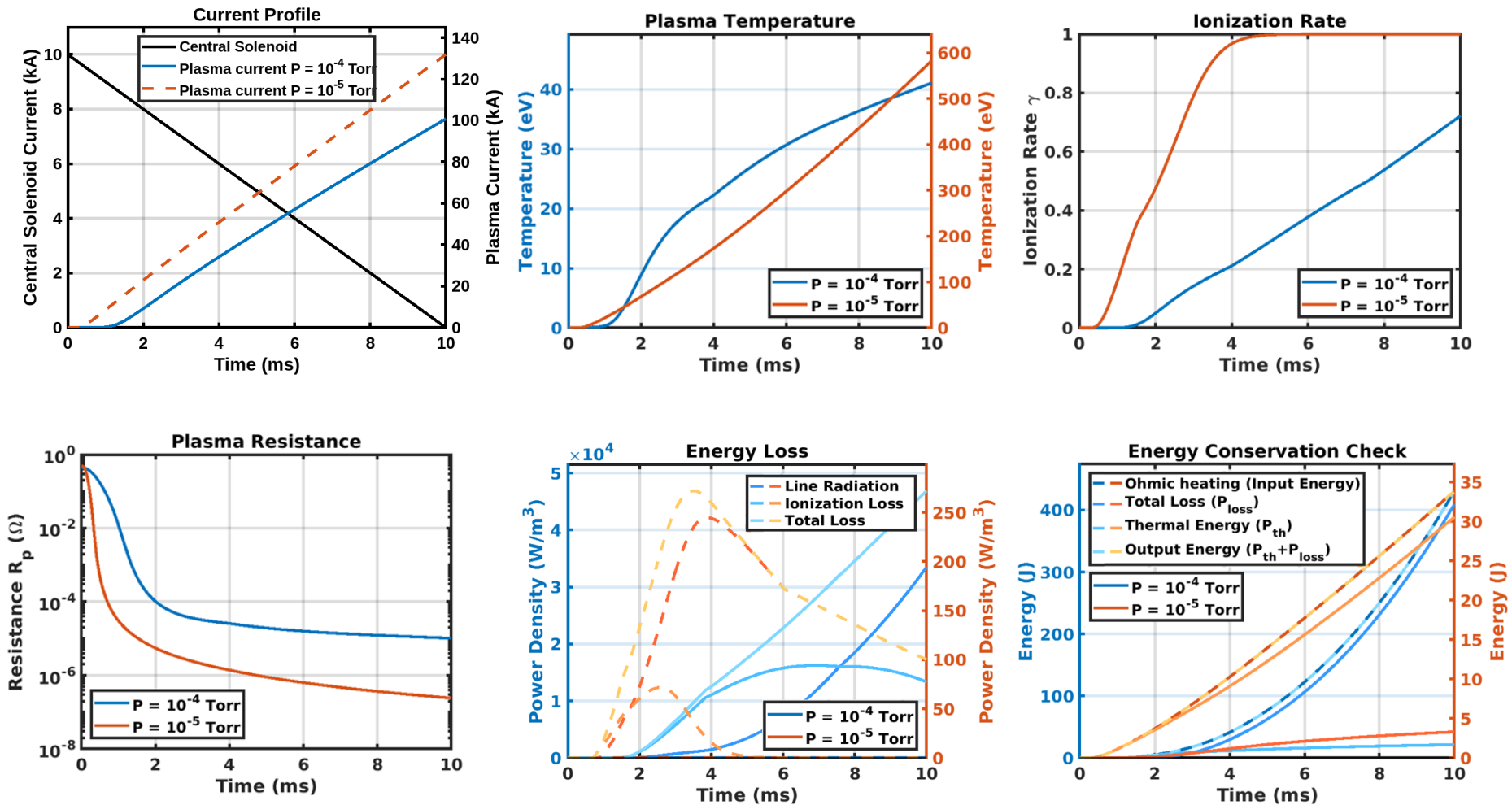
Eddy current on the chamber wall is induced when the current of the solenoid changes with time



Temperature of 100 eV is the threshold of radiation barrier by impurities



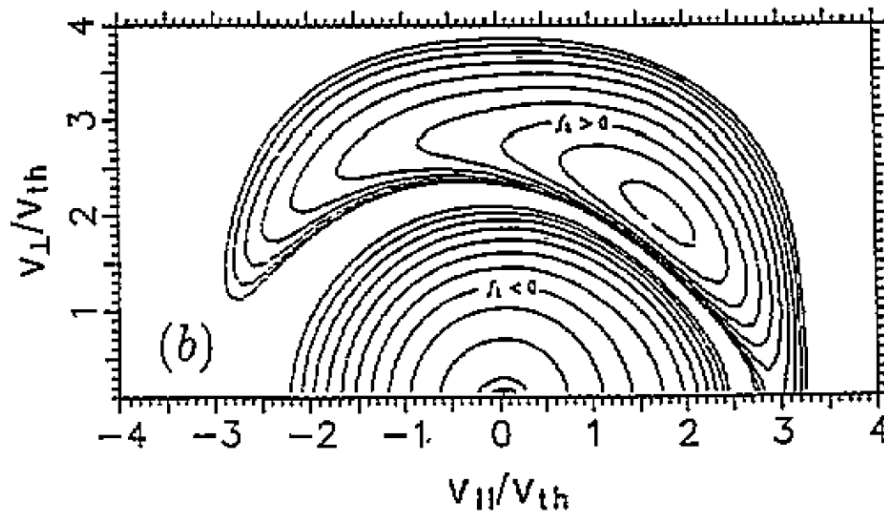
Plasma temperature can be estimated using the simple circuit model



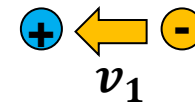
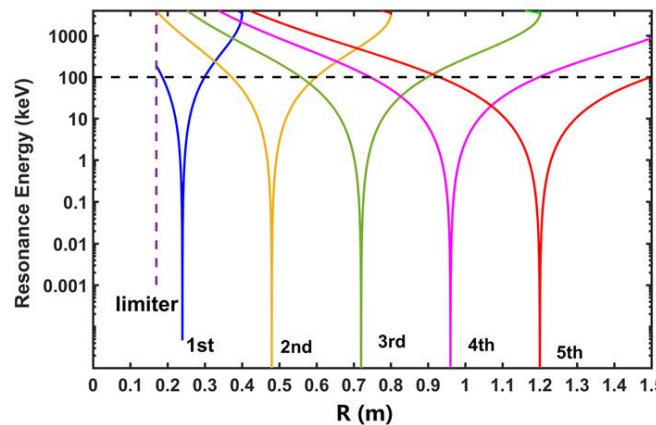
The collisional re-distribution of the ECRH-driven anisotropy in E_{\perp} causes some parallel momentum to flow from e^{-} to ions



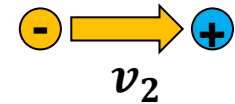
- Coulomb collisions are more efficient at lower energies.



- Electron cyclotron current drive:



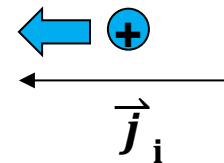
v_1



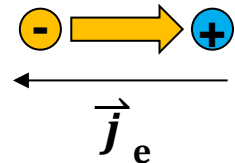
v_2

Velocity: $v_2 > v_1$

Collisions: $v_2 < v_1$



\vec{j}_i



\vec{j}_e

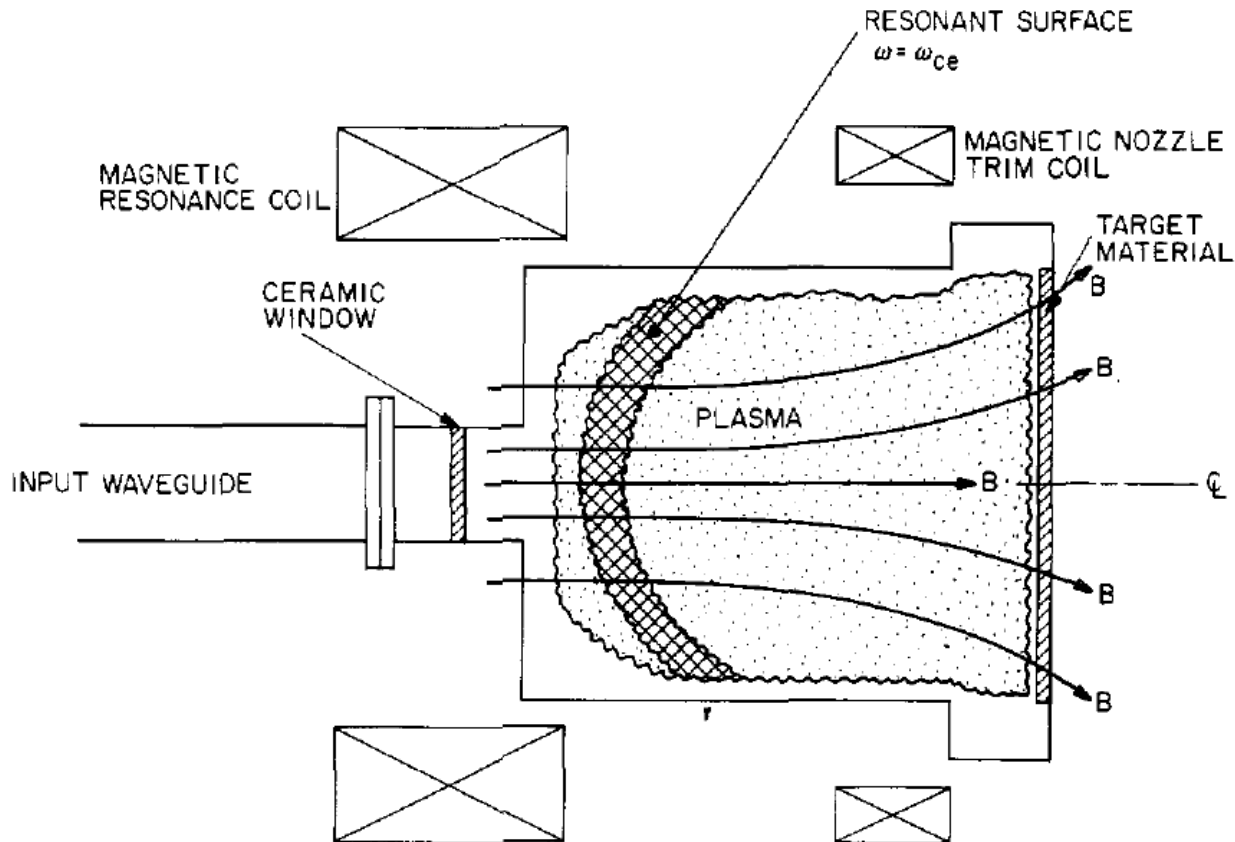
$$\vec{j}_p = -en_e \vec{v}_e + en_i \vec{v}_i$$

$$\vec{P} = n_e m_e \vec{v}_e + n_i m_i \vec{v}_i \approx 0$$

Strong absorption occurs when the frequency matches the electron cyclotron frequency



- Electron cyclotron resonance (ECR) plasma reactor



Electron cyclotron frequency depends on magnetic field only



$$m_e \frac{d\vec{v}}{dt} = -\frac{e}{c} \vec{v} \times \vec{B}$$

- Assuming $\vec{B} = B\hat{z}$ and the electron oscillates in x-y plane

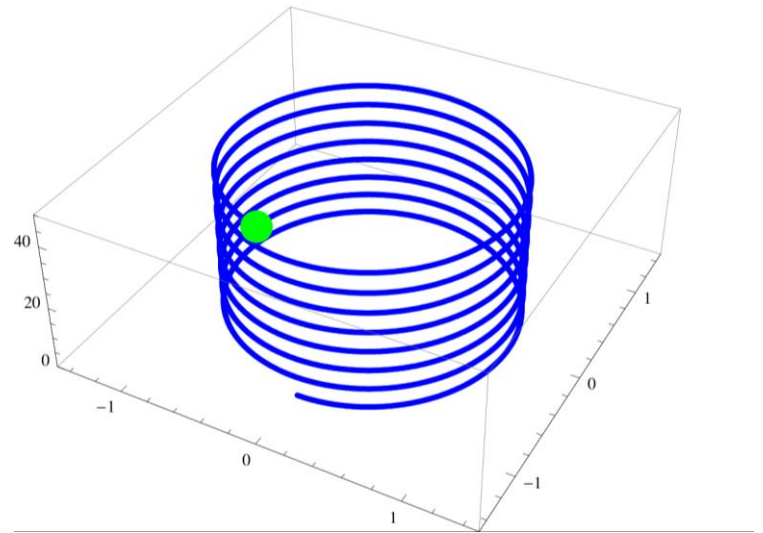
$$\begin{aligned} m_e \dot{v}_x &= -\frac{e}{c} B v_y & m_e \dot{v}_z &= 0 \\ m_e \dot{v}_y &= \frac{e}{c} B v_x \end{aligned}$$

$$\ddot{v}_x = -\frac{eB}{m_e c} \dot{v}_y = -\left(\frac{eB}{m_e c}\right)^2 v_x$$

$$\ddot{v}_y = -\frac{eB}{m_e c} \dot{v}_x = -\left(\frac{eB}{m_e c}\right)^2 v_y$$

- Therefore

$$\omega_{ce} = \frac{eB}{m_e c}$$



Electrons keep getting accelerated when a electric field rotates in electron's gyrofrequency



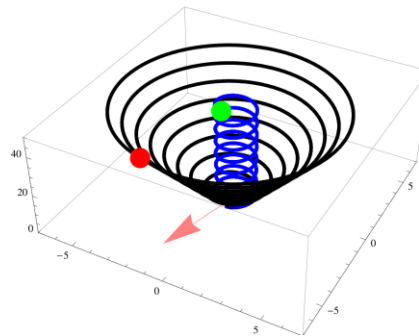
$$m_e \frac{d\vec{v}}{dt} = -\frac{e}{c} \vec{v} \times \vec{B} - e \vec{E} \quad \vec{B} = B_0 \hat{z} \quad \vec{E} = E_0 [\hat{x} \cos(\omega t) + \hat{y} \sin(\omega t)]$$

$$m_e \dot{v}_x = -\frac{e}{c} B v_y + E_0 \cos(\omega t) \quad m_e \dot{v}_y = \frac{e}{c} B v_x + E_0 \sin(\omega t) \quad m_e \dot{v}_z = 0$$

$$\ddot{v}_x = -\frac{eB}{m_e c} \dot{v}_y - \frac{E_0}{m_e} \omega \cos(\omega t) = -\omega_{ce}^2 v_x - \frac{E_0}{m_e} (\omega_{ce} + \omega) \cos(\omega t)$$

$$\ddot{v}_y = -\frac{eB}{m_e c} \dot{v}_x + \frac{E_0}{m_e} \omega \sin(\omega t) = -\omega_{ce}^2 v_y + \frac{E_0}{m_e} (\omega_{ce} + \omega) \sin(\omega t)$$

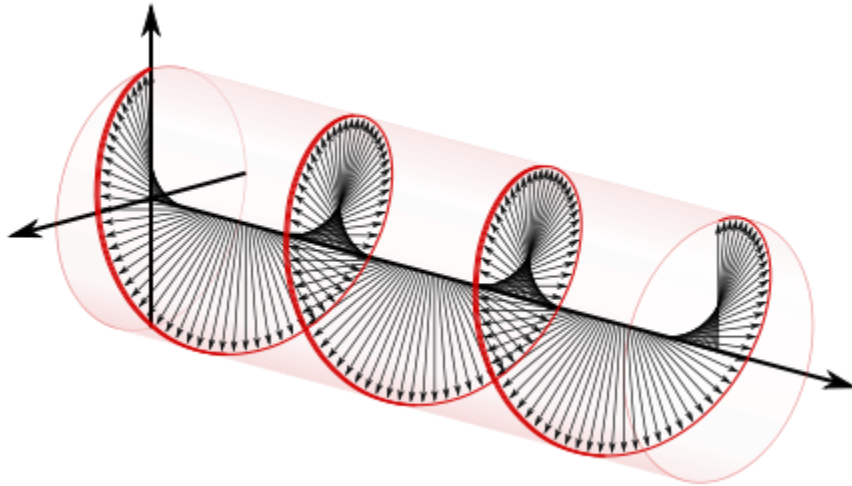
$$\omega_{ce} = \frac{eB}{m_e c}$$



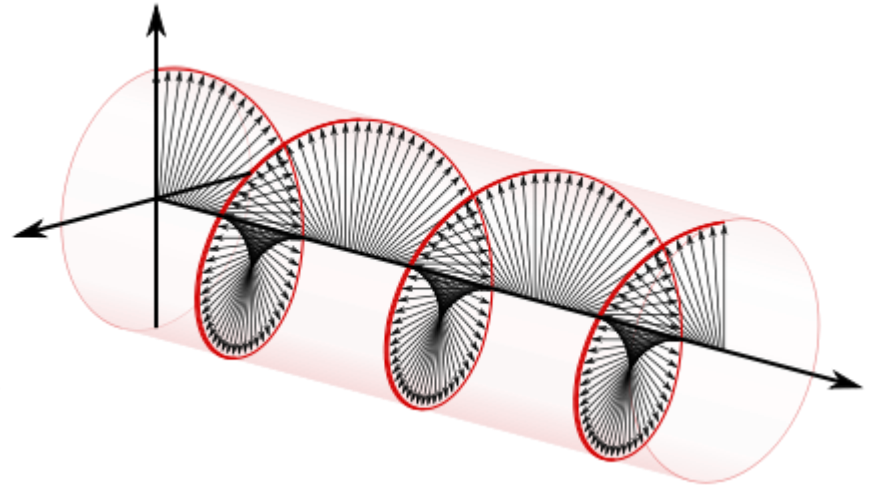
Electric field in a circular polarized electromagnetic wave keeps rotating as the wave propagates



- Right-handed polarization



- Left-handed polarization



Only right-handed polarization can resonance with electron's gyromotion

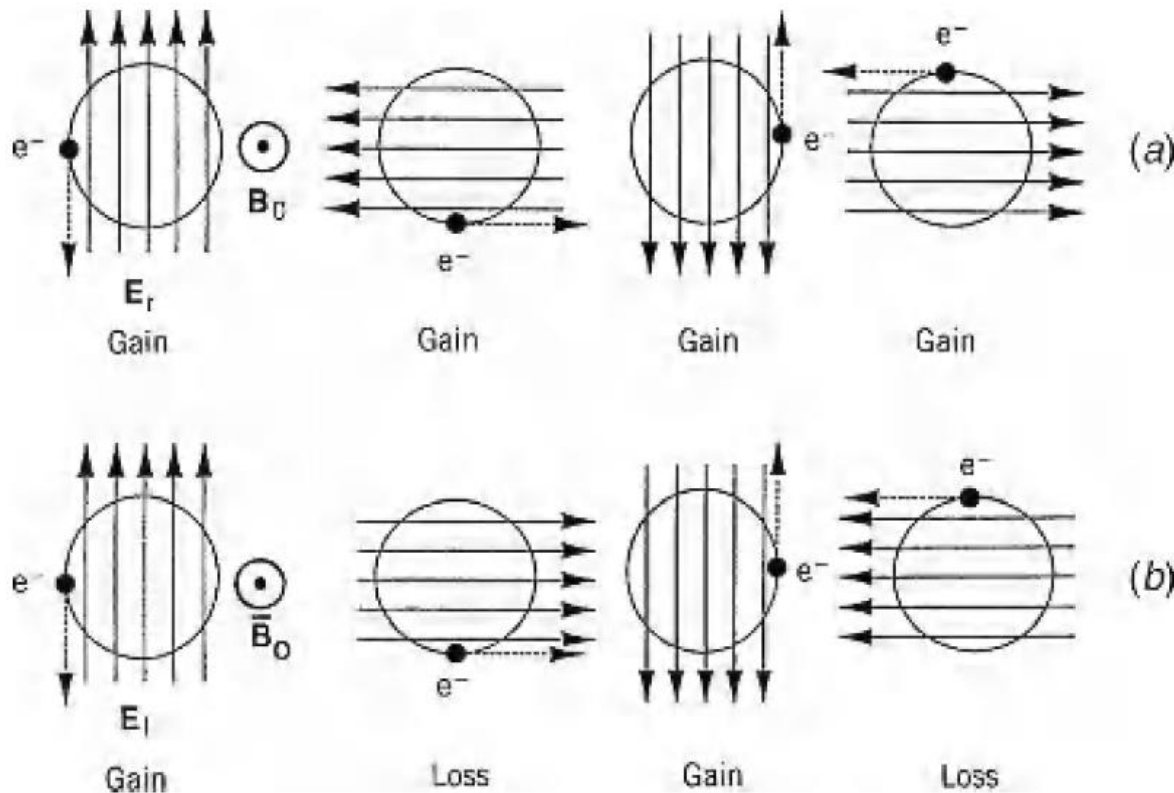
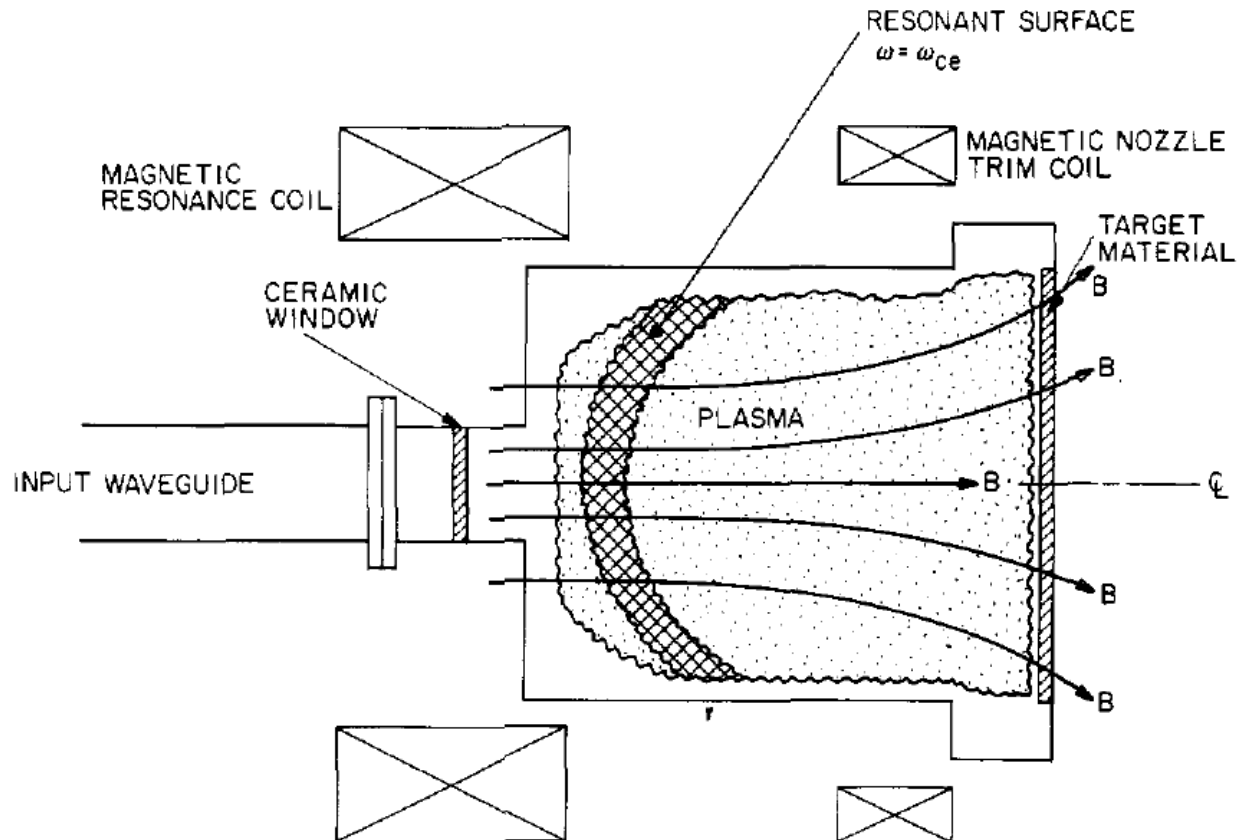


FIGURE 13.5. Basic principle of ECR heating: (a) continuous energy gain for right-hand polarization; (b) oscillating energy for left-hand polarization (after Lieberman and Gottscho, 1994).

Strong absorption occurs when the frequency matches the electron cyclotron frequency



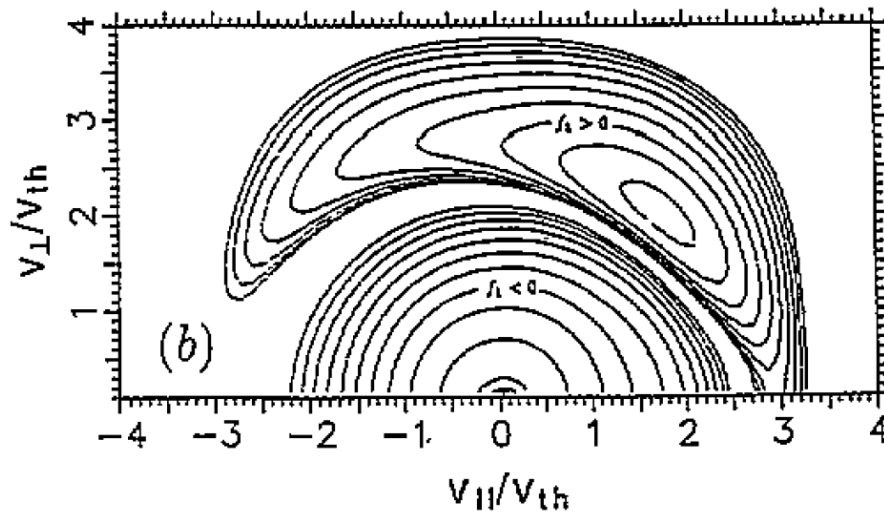
- Electron cyclotron resonance (ECR) plasma reactor



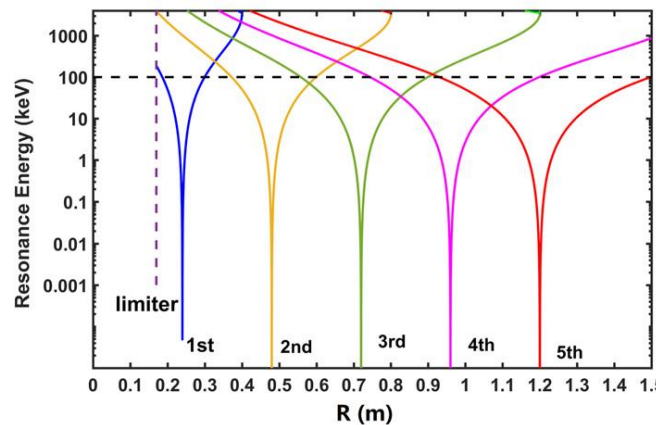
The collisional re-distribution of the ECRH-driven anisotropy in E_{\perp} causes some parallel momentum to flow from e^{-} to ions



- Coulomb collisions are more efficient at lower energies.

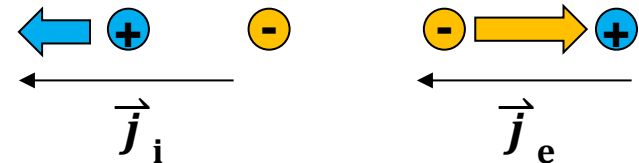


- Electron cyclotron current drive:



Velocity: $v_2 > v_1$

Collisions: $v_2 < v_1$



$$\vec{j}_p = -en_e \vec{v}_e + en_i \vec{v}_i$$

$$\vec{P} = n_e m_e \vec{v}_e + n_i m_i \vec{v}_i \approx 0$$

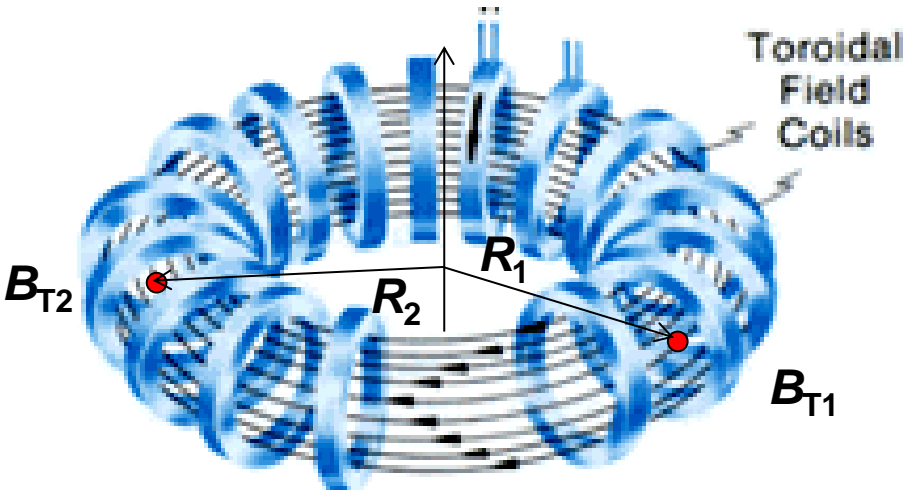
With poloidal fields, charged particles see nonuniform toroidal magnetic field



- W/o poloidal field

$$R_1 = R_2$$

$$B_{T1} = B_{T2}$$



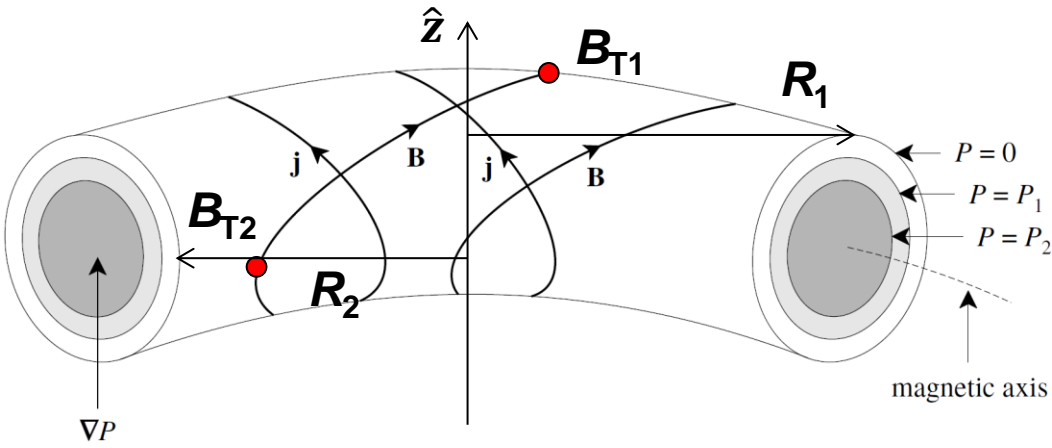
$$B_T \propto \frac{1}{R}$$

$$B_T \gg B_p$$

- W/ poloidal field

$$R_1 > R_2$$

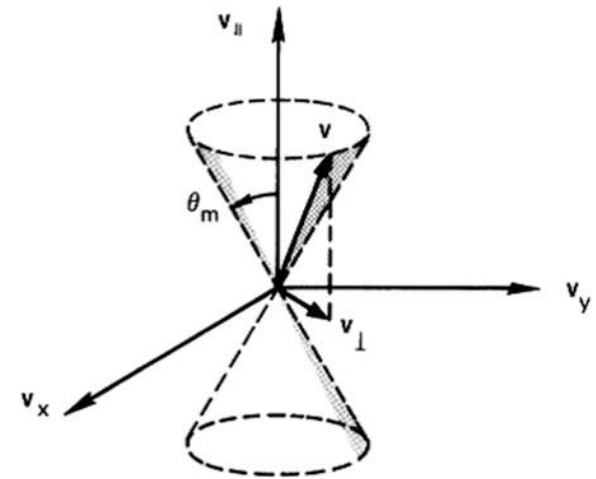
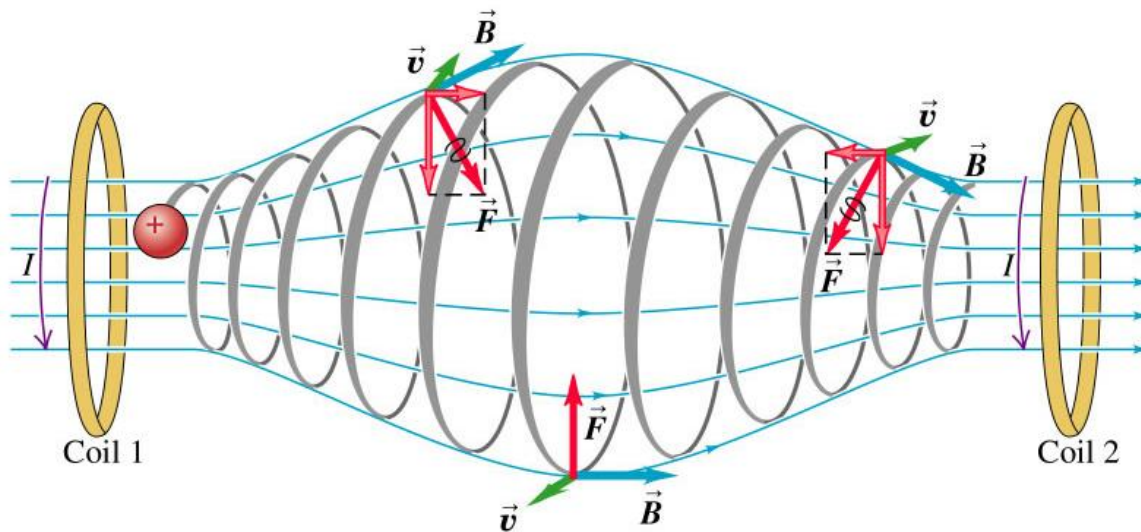
$$B_{T1} < B_{T2}$$



Charged particles can be partially confined by a magnetic mirror machine



- Charged particles with small v_{\parallel} eventually stop and are reflected while those with large v_{\parallel} escape.



$$\frac{1}{2}mv^2 = \frac{1}{2}mv_{\parallel}^2 + \frac{1}{2}mv_{\perp}^2 \quad \text{Invariant: } \mu \equiv \frac{1}{2} \frac{mv_{\perp}^2}{B}$$

$$v_{\perp}^{\prime 2} = v_{\perp o}^2 + v_{\parallel o}^2 \equiv v_o^2$$

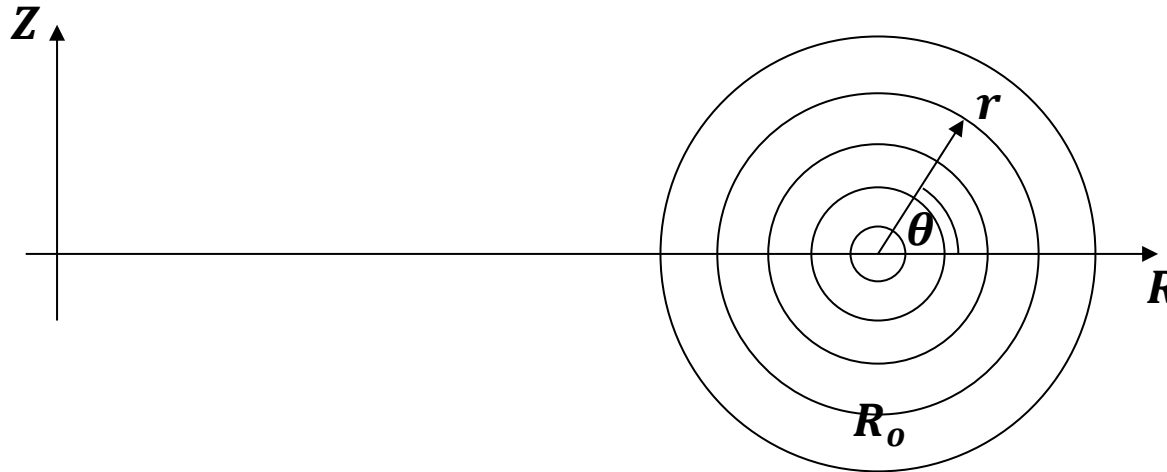
$$\frac{B_o}{B'} = \frac{v_{\perp o}^2}{v_{\perp}^{\prime 2}} = \frac{v_{\perp o}^2}{v_o^2} \equiv \sin^2 \theta$$

$$\frac{B_o}{B_m} \equiv \frac{1}{R_m} = \sin^2 \theta_m$$

- Large v_{\parallel} may occur from collisions between particles.

Those confined charged particle are eventually lost due to collisions.

Parallel velocity changes when particles follow field the field line



$$R \gg r$$

$$B_T \gg B_p$$

$$R = R_0 + r \cos \theta = R_0(1 + \epsilon \cos \theta)$$

Inverse aspect ratio:

$$\epsilon \equiv \frac{r}{R_0}$$

$$B \simeq \frac{B_0}{1 + \epsilon \cos \theta} \simeq B_0(1 - \epsilon \cos \theta)$$

Invariant: $\mu \equiv \frac{1}{2} \frac{mv_{\perp}^2}{B}$

$$\frac{v_{\perp}^2}{B_0(1 - \epsilon \cos \theta)} = \frac{v_{\perp 0}^2}{B_0(1 - \epsilon)} \quad v_{\perp}^2 = \frac{v_{\perp 0}^2(1 - \epsilon \cos \theta)}{1 - \epsilon}$$

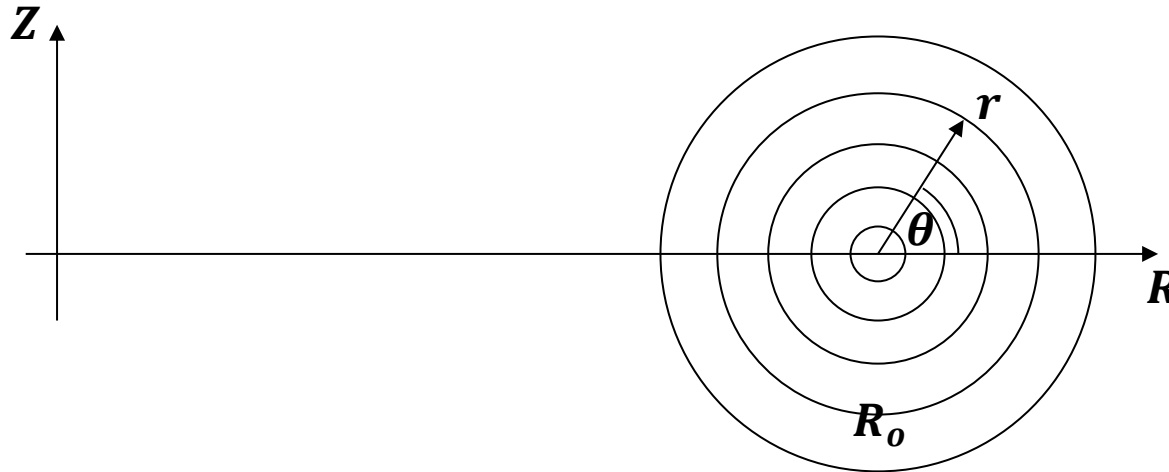
$$v^2 = v_{\perp}^2 + v_{\parallel}^2 = v_{\perp 0}^2 + v_{\parallel 0}^2$$

$$v_{\parallel}^2 = v^2 \left(1 - \frac{v_{\perp}^2}{v^2} \right)$$

$$v_{\parallel}^2 = v^2 \left[1 - \frac{v_{\perp 0}^2}{v^2} \frac{(1 - \epsilon \cos \theta)}{1 - \epsilon} \right]$$

$$\approx v^2 \left\{ 1 - \frac{v_{\perp 0}^2}{v^2} \left[1 + 2\epsilon \sin^2 \left(\frac{\theta}{2} \right) \right] \right\}$$

Particles may be trapped by nonuniform magnetic field



$$R \gg r$$
$$B_T \gg B_p$$

$$\epsilon \equiv \frac{r}{R_0}$$

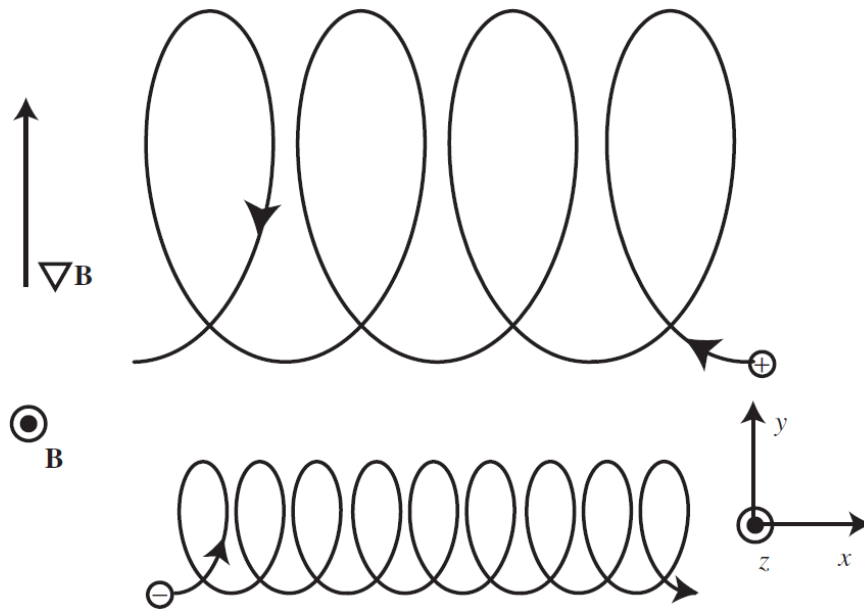
$$v_{||}^2 \approx v^2 \left\{ 1 - \frac{v_{\perp 0}^2}{v^2} \left[1 + 2\epsilon \sin^2 \left(\frac{\theta}{2} \right) \right] \right\}$$

- For $v_{||}^2 \geq 0$, particles are passing.
- For $v_{||}^2 \leq 0$, particles are trapped.

Charge particles drift across magnetic field lines when the magnetic field is not uniform or curved

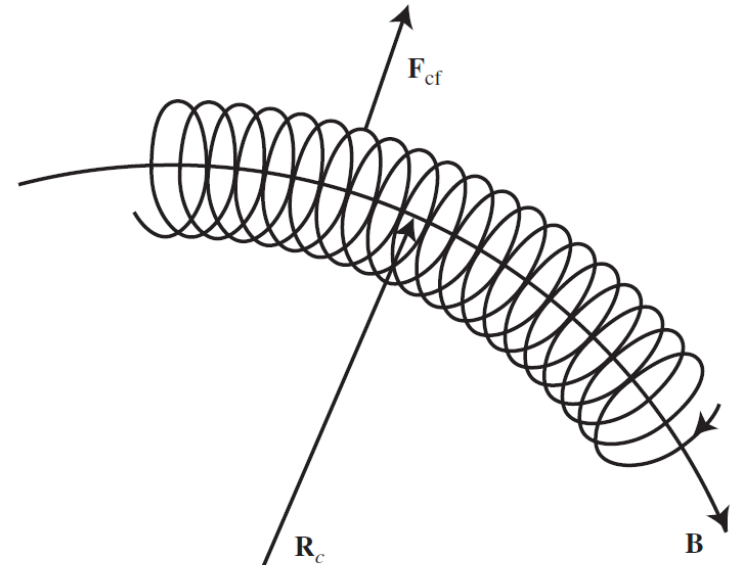


- Gradient-B drift



$$\vec{v}_{\nabla} = \frac{mv_{\perp}^2}{2q} \frac{\vec{B} \times \nabla B}{B^3}$$

- Curvature drift



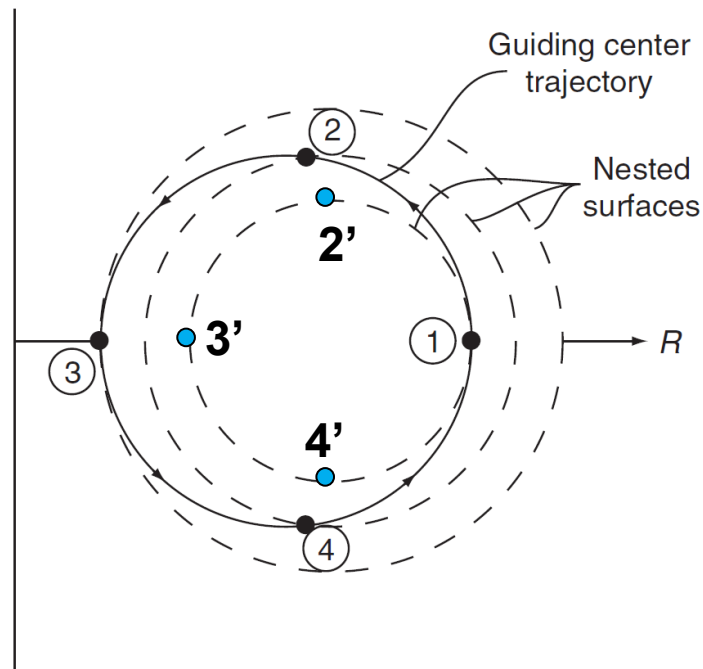
$$\vec{v}_R = \frac{mv_{\parallel}^2}{2q} \frac{\vec{R}_c \times \vec{B}}{R_c B^2}$$

$$\vec{v}_{\text{total}} = \vec{v}_R + \vec{v}_{\nabla} = \frac{\vec{B} \times \nabla B}{\omega_c B^2} \left(v_{\parallel}^2 + \frac{1}{2} v_{\perp}^2 \right) = \frac{m}{q} \frac{\vec{R}_c \times \vec{B}}{R_c^2 B^2} \left(v_{\parallel}^2 + \frac{1}{2} v_{\perp}^2 \right)$$

For passing particles, they drift back to the original position with a “semicircle” orbit



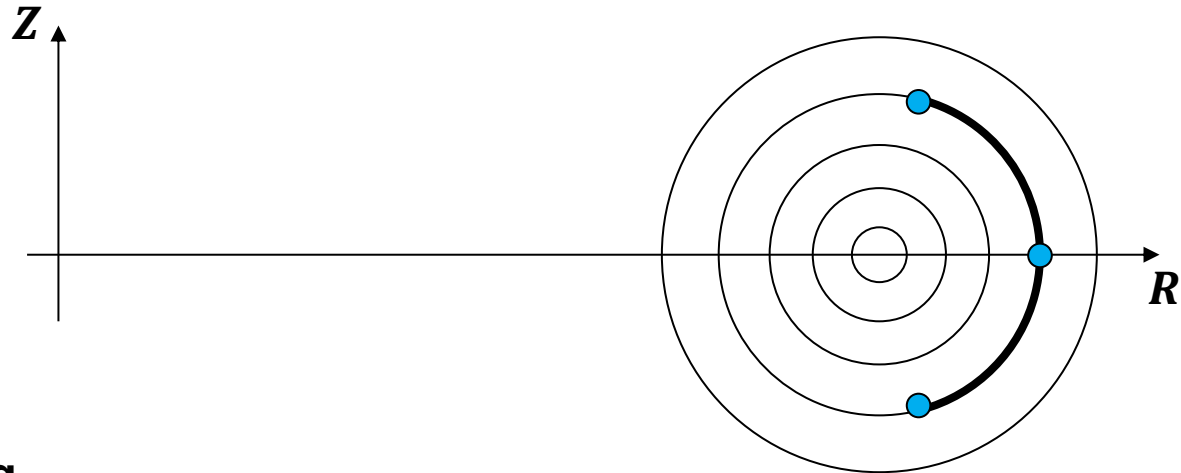
$$\vec{v}_{\text{total}} = \vec{v}_R + \vec{v}_\nabla = \frac{\vec{B} \times \nabla B}{\omega_c B^2} \left(v_{\parallel}^2 + \frac{1}{2} v_{\perp}^2 \right) = \frac{m}{q} \frac{\vec{R}_c \times \vec{B}}{R_c^2 B^2} \left(v_{\parallel}^2 + \frac{1}{2} v_{\perp}^2 \right)$$



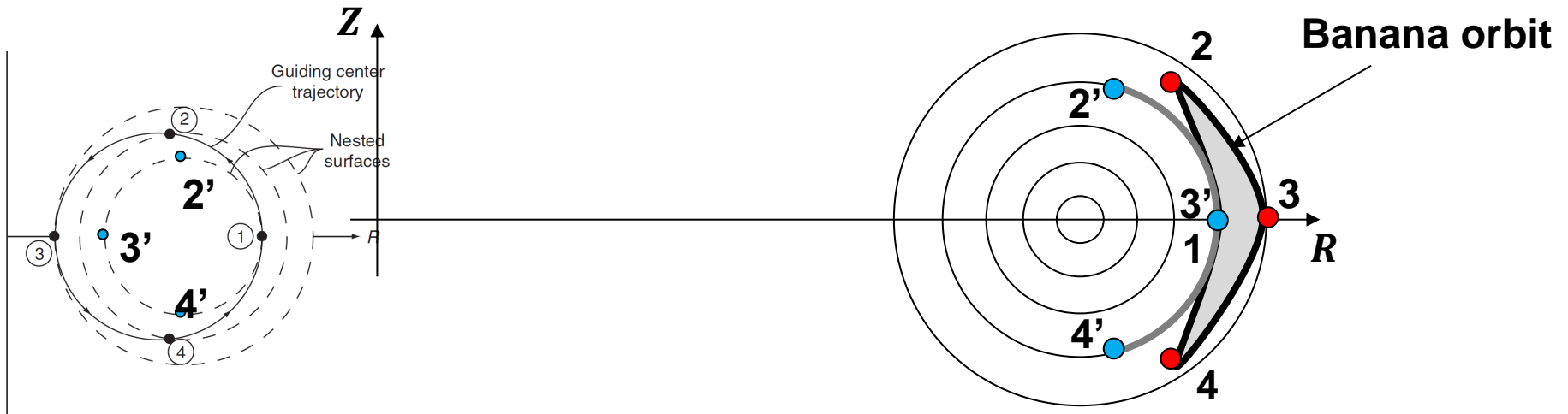
For trapped particles, they drift back to the original position with a banana orbit



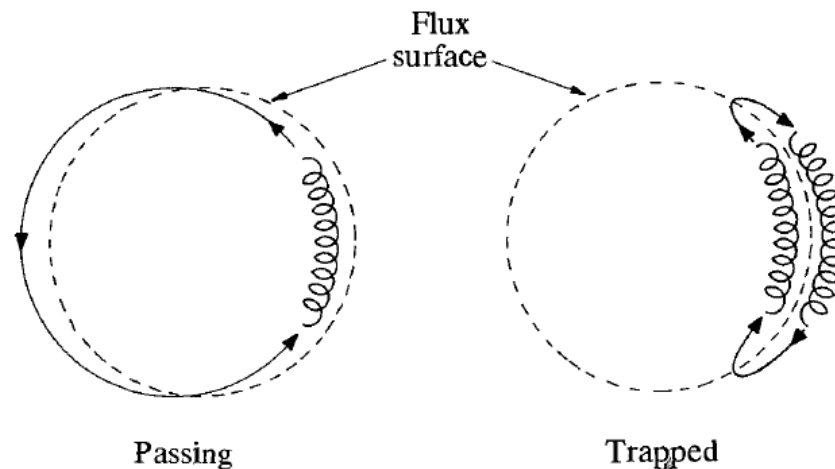
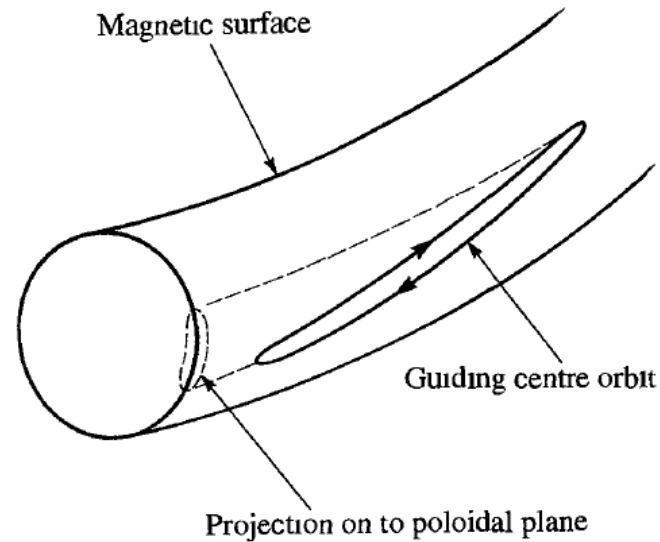
- W/o drifting



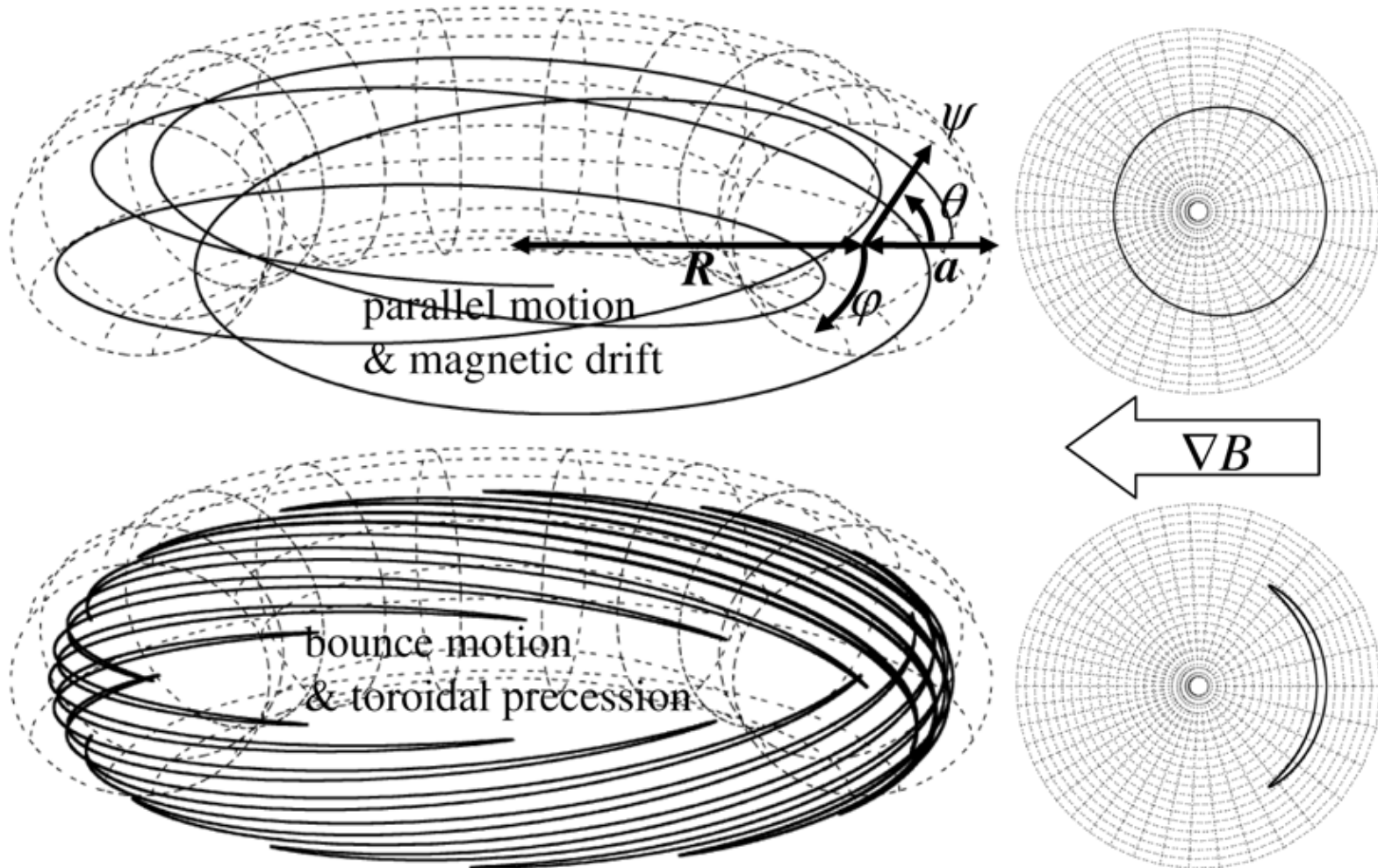
- W/ drifting



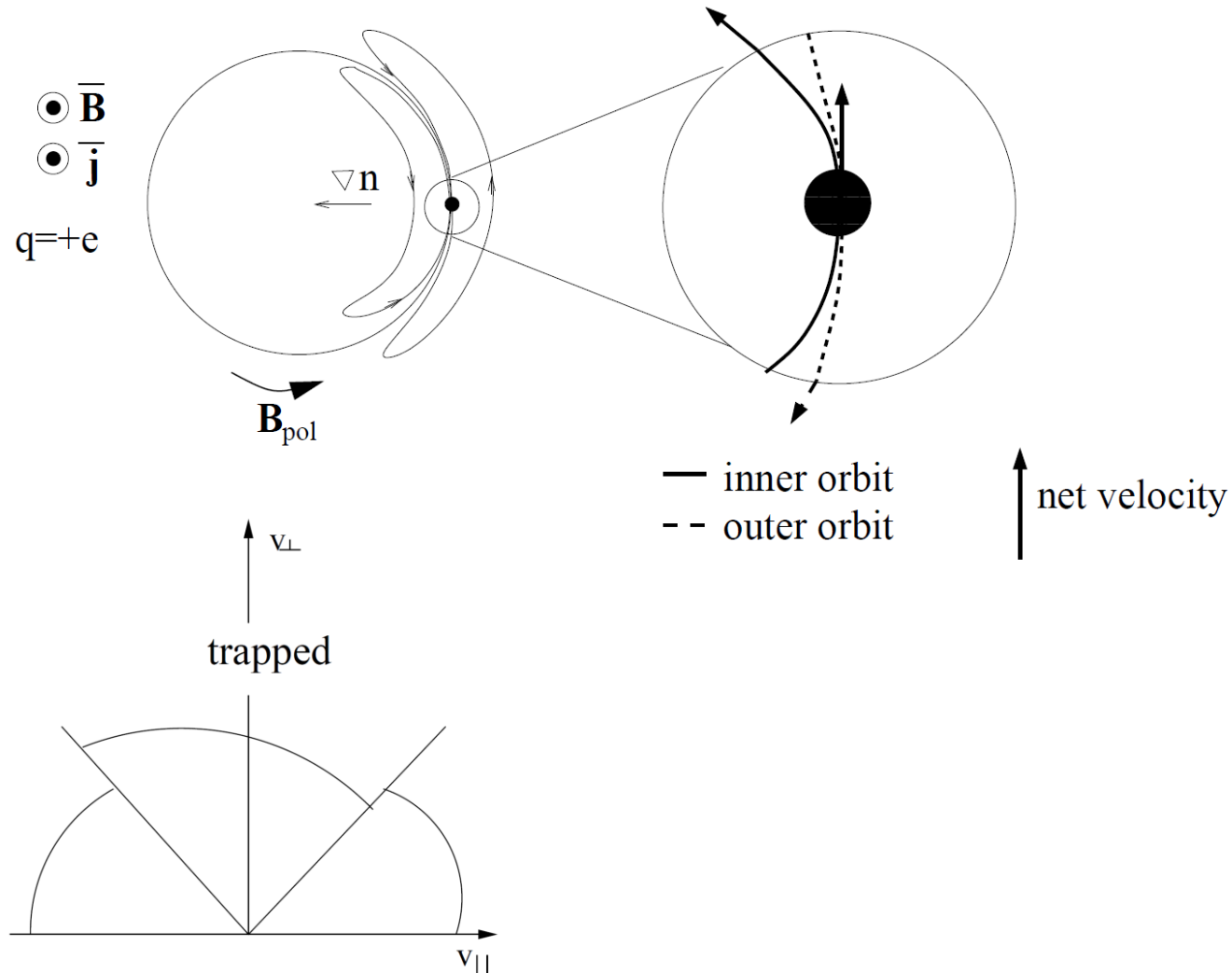
Trajectories of charged particles



The trajectories of charged particles follow the toroidal field lines



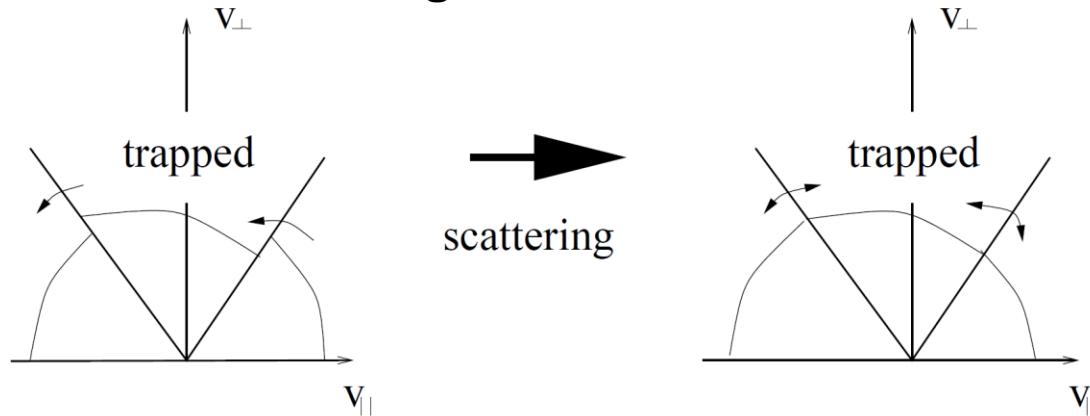
A banana current is generated when there is a pressure gradient in the plasma



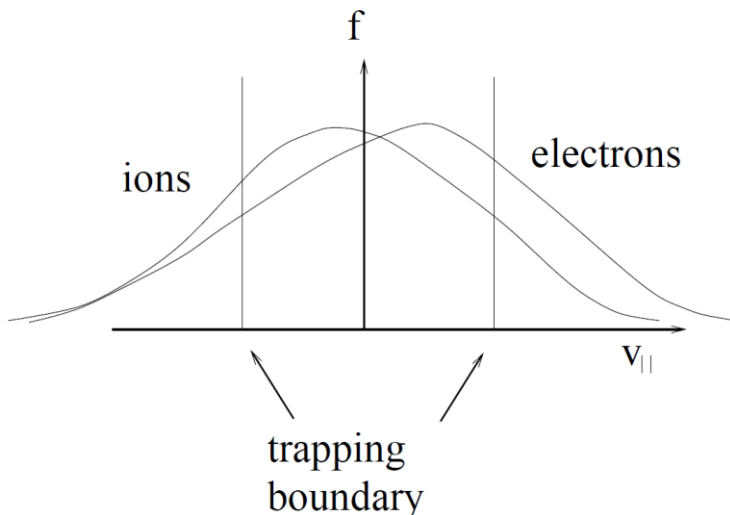
Bootstrap current is generated when passing particles are scattered by the trapped particles



- Scattering smooths the velocity distribution and shifts it in the parallel direction, i.e., a current is generated. It is called the bootstrap current.

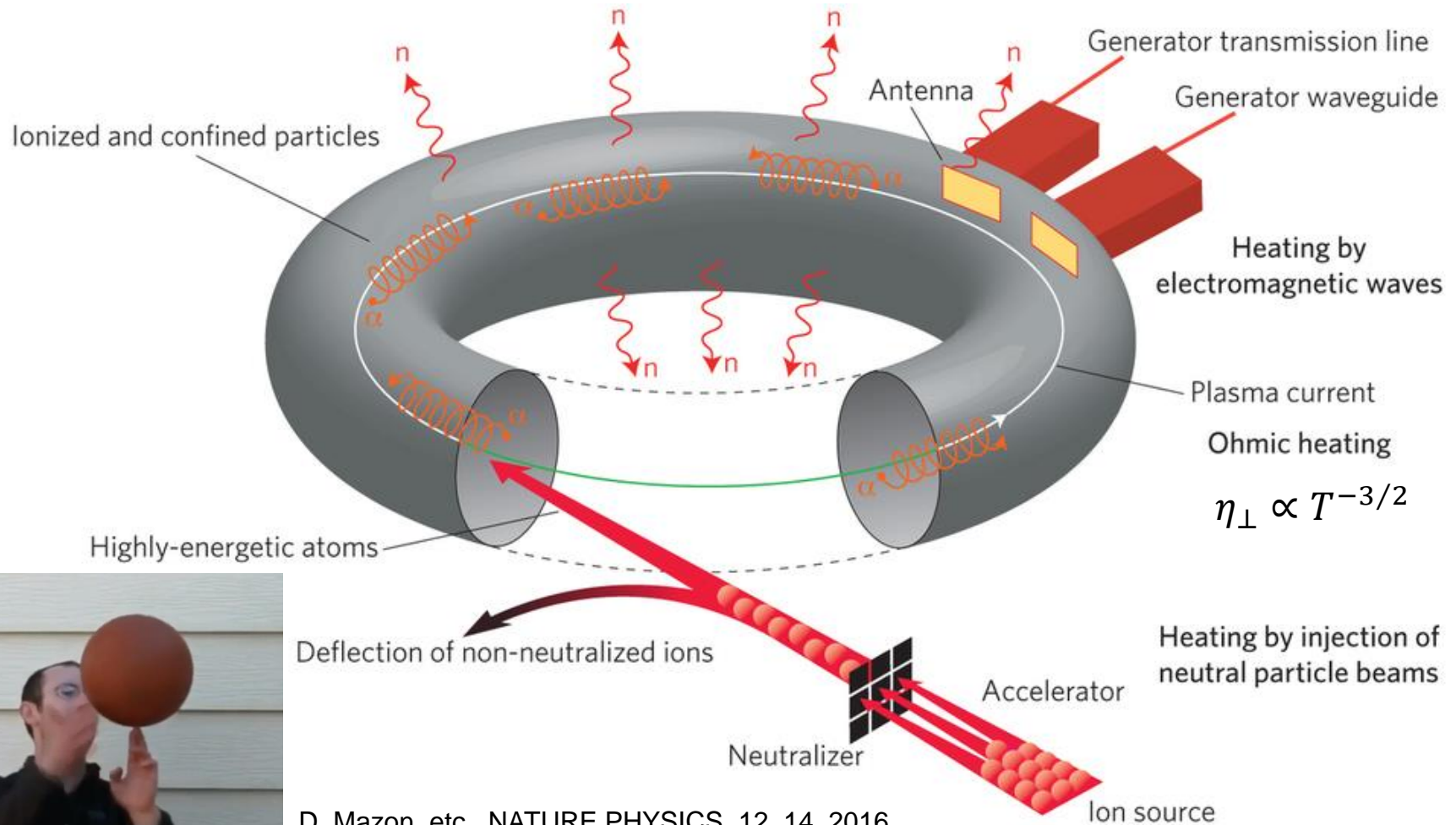


$$\mathbf{j} = -en\mathbf{u}_{||e} + en\mathbf{u}_{||i} = 4\epsilon^{3/2} \frac{1}{B_p} T \frac{dn}{dr}$$



- The bootstrap current is vital for steady-state operation.

Neutral beam injector is one of the main heat mechanisms in MCF



D. Mazon, etc., NATURE PHYSICS, 12, 14, 2016

<https://zh.wikihow.com/%E5%9C%A8%E6%89%8B%E6%8C%87%E4%B8%8A%E8%BD%AC%E7%AF%AE%E7%90%83>



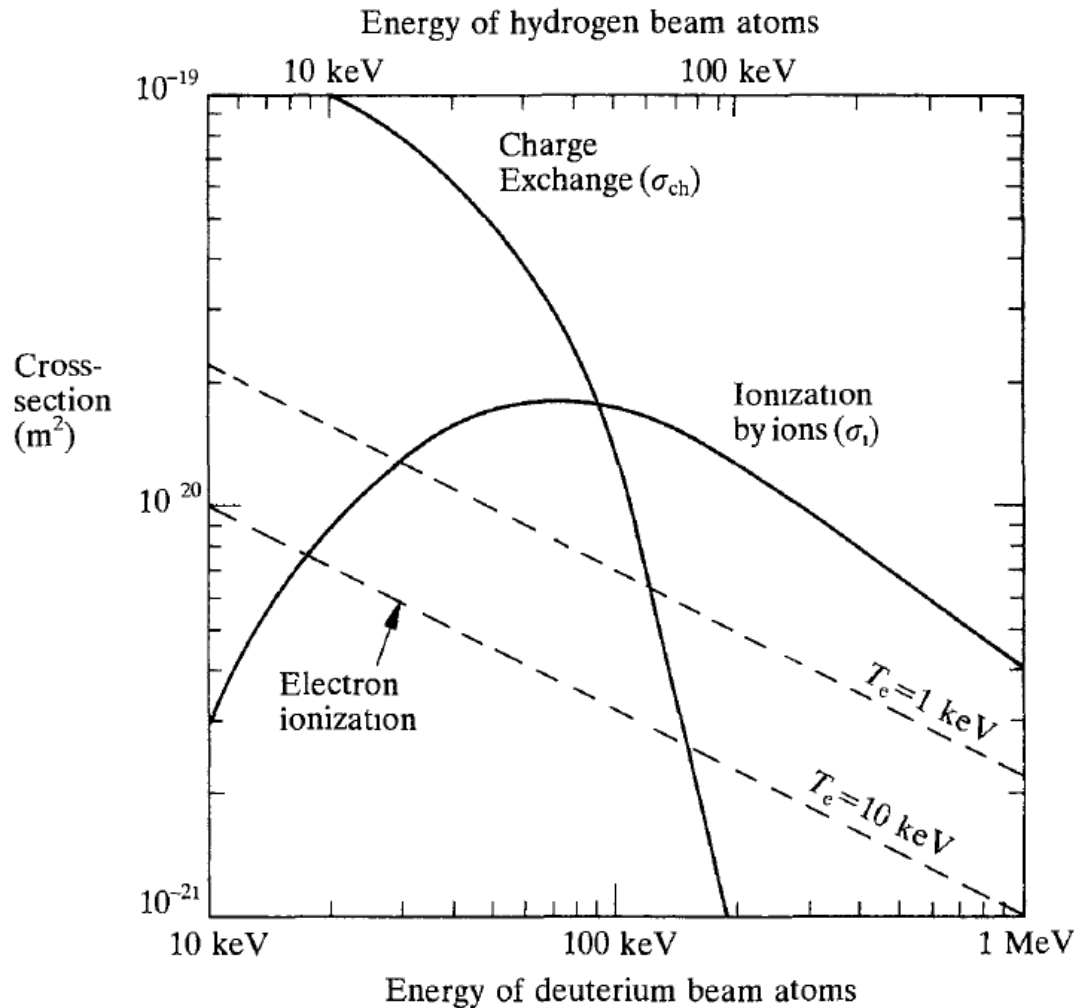
Varies way of heating a MCF device



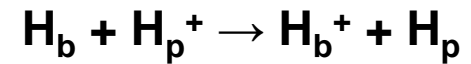
	System	Frequency/ energy	Maximum power coupled to plasma	Overall system efficiency	Development/ demonstration required	Remarks
ECRF	Demonstrated in tokamaks	28–157 GHz	2.8 MW, 0.2 s	30–40%	Power sources and windows, off-axis CD	Provides off-axis CD
	ITER needs	150–170 GHz	50 MW, SS			
ICRF	Demonstrated in tokamaks	25–120 MHz	22 MW, 3 s (L-mode); 16.5 MW, 3 s (H-mode)	50–60%	ELM tolerant system	Provides ion heating and smaller ELMs
	ITER needs	40–75 MHz	50 MW, SS			
LHRF	Demonstrated in tokamaks	1.3–8 GHz	2.5 MW, 120 s; 10 MW, 0.5 s	45–55%	Launcher, coupling to H-mode	Provides off-axis CD
	ITER needs	5 GHz	50 MW, SS			
NBI	+ve ion Demonstrated in tokamaks	80–140 keV	40 MW, 2 s; 20 MW, 8 s	35–45%	None	Not applicable
	ITER needs	None	None			
	–ve ion Demonstrated in tokamaks	0.35 MeV	5.2 MW, D ⁺ , 0.8 s (from 2 sources)	~37%	System, tests on tokamak, plasma CD	provides rotation
	ITER needs	1 MeV	50 MW, SS			

‘SS’ indicates steady state

Neutral atoms are ionized by collisions in the plasma



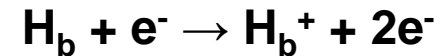
- Charge exchange:



- Ionization by ions



- Ionization by electrons

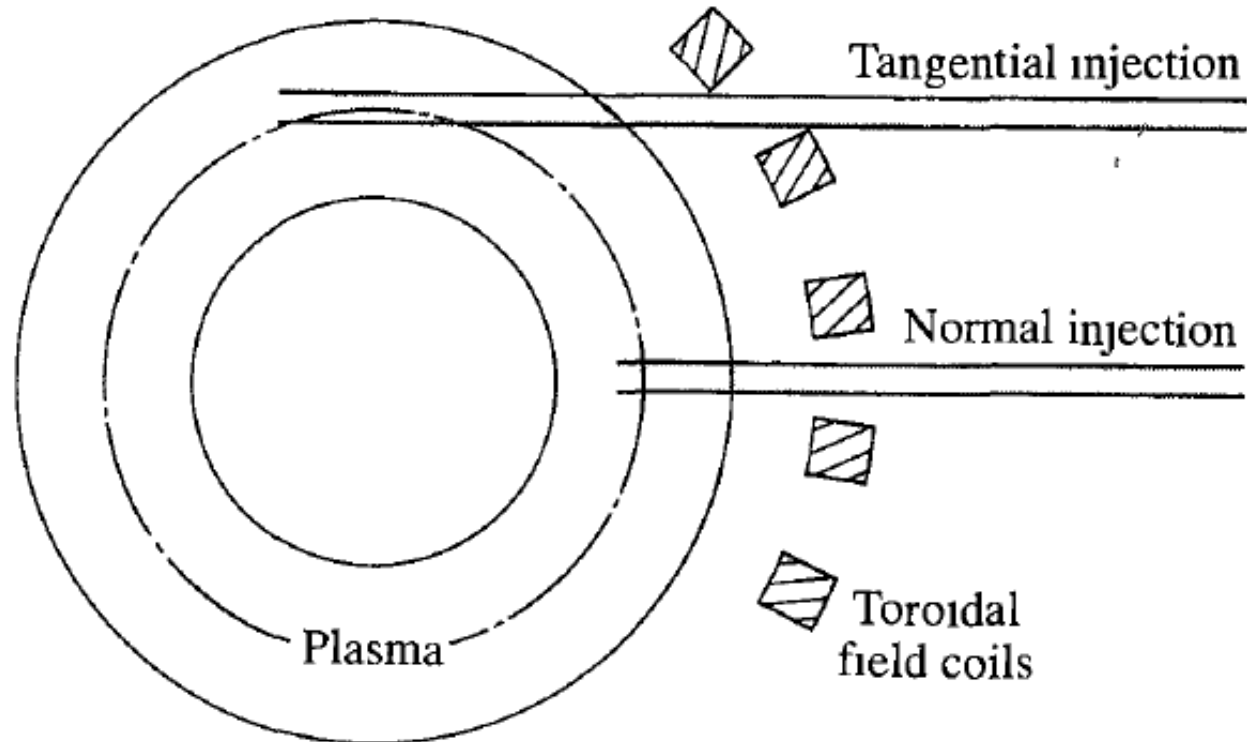


b: beam
p: plasma

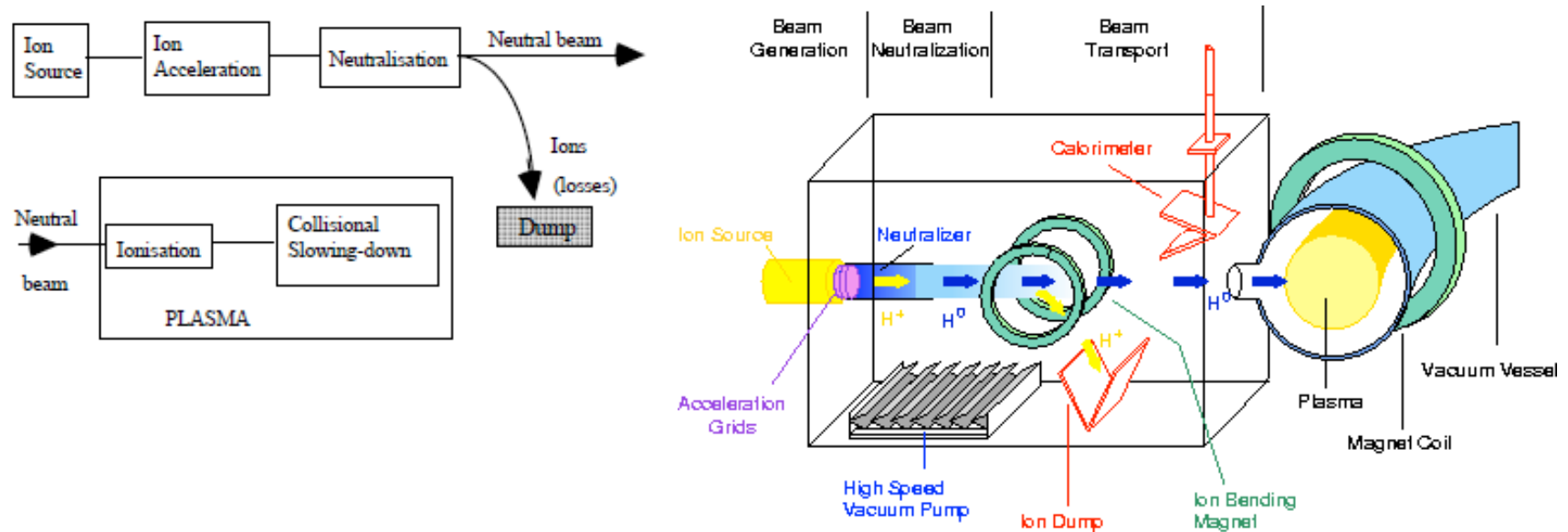
Neutral beam absorption length increases with tangential injection



- It is more difficult to access through the toroidal field coils with tangential injection.

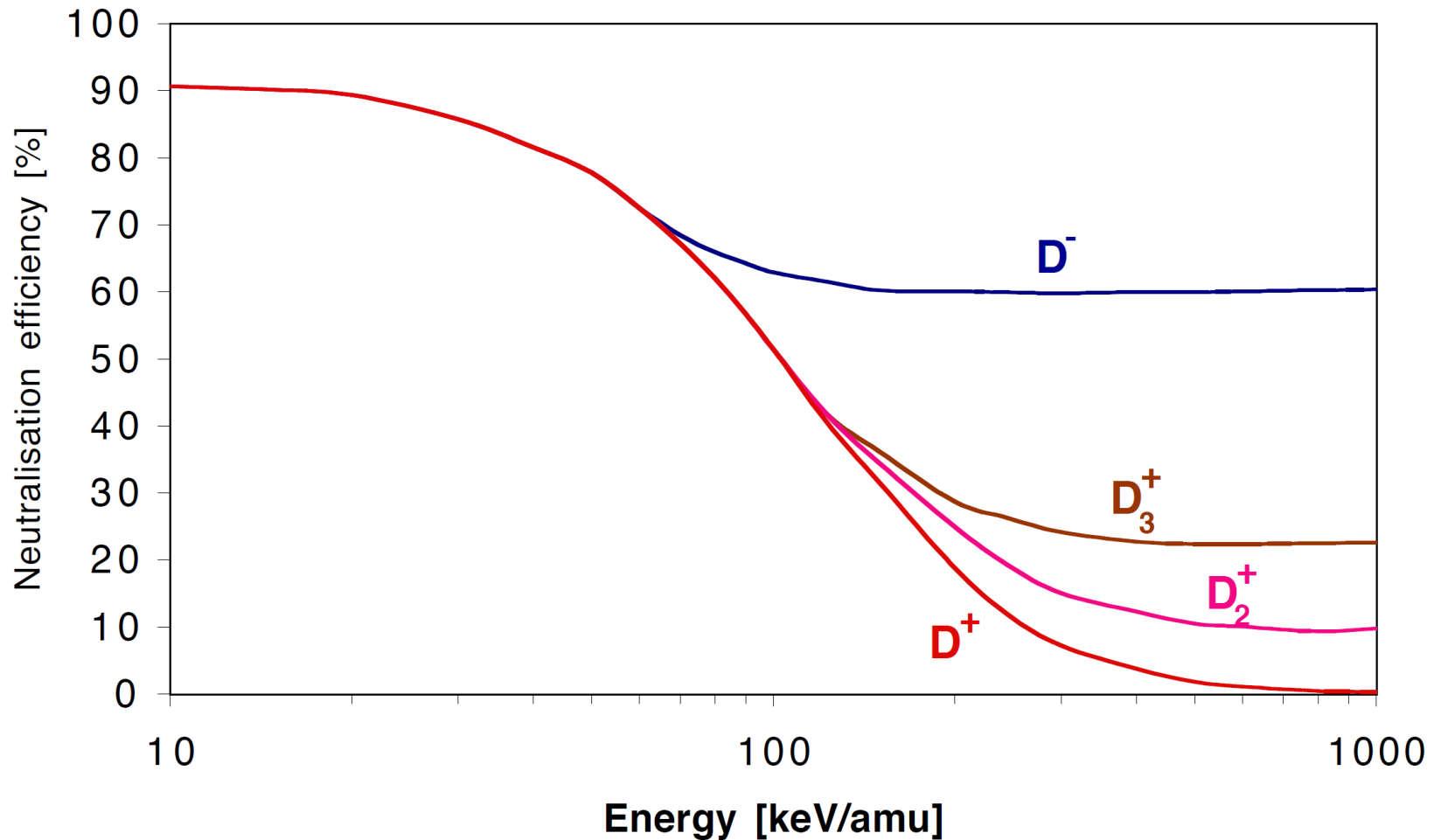


Neutral particles heat the plasma via coulomb collisions



1. create energetic (fast) neutral ions
2. ionize the neutral particles
3. heat the plasma (electrons and ions) via Coulomb collisions

Negative ion source is preferred due to higher neutralization efficiency

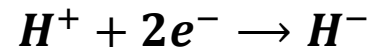
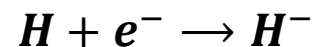
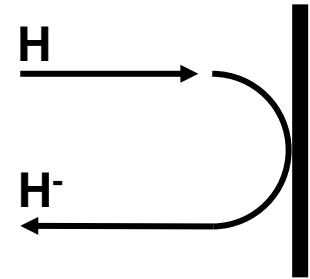


There are two ways to make negative ions – surface and volume production

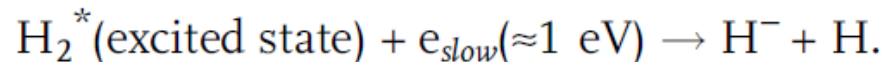
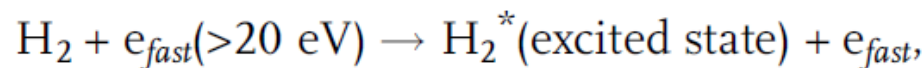


- **Surface production, depends on :**

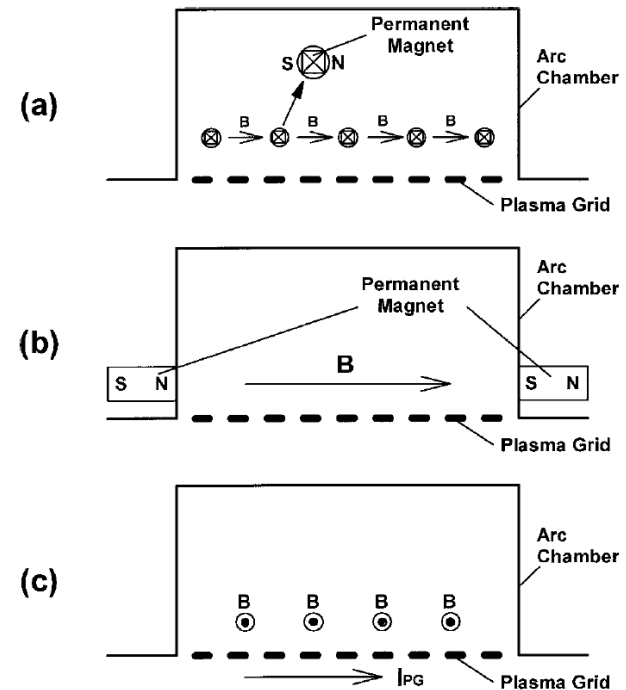
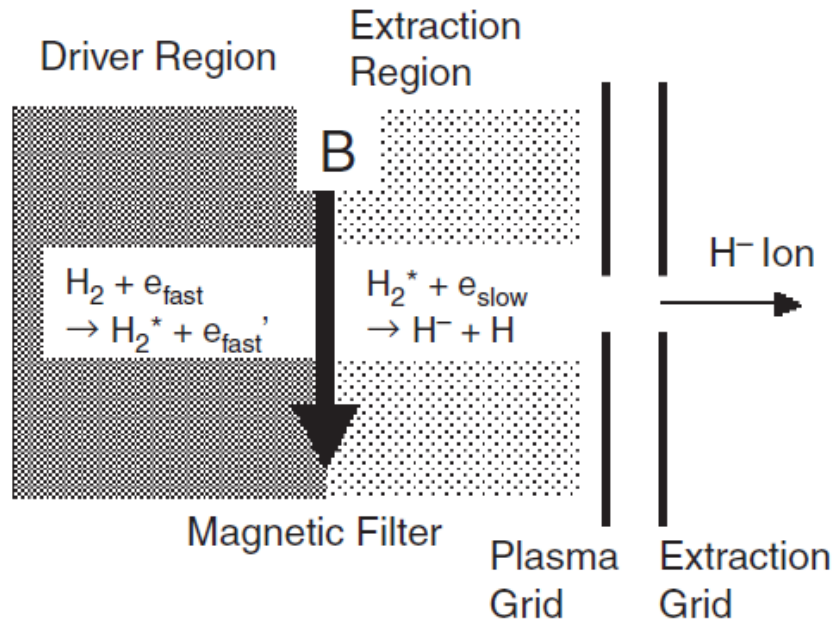
- Work function Φ
- Electron affinity level, 0.75 eV for H^-
- Perpendicular velocity
- Work function can be reduced by covering the metal surface with cesium



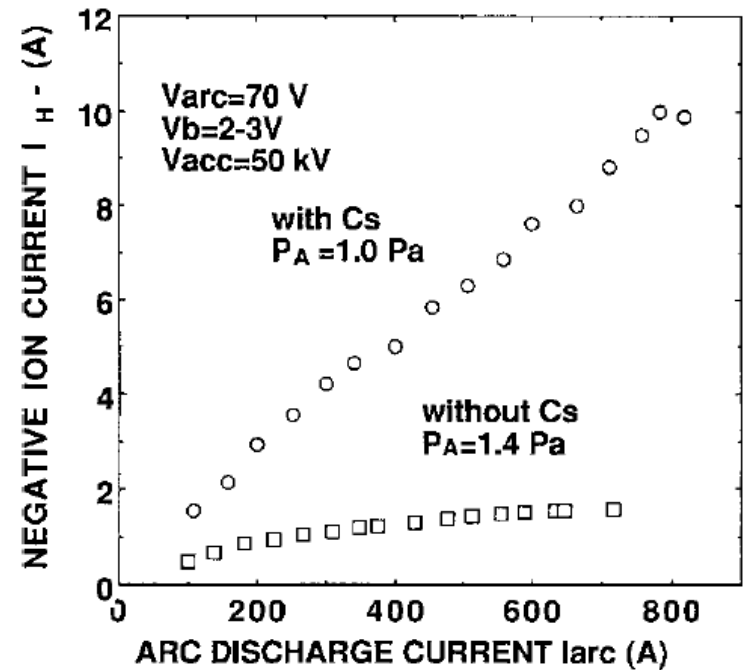
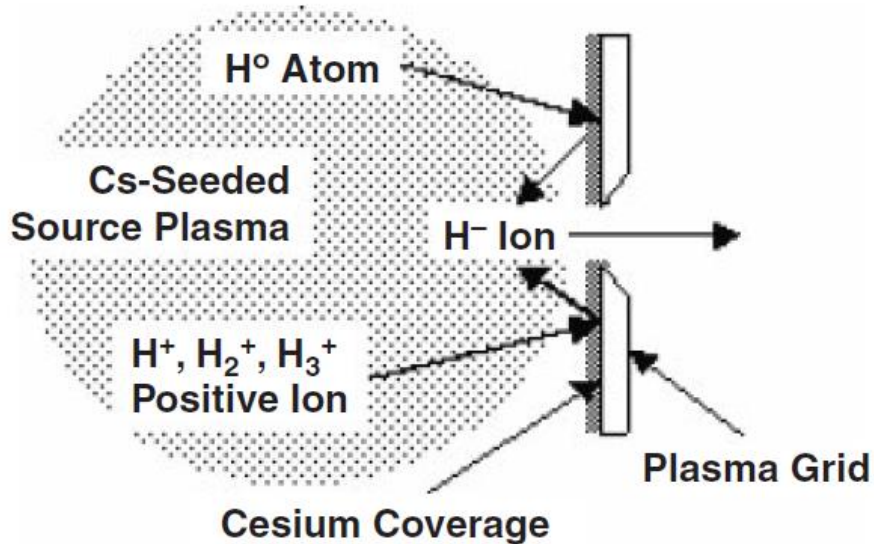
- **Volume production:**



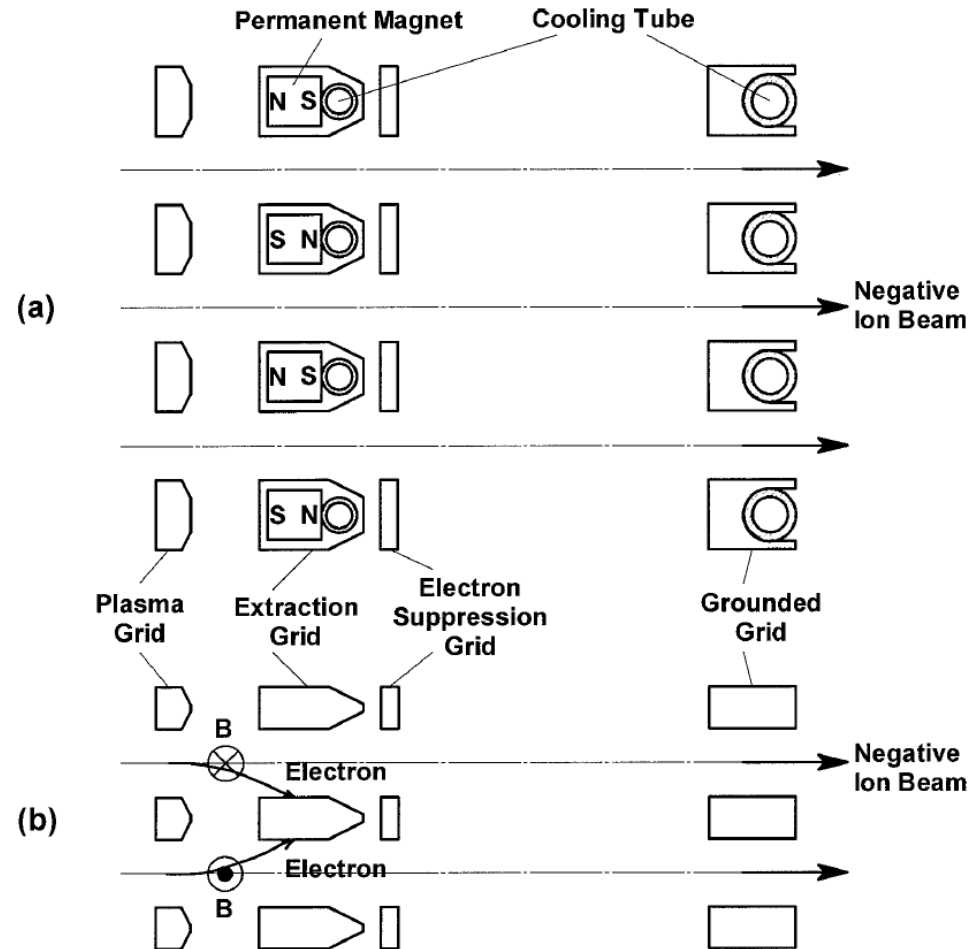
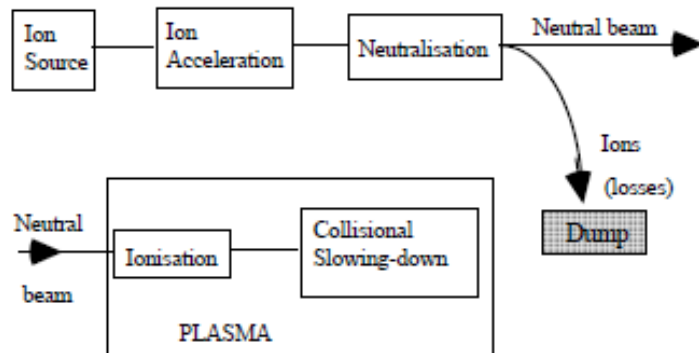
Two-chamber method of negative ions in volume production with a magnetic filter



Adding cesium increases negative ion current



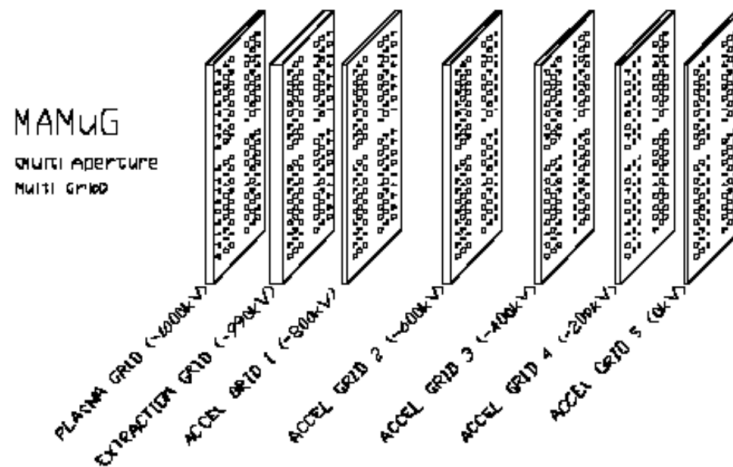
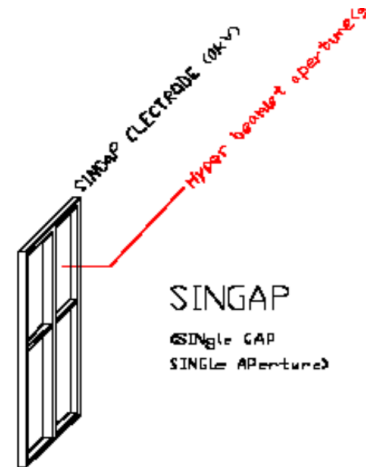
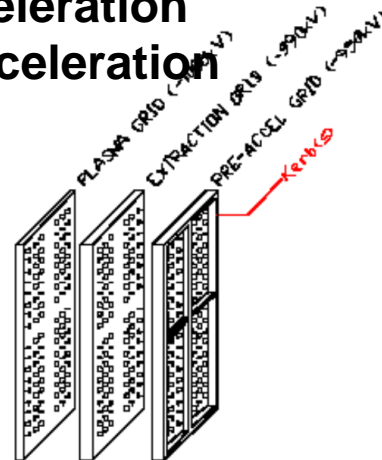
Electrons need to be filtered out since they are extracted together with negative ions



Acceleration

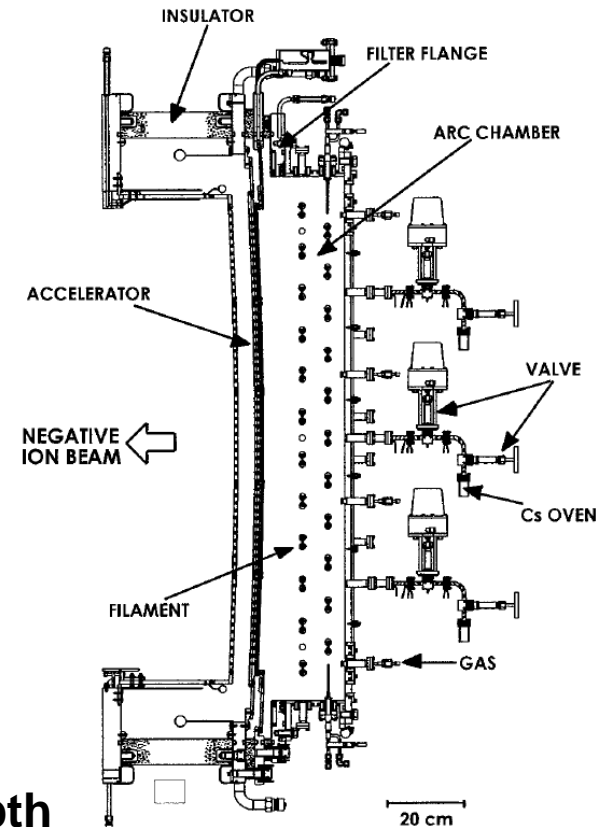
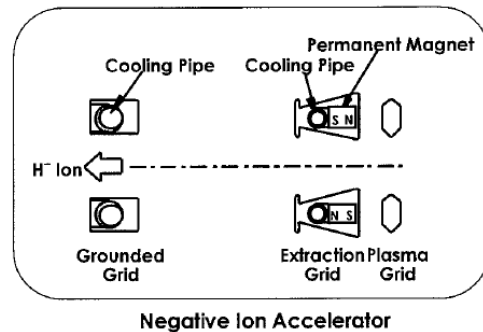


- Multi-stage acceleration
- Single-stage acceleration



The ITER neutral beam system: status of the project and review of the main technological issues, presented by V. Antoni

NBI system of the LHD fusion machine

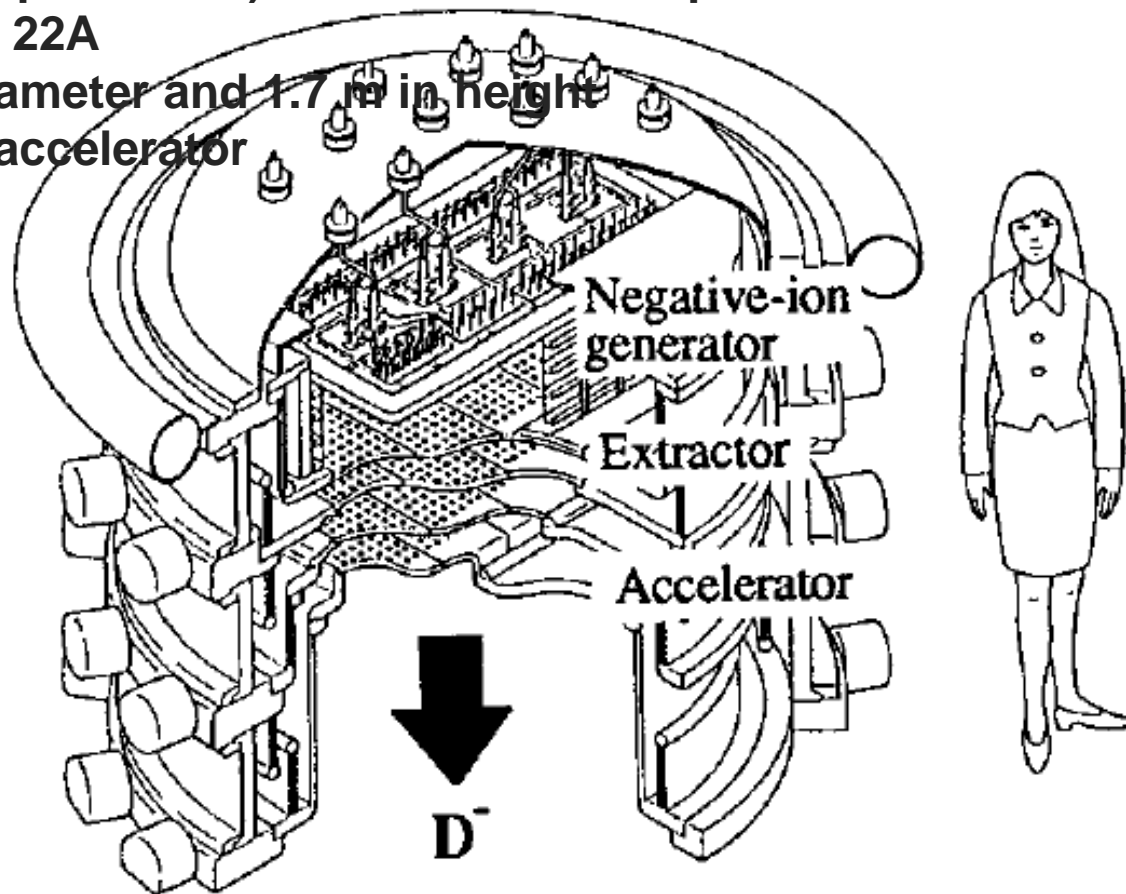


- 180 keV and 30 A
- Arc chamber: 35 cm x 145 cm, 21cm in depth
- Single stage accelerator

JT60U NBI system



- JT-60 (Japan-Torus) is a tokamak in Japan.
- 550 keV, 22A
- 2m in diameter and 1.7 m in height
- 3-stage accelerator

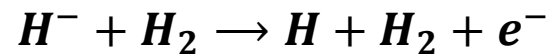


Neutralization



- **Gas neutralization**

- **Collisions between fast negative ions and atoms**

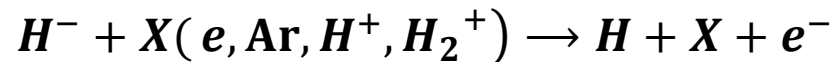


- **Fast ions can lose another electron after neutralized**



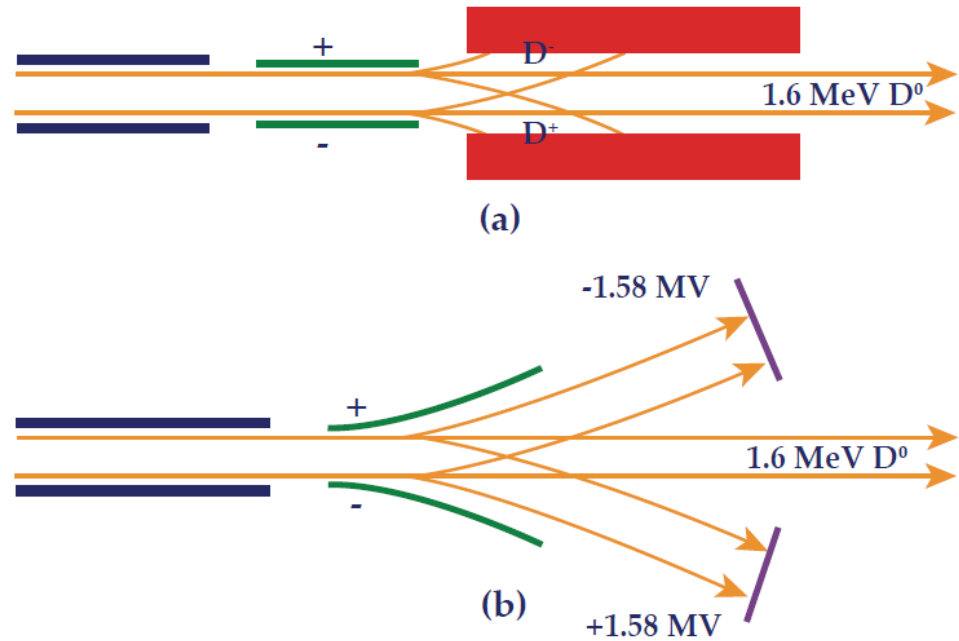
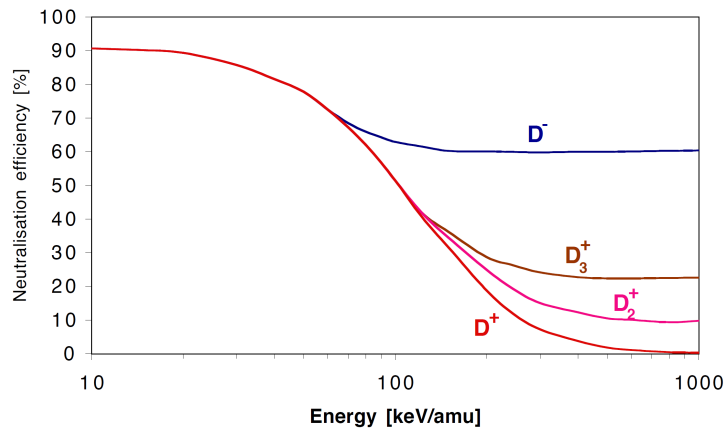
- **Plasma neutralization**

- **Collisions with charged particles in plasma**



- **The efficiencies reach up to 85% for fully ionized hydrogen plasma**

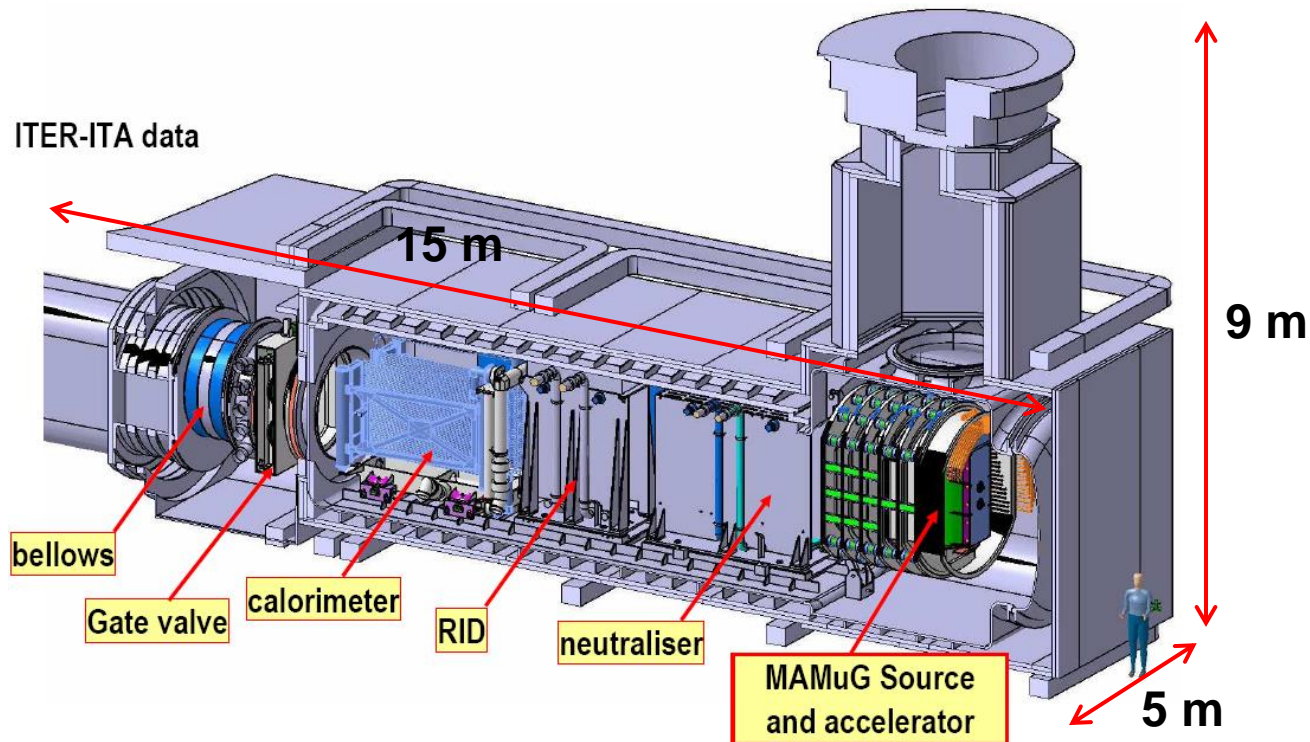
Beam dump



NBI for ITER

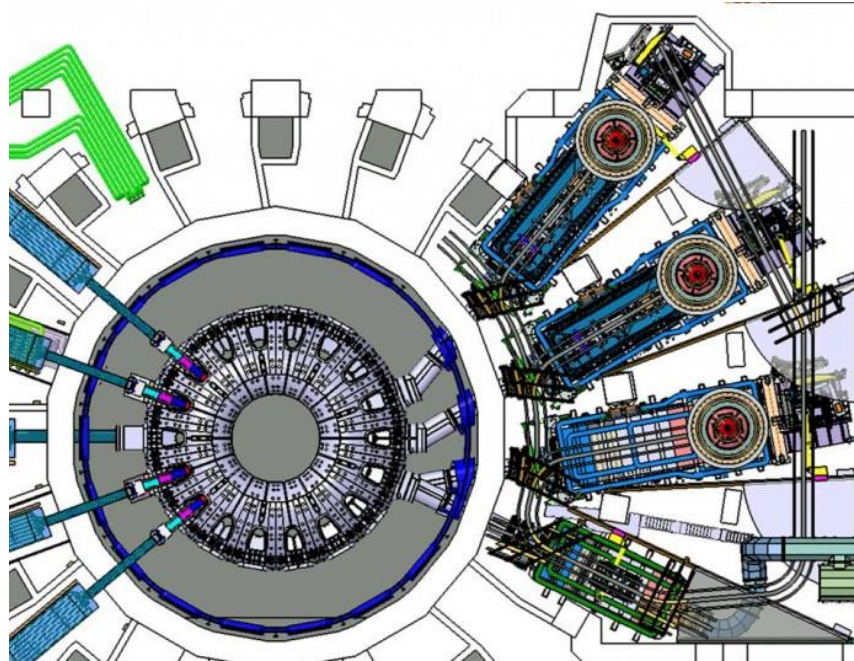


- beam components (Ion Source, Accelerator, Neutralizer, Residual Ion Dump and Calorimeter)
- other components (cryo-pump, vessels, fast shutter, duct, magnetic shielding, and residual magnetic field compensating coils)



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Neutral beam penetration



- **Parallel direction**
 - Longest path through the densest part of the plasma
 - Harder to be built
- **Perpendicular direction**
 - Path is short
 - Larger perpendicular energies leads to larger losses
 - Easier to be built